Two Dynamical Classes of Centaurs

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Abstract

The Centaurs are a transient population of small bodies in the outer solar system whose orbits are strongly chaotic. These objects typically suffer significant changes of orbital parameters on timescales of a few thousand years. For the known sample of Centaurs, our investigation has revealed two types of orbital evolution: (1) random walk-type behavior consistent with so-called generalized diffusion in which the rms deviation of the semimajor axis grows with time $t$ as $\sim t^H$, with $H$ in the range 0.22–0.95, and (2) intermittent resonance sticking with sudden jumps from one mean motion resonance to another, in which $H$ is poorly defined. We find that these two types of behavior are correlated with Centaur dynamical lifetime: most Centaurs whose dynamical lifetime is less than $\sim 22$ Myr exhibit diffusion, whereas most Centaurs of longer dynamical lifetimes exhibit intermittent resonance sticking.

1. Introduction

The Centaurs are a dynamical class of small bodies in the outer solar system whose orbital parameters lie in a range intermediate between those of the Kuiper belt and of the Jupiter-family comets. Numerical simulations have found that the Centaurs are typically removed from the solar system on timescales of only a few million years (Levison and Duncan, 1997; Dones et al., 1996; Tiscareno and Malhotra, 2003; Horner et al., 2004). These dynamical lifetimes are very short compared to the age of the solar system,
implying that the Centaurs are a transitional population with a source elsewhere in the system. Likely source populations are the several dynamical subclasses of the Kuiper belt beyond Neptune (Levison and Duncan, 1997; Volk and Malhotra, 2008). Possible sinks of the Centaur population include the Kuiper belt’s scattered disk, the Jupiter-family comets, and the Oort cloud; Centaurs are also removed from the solar system by collisions with a planet or by ejection on hyperbolic orbits. Numerical analysis of their orbital evolution shows that these objects typically suffer frequent close encounters with the giant planets and their orbits are strongly chaotic. The present study aims to characterize the dynamics of Centaurs by quantitative analysis of the range of behavior in their orbital evolution and by identifying the processes that can produce these behaviors.

To characterize the orbital evolution of Centaurs, we have carried out a 100 million year (Myr) numerical integration of the observed Centaurs. This length of time is more than ten times the median dynamical lifetimes of Centaurs found in previous studies. By analyzing the variations in semimajor axis over a broad range of timescales, we find two distinct modes of behavior, suggesting that the Centaurs may be comprised of two dynamical classes. The first is characterized by a diffusion-like random walk in orbital element space. The second is characterized by resonance sticking, in which Centaurs become temporarily trapped in mean motion resonances with the giant planets. These Centaurs typically hop from one resonance to another for much of their dynamical lifetimes. These two types of behavior are strongly correlated with Centaur lifetime.

This paper is organized as follows. We summarize previous studies of Centaur dynamics in section 2. In section 3, we describe the numerical simulations we have carried out to explore the orbital evolution of Centaurs. Section 4 describes the analyses that we have applied to the results of our simulations. In section 5 we provide a summary and conclusions.

2. Previous Work

The Minor Planet Center (MPC) defines Centaurs as “objects [with] perihelia beyond the orbit of Jupiter and semimajor axes inside the orbit of Neptune” (http://www.cfa.harvard.edu/iau/lists/Unusual.html). The MPC provides a combined list of Centaurs and scattered disk objects. (The latter are not defined on the MPC’s webpages but are generally identified as objects with perihelia near or slightly beyond Neptune’s orbit and semimajor axes
greater than 50 AU.) While there is thus a general consensus on the lower bound for Centaur orbits (although Gladman et al. (2008) propose a higher cutoff of \( q > 7.35 \) AU to exclude objects whose dynamics are controlled by Jupiter), the upper bound is open for interpretation. The samples of Centaurs studied by different authors thus vary slightly based on the authors’ chosen criterion, with some authors constraining semimajor axis only and others using constraints based also on perihelion and aphelion distance.

The first Centaur was discovered in 1977 (Kowal, 1989), but only in the past decade or so has there been sufficient computing power to explore their dynamical behavior using large-scale integrations of particle orbits. Dones et al. (1996) simulated the orbital evolution of \( \sim 800 \) particles “cloned” from the six Centaurs known at that time that had values of semimajor axis \( a \) between 6 and 25 AU. The initial orbital elements of each particle were identical to those of one of the Centaurs, save for the addition of a random variation in \( a \) of order \( 10^{-5} \) AU. They focused on the dynamical lifetimes of the particles, and found median lifetimes of 0.5 to 5 Myr for their six ensembles of clones. Lifetime was most sensitive to perihelion distance: at smaller perihelion, particles are more likely to encounter one of the more massive planets and receive large gravitational “kicks”, and thereby be removed from the Centaur population. They also reported that the number of surviving particles in each ensemble decreased at first roughly exponentially with time, then more slowly as a power law.

In work published in 1997, Levison and Duncan followed the evolution of a sample of hypothetical Kuiper belt objects as they evolved their way inward toward the Sun to become Jupiter-family comets. A subset of their sample thus spent time as Centaurs. These authors argued that a dynamical classification based on Tisserand parameter \( T_p \) is more appropriate for objects on planet-encountering orbits than the traditional divisions based solely on semimajor axis (or equivalently, orbital period). The Tisserand parameter is defined in the context of the circular restricted 3–body problem, and is given by

\[
T_p = \frac{a_p}{a} + 2 \sqrt{\frac{a}{a_p} (1 - e^2) \cos i},
\]

where \( a_p \) is the semimajor axis of the planet, \( a \) and \( e \) are the semimajor axis and eccentricity of the small body in the heliocentric frame, and \( i \) is the inclination of the small body relative to the orbit of the planet. The Tisserand parameter is nearly constant for a given particle before and after
an encounter with a planet. Note that when \( i = 0, e = 0, \) and \( a = a_p, \) then \( T_p = 3, \) so values of \( T_p \) near 3 indicate that the orbit of the particle is similar to the orbit of that planet, and the planet can strongly influence the orbit of the particle. In particular, Levison and Duncan identify the Centaurs with what they call Chiron-type comets, defined by \( T_J > 3 \) and \( a > a_J, \) where \( T_J \) is the Tisserand parameter with respect to Jupiter and \( a_J = 5.2 \) AU is the semimajor axis of Jupiter. Jupiter-family comets are defined as objects with \( 2 < T_J < 3. \)

Levison and Duncan’s results suggested that Centaurs can become Jupiter-family comets by being “handed” inward from one planet to the next through a series of close encounters. Based on the approximate conservation of \( T_p \) and their assumed initial values of \( a, e, \) and \( i \) for their hypothetical source population in the Kuiper belt, they calculated that, starting with Neptune, each planet could scatter a small body just far enough inward to reduce its perihelion distance so that the body could cross the orbit of the next planet in. About 30% of the particles in their integrations did become Jupiter-family comets.

More recently, Tiscareno and Malhotra (2003) carried out a study of the dynamics of all of the known Centaurs as of 2002. Their numerical simulation included the four giant planets and 53 Centaurs, the latter treated as massless test particles, and they followed the orbits for 100 Myr. They chose their sample of Centaurs based on perihelion distance alone, using the criterion \( 5.2 < q < 30 \) AU. Particles were removed from the simulation when they reached either \( r > 20,000 \) AU or \( r < 2.5 \) AU. From this simulation, they found a median dynamical lifetime of 9 Myr, longer than but on the same order as the lifetimes found by Dones et al. (1996). Only 7 of the 53 particles (13%) survived the full 100 Myr integration.

Tiscareno and Malhotra also observed qualitatively different types of behavior over time, as indicated by time series plots of semimajor axis for different particles. They described these as “resonance hopping” and “random fluctuations,” with some particles exhibiting a combination of both. This work provides the motivation and starting point for our own work, described in section 3, in which we found similar types of behavior among the Centaurs.

Horner et al. (2004) have also investigated the dynamical evolution of Centaurs. They integrated the orbits of 23328 particles cloned from 32 Centaurs, for 3 Myr both forward and backward in time. From their results, they extrapolate half-lives of 0.5 to 32 Myr for each Centaur, defined as the time when half of the ensemble of clones of that Centaur have been removed.
from the simulation by either colliding with a massive body or reaching a heliocentric distance of 1000 AU. They also estimate a total population of \( \sim 44300 \) Centaurs with diameters greater than 1 km, based on the fraction of particles in their simulation that become short-period comets and an assumed flux of one new short-period comet every 200 years. The authors propose a classification scheme for Centaurs based on both perihelion and aphelion, suggesting that whichever planet is nearest at those parts of the orbit controls the dynamics of the Centaur. This results in 18 dynamical classes for objects with perihelia between 4 and 33.5 AU. While the defining assumption is reasonable for a very detailed description, the number of categories is probably too large for the purpose of describing the big picture of Centaur dynamics.

3. Simulations

Our orbital integrations were done using the RA15 integrator (Everhart, 1985), a 15th-order variable step size method for ordinary differential equations, which is part of the public-domain software package *Mercury* (Chambers, 1999), designed for N-body integrations for planetary dynamics applications. Everhart’s orbit integrator has often been used for cometary orbits and is very stable for large eccentricities and close planetary encounters; the price for its high accuracy is its larger computational time requirement, compared to the lower accuracy hybrid symplectic method also offered in the Mercury package. As numerical accuracy was a priority for the analysis of the strongly chaotic orbit evolution, and our simulation involved only a small number of known Centaurs, the penalty in computational time was not prohibitive. We used a relative position and relative velocity error tolerance of \( 10^{-12} \).

Our primary simulation included the Sun, the four giant planets, and 63 Centaurs treated as massless test particles. The sizes, masses, and initial positions of the Sun and the giant planets were obtained from JPL Horizons service. The initial conditions for the Centaurs were taken from the Minor Planet Center’s online list of Centaurs and Scattered Disk Objects (http://www.cfa.harvard.edu/iau/lists/Centaurs.html) on 6 March 2007. Our sample is a subset of that list, selected based on the criterion \( q > 5.2 \) AU and \( a < 30 \) AU. Note that this is slightly different from the criterion used by Tiscareno and Malhotra (2003), and excludes more fully the scattered disk objects.
A plot of the initial semimajor axes, eccentricities and inclinations of our sample of Centaurs is shown in Fig. 1. The circles mark the semimajor axes and the horizontal bars on the plot extend from perihelion to aphelion for each Centaur, illustrating the eccentricity of each orbit. As seen in the figure,

the initial inclinations of the Centaurs span the range $3^\circ < i < 40^\circ$. Their eccentricities range from $\sim 0.01$ to 0.68.

We integrated the orbits of the planets and Centaurs for 100 Myr and recorded the evolved orbital elements every 300 years. Centaurs were removed from the simulation when they either collided with a massive object (planet or Sun) or reached a heliocentric distance of $10^4$ AU; we refer to the latter as ‘ejected’.

Our simulations confirmed the two types of behavior noted by Tiscareno and Malhotra (2003). Sample results are shown in Fig. 2. In the top panel,
Figure 2: Two examples of Centaur orbital evolution. Top panel: a particle undergoing a random walk; bottom panel: a particle engaged in resonance hopping. Note the different scales for the two panels.
2002 CB249 follows a random walk in semimajor axis. In the bottom panel, the orbital evolution of 1998 TF35 is dominated by resonance hopping. Note that due to the chaotic nature of the orbital evolution for all Centaurs, these plots should not be taken as predictions of the actual future evolution of particular objects, but only as examples of the types of behavior that can occur. Both objects reach semimajor axes \( a > 30 \) AU during their lifetimes, thus leaving the Centaur region.

Of our initial sample of 63 test particles, all but one spent part of their lifetimes as members of other dynamical classes, including scattered disk objects, resonant Kuiper belt objects, and Jupiter-family comets. The exception (2006 RJ103) was identified as a Neptune Trojan and we discarded it from further analysis. Nine others survived the full 100 Myr integration. A histogram of the dynamical lifetimes of our sample of particles is shown in Fig. 3. The first large gap in lifetimes occurs between 22 Myr and 38 Myr.

![Histogram of dynamical lifetimes](image)

Figure 3: The distribution of dynamical lifetimes for our sample of particles. The nine Centaurs that survived the full 100 Myr integration are not shown.
Based on this gap, we have designated all particles that survived more than 22 Myr as “long-lived” particles, a total of 15 objects. One of these (2005 TH173) appeared to be in a quasi-stable orbit between Saturn and Uranus for almost the entire integration; we describe this exceptional case in section 4.3. Those particles that survived less than 22 Myr before being removed from the simulation are designated as “short-lived”.

The median lifetime for particles in our simulation was 6 Myr, similar to the value of 9 Myr found by Tiscareno and Malhotra (2003) and close to the longest dynamical lifetimes found by Dones et al. (1996). The larger value found by Tiscareno and Malhotra is likely due to the fact that they included objects with initial $a > 30$ AU, which likely belong in the scattered disk classification and may have survived longer due to fewer encounters with planets.

4. Analysis

In this section we describe our analysis of the two distinct types of behavior seen in the results of our simulation: random walks and resonance hopping.

4.1. Generalized Diffusion

If a particle undergoes a random walk with either fixed or normally distributed stationary independent increments, its mean square displacement from the origin $\langle x^2 \rangle$ at time $t$ grows linearly with $t$. In the limit as the step sizes approach 0, this process leads to Brownian motion (Einstein, 1905). Recent work has extended this framework to generalized diffusion (Weeks and Swinney, 1998; Metzler and Klafter, 2000; Cordeiro, 2006), in which

$$\langle x^2 \rangle = Dt^{2H}, \quad \text{for } 0 < H < 1,$$

where $D$ is a generalized diffusion coefficient and $H$ is called the Hurst exponent. In the case of $H \neq \frac{1}{2}$, the random process is called anomalous diffusion, and it occurs if the steps are correlated in some way. The degree of correlation is related to the deviation of $H$ from the classical diffusion value of $\frac{1}{2}$.

As noted above, many of the particles in our simulations appear to follow a random walk in semimajor axis. We have analyzed the diffusion characteristics of our sample of Centaurs by calculating the Hurst exponent of each
Centaur based on the time series of its semimajor axis. Since the orbital energy per unit mass is related to semimajor axis \( (E \propto \frac{1}{a}) \), \( a \) is a proxy for the orbital energy and provides a useful measure of the orbital evolution. The steps in our analysis for orbital diffusion of Centaurs are as follows:

1. Choose a window length \( w \), corresponding to a fixed time interval.
2. Apply overlapping windows of length \( w \) to the data set. Each window was allowed to overlap its neighbors by half its length. If the amount of data not included in any window was greater than \( \frac{1}{4} \) the window length, an additional window was applied to cover the end of the data set.
3. Calculate the standard deviation \( \sigma \) of \( a \) within each window.
4. Find the average standard deviation \( \bar{\sigma}(w) \) for all windows of length \( w \).
5. Repeat steps 1-4 for different window lengths.
6. Plot \( \log \bar{\sigma}(w) \) vs. \( \log w \). The slope of the best fit line is an estimate of the Hurst exponent, \( H \).

The window lengths were chosen uniformly in logarithmic bins, from 3000 years up to the length of the data set. Any windows larger than 25% of the data set were then discarded to minimize errors.

Results of this calculation for the two Centaurs shown in Fig. 2 are presented in Fig. 4. The upper panel illustrates an example of generalized diffusion, in which the plot of \( \log \bar{\sigma} \) vs. \( \log w \) is well fitted by a straight line; in this case, the calculated Hurst exponent is \( H = 0.48 \). In the lower panel, the dependence of \( \log \bar{\sigma} \) on \( \log w \) is smoothly curved rather than linear, so \( H \) is poorly defined in this case.

Our results for this calculation for all the Centaurs in our simulation are shown in Fig. 5.

In the left-hand panel, the plots of \( \log \bar{\sigma} \) vs. \( \log w \) for the short-lived Centaurs are generally well fitted by lines of constant slope, indicating that generalized diffusion is a good model for the orbital evolution of these particles; the values of \( H \) for this group range from 0.22 to 0.95, with mean 0.56 and standard deviation 0.15.

In the right-hand panel of Fig. 5, the plots of \( \log \bar{\sigma} \) vs. \( \log w \) for most of the long-lived Centaurs are smoothly curved rather than straight. Note also that the values of \( \bar{\sigma} \) are typically lower for this group of Centaurs than for the group in the left panel. The “curved” group have residuals to a best-fit linear function that can exceed 0.08 with a clear pattern of positive values at
Figure 4: Log-log plots of $\bar{\sigma}$ vs. $w$ for the two sample Centaurs shown in Fig. 2. The dotted lines indicate the best-fit linear function. The uncertainties in $H$ are quoted at the 1-\(\sigma\) level.
Figure 5: Log-log plots of $\bar{\sigma}$ vs. $w$ for particles in our simulation. Left panel: short-lived Centaurs; right panel: long-lived Centaurs. The dotted line in each panel is a reference line with slope $H = \frac{1}{2}$. 
the ends and negative values in the middle. These Centaurs’ evolution is not well described by a generalized diffusion process. We discuss this further in section 4.2. Two objects in this plot lie well above the rest, indicating large values of $\bar{\sigma}$ for all time intervals. These objects are discussed in section 4.3.

One mechanism for the diffusion in $a$ is suggested by the plots in the upper panels of Fig. 6, which shows the traces in $(a, e)$ and $(a, i)$ planes. This object, 2002 CB249, is also shown in the top panel of Fig. 2. The plot of $e$ vs. $a$ shows that this particle spends essentially all of its dynamical lifetime at constant perihelion (near Saturn’s orbit), being pumped to higher and higher values of eccentricity until it is ejected from the solar system.

In contrast, as shown in the bottom panels, 1998 TF35 wanders through a small region of the $(a, e)$-plane, but never exceeds $e \approx 0.5$. We also see a contrast in the inclination evolution: 1998 TF35 visits a much wider range of inclinations compared with 2002 CB249. The vertical features indicate times spent in resonance. This pattern is characteristic of resonance hopping, discussed below.

4.2. Resonance Hopping

Of the 15 long-lived Centaurs in our sample, 10 exhibit nonlinear curves of log $\bar{\sigma}$ vs. log $w$, as seen in Fig. 5. At small values of $w$ (i.e., small timescales), the asymptotic slopes of these curves approach 0.06-0.27, with a mean of 0.15. These low values reflect the small variations in semimajor axis on timescales of up to $\sim 10^4$ years. At the high range of values of $w$ (i.e., timescales of $10^6$ years or more), the asymptotic slopes are higher, 0.23-0.85, with mean 0.57; these values are similar to the range of the Hurst exponent for the short-lived Centaurs. This suggests that the generalized diffusion model may still be applicable for this long-lived group, but only over much longer timescales than for the short-lived group.

As illustrated in the bottom panel of Fig. 2, many of the long-lived Centaurs spent considerable portions of time at constant semimajor axis. In many cases, we have identified these time segments as mean motion resonances with the planets. An example is presented in Fig. 7. We identified mean motion resonances by looking for small integer ratios $p : q$ between the orbital periods of the Centaur and the giant planets. Each candidate pair $(p, q)$ was then used to define resonance angles of the form $\phi_a = p\lambda_C - q\lambda_P - (p - q)\varpi_C$ and $\phi_b = p\lambda_C - q\lambda_P - (p - q)\Omega_C$, where $\lambda$ is the mean longitude, $\varpi$ is the longitude of perihelion, $\Omega$ is the longitude of the ascending node, and the subscripts $C$ and $P$ refer to the Centaur and planet,
Figure 6: Plots of $i$ vs. $a$ and $e$ vs. $a$ for two Centaurs. Top: 2002 CB249, a short-lived, diffusion-dominated Centaur; Bottom: 1998 TF35, a long-lived, resonance-hopping Centaur. In the right-hand panels, the overlying curves indicate where the Tisserand parameter $T = 3$ with respect to Jupiter, Saturn, Uranus, or Neptune, for zero inclination orbits.
Figure 7: A selection of mean motion resonances identified for 1998 TF35. The upper trace depicts resonances with Uranus; the lower trace corresponds to resonances with Neptune.
respectively. (It is possible to define many other combinations, involving the $\varpi$ and $\Omega$ angles for the planets; we did not consider those because such resonances are generally weaker due to the much smaller eccentricities and inclinations of the planets compared to those of the Centaurs.) If either $\phi_a$ or $\phi_b$ librates, then $p : q$ is a mean motion resonance.

Most, though not all, of the long-lived Centaurs in our simulation exhibited resonance sticking during a significant fraction of their dynamical lifetimes. Conversely, the short-lived Centaurs spent very little time in resonances. From our results, resonance hopping is a relatively slow mechanism for chaotic orbital evolution, in contrast to the processes that cause the short-lived Centaurs to diffuse rapidly and either be ejected from the solar system or collide with a planet.

4.3. Exceptional Cases

Two curves in the right-hand panel of Fig. 5 lie well above the rest, with values of $\bar{\sigma}$ that are almost an order of magnitude larger than those of the other long-lived Centaurs. The individual results for these objects are shown in Fig. 8 and Fig. 9. These objects, 2003 QC112 and 2006 AA99, spend much of their dynamical lifetimes at large semimajor axis, with large jumps near perihelion passage, and we have not detected any resonance sticking in their evolution. As seen in the bottom panels of each figure, their plots of log $\bar{\sigma}$ vs. log $w$ are nearly linear. These objects are members of the diffusion class rather than the resonance-hopping class, despite being long-lived.

Another object in our sample, 2005 TH173, remained at nearly constant semimajor axis for over 85 Myr (see Fig. 10). It follows a nearly circular, but inclined, orbit between Saturn and Uranus, with $a \simeq 15.8$ AU and inclination $i = 16^\circ$. It is not in a mean motion resonance with either Saturn or Uranus. Its log $\bar{\sigma}$ vs. log $w$ curve is the lowermost line in the right-hand panel of Fig. 5 and has slope zero. This object could be a candidate for long sought but hitherto undiscovered long-lived orbits between the orbits of the giant planets. To explore the stability of this orbit further, we numerically integrated an ensemble of 10 “clones” of 2005 TH173 for 125 Myr. Each clone was randomly assigned an initial semimajor axis in the range $a_0 \pm 10^{-5}$ AU, where $a_0 = 15.724$ AU is the initial semimajor axis of the original object; all other initial orbital elements were identical to that of the original object. For this integration, particles were removed from the simulation when they reached a heliocentric distance of 100 AU, and the evolved orbital elements were recorded every $10^5$ years. As shown in Fig. 11, every clone survived at
least 22 Myr in the same orbit, with the longest lasting more than 110 Myr.

4.4. Correlations

We have explored in some detail how the initial conditions of the Centaurs are correlated with their dynamical behavior. The mean values of initial $a$, $i$, and $q$ are slightly larger for the resonance-sticking Centaurs than for the diffusion-dominated Centaurs, but the standard deviations within each group are high enough that these differences are not significant. We measure the degree of correlation among initial conditions using Spearman’s rank
Figure 9: The upper panel shows semimajor axis and perihelion vs. time for 2006 AA99, a long-lived particle with exceptionally large standard deviation in semimajor axis; note the log scale on the vertical axis. The plot of log $\sigma$ vs. log $w$ is shown in the bottom panel.

correlation coefficient, $r$:

$$r = \frac{\langle (x - \bar{x})(y - \bar{y}) \rangle}{\sqrt{\langle (x - \bar{x})^2 \rangle \langle (y - \bar{y})^2 \rangle}}. \quad (3)$$

For the group of ten long-lived resonance-sticking Centaurs, we find weak positive correlations between $a$ and $e$ ($r = 0.52$) and between $e$ and $i$ ($r = 0.67$), and negative correlations between $e$ and $q$ ($r = -0.73$) and $i$ and $q$ ($r = -0.91$). In contrast, we find no correlations among $a$, $e$ and $i$ for the diffusion-dominated Centaurs (maximum $|r| = 0.22$). There is a weak positive correlation between $a$ and $q$ for this group, with $r = 0.67$, and a weak negative correlation between $e$ and $q$, with $r = -0.61$.

We also find weak correlations between absolute magnitude and $e$, $i$, and $q$ for the resonance-sticking Centaurs, with $r = 0.72, 0.71, \text{ and } -0.76$, respec-
Figure 10: A quasistable object between Saturn and Uranus. The top and middle panels show the time evolution of semimajor axis, perihelion, and inclination; the bottom panel shows the analysis of log $\bar{\sigma}$ vs. log $w$ for the first 80 Myr of the particle’s dynamical lifetime.
Figure 11: A plot of semimajor axis vs. time for an ensemble of ten clones of 2005 TH173. The asterisks indicate the endpoints of the orbital evolution for each clone.
atively. There are no such correlations for the diffusion-dominated group. We see weak negative correlations between absolute magnitude and the Tisserand parameters with respect to Jupiter, Saturn, and Uranus, with $r \approx -0.7$ in each case, for the resonance-sticking group, but not for the diffusion-dominated group. The strongest correlations are between $i$ and Tisserand parameter for the resonance-sticking Centaurs, with values of $-0.92$ for $r(i, T_U)$ and $-0.95$ for $r(i, T_J)$ and $r(i, T_S)$. For the diffusion-dominated Centaurs, the most significant correlation between $i$ and Tisserand parameter is only $r = -0.37$, for $r(i, T_U)$. These results suggest that the diffusing Centaurs are efficiently mixed, erasing information about their origins, but the resonance-hopping Centaurs may be preserving more memory of their source.

We also considered possible correlations with spectral colors of the Centaurs. Tegler et al. (2008) report that the B–R colors of Centaurs are bimodal, with one gray and one red subpopulation, but that these colors show no correlation with orbital elements or absolute magnitude. Only four of our long-lived, resonance-hopping class have published colors; this is too small a data set to test for correlations between color and dynamical class from our sample.

4.5. Link to Jupiter-family Comets

We have also investigated the dynamical link between Centaurs and the Jupiter-family comets (JFCs). Because many of the particles in our simulation reach high inclinations, the definition of JFCs as given by Levison and Duncan (1997), $2 < T_J < 3$, is not sufficient to identify objects whose dynamics are dominated by Jupiter. We therefore adopted a modified definition, as proposed by Gladman et al. (2008), which includes a condition on perihelion distance: $q < 7.35$ AU. This distance is midway between the orbits of Jupiter and Saturn.

Using the modified definition of JFCs, we found that 47 of the 62 particles (76%) spent part of their dynamical lifetimes as JFCs. A histogram of the time spent as a JFC for our sample of particles is shown in Fig. 12. The median time spent as a JFC was $1.6 \times 10^5$ years, comparable to the dynamical lifetimes of JFCs found in other work (Levison and Duncan, 1994). All but one of these 47 were members of the diffusing class of Centaurs. In contrast, 9 out of 10 of the resonance-hopping class never became JFCs. This suggests that the JFCs are supplied by a subset of the Centaurs, the diffusing dynamical class.
Figure 12: Histogram of the time spent as a JFC for the particles in our simulation. Members of the diffusing class are shown in black, while resonance-hopping particles are shown in gray.
5. Summary and Conclusions

Our analysis of the long term orbital evolution of Centaurs shows that these objects can be classified into two dynamical classes: one is characterized by diffusive evolution of semimajor axis and the other is dominated by resonance sticking. This dynamical classification is strongly correlated with dynamical lifetime: all ten of the Centaurs in the resonance-hopping category survived at least 40 Myr, and eight survived the full 100 Myr; in contrast, 46 of the 51 diffusing Centaurs were ejected or collided with a massive body within 22 Myr, more than half of these within 6 Myr.

The resonance-hopping class of Centaurs exhibits weak correlations among the initial orbital elements $a$, $e$, $i$, and $q$, as well as absolute magnitude; no such correlations are found in the diffusive class of Centaurs. There are currently insufficient data on the colors of Centaurs to determine whether the two dynamical classes exhibit different color trends. Our simulations indicate that the diffusing class of Centaurs are far more likely to evolve into Jupiter family comet-type orbits than the resonance-sticking class of Centaurs. More work needs to be done to evaluate the significance of these correlations (or lack thereof), and to understand the origins of the diffusive and resonance-sticking dynamical classes.

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