# The CH<sub>4</sub> structure in Titan's upper atmosphere revisited

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[1] In this study, we reanalyze the  $CH_4$  structure in Titan's upper atmosphere combining the Cassini Ion Neutral Mass Spectrometer (INMS) data from 32 flybys and incorporating several updates in the data reduction algorithms. We argue that based on our current knowledge of eddy mixing and neutral temperature, strong  $CH_4$  escape must occur on Titan. Ignoring ionospheric chemistry, the optimal CH<sub>4</sub> loss rate is  $\sim 3 \times 10^{27} \text{ s}^{-1}$  or 80 kg s<sup>-1</sup> in a globally averaged sense, consistent with the early result of Yelle et al. (2008). The considerable variability in  $CH_4$  structure among different flybys implies that  $CH_4$  escape on Titan is more likely a sporadic rather than a steady process, with the  $CH_4$ profiles from about half of the flybys showing evidence for strong escape and most of the other flybys consistent with diffusive equilibrium.  $CH_4$  inflow is also occasionally required to interpret the data. Our analysis further reveals that strong  $CH_4$  escape preferentially occurs on the nightside of Titan, in conflict with the expectations of any solar-driven model. In addition, there is an apparent tendency of elevated  $CH_4$  escape with enhanced electron precipitation from the ambient plasma, but this is likely to be a coincidence as the time response of the  $CH_4$  structure may not be fast enough to leave an observable effect during a Titan encounter.

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### 1. Introduction

[2] Among the major species in Titan's neutral upper atmosphere, CH<sub>4</sub> is the most elusive. The CH<sub>4</sub> density structure as measured by the Cassini Ion Neutral Mass Spectrometer (INMS) implies a large escape flux of  $\sim 3 \times 10^9$  cm<sup>-2</sup> s<sup>-1</sup> referred to the surface, or equivalently a loss rate of  $\sim 2.5 \times 10^{27}$  s<sup>-1</sup>, according to Yelle et al. [2008] (hereafter referred to as Y08). However, no convincing mechanism has been proposed so far that drives such a large CH<sub>4</sub> outflow. At the range of temperature in Titan's upper atmosphere (~110-190 K [Westlake et al., 2011]), the thermal Jeans escape rate of  $10^{13}$ – $10^{20}$  s<sup>-1</sup> is far from sufficient. Strobel [2008, 2009] has argued that CH<sub>4</sub> loss from Titan is of hydrodynamic nature, but this was not confirmed by the Direct Simulation Monte Carlo (DSMC) results of Tucker and Johnson [2009] and Schaufelberger et al. [2012]. Current estimates of the nonthermal escape rates fall short by 2 orders of magnitude [e.g., *De La Haye et al.*, 2007]. Finally, *Bell et al.* [2010a] have proposed an alternative mechanism of aerosol trapping to interpret the CH<sub>4</sub> distribution with a negligible CH<sub>4</sub> escape rate, but later, *Strobel* [2012] has argued that this mechanism is operative well below the altitude range probed by the INMS and does not reduces the CH<sub>4</sub> escape rate significantly.

[3] The motivations for this study are twofold. First, there is still controversy on the interpretation of the INMS CH<sub>4</sub> data. The recent analysis of Bell et al. [2011] has obtained an optimal homopause level of  $\sim 1000$  km on Titan and a typical CH<sub>4</sub> escape flux at least 2 orders of magnitude smaller than those of Y08 and *Strobel* [2008, 2009]. Since the early INMS works were published, the data from significantly more Titan flybys have now become available, and the data reduction algorithms have also been improved. These call for a reanalysis of the INMS CH<sub>4</sub> structure to solve the discrepancy between existing works. Second, the INMS investigations of the CH<sub>4</sub> structure so far primarily focus on the globally averaged situation. An analysis of the flyby-to-flyby variability is currently lacking and will be attempted here. This allows an assessment of the response of the CH<sub>4</sub> structure to varying solar and/or magnetospheric conditions.

[4] The organization of the paper is as follows. In section 2, we describe briefly the INMS sample included in this work, followed by a detailed description of the improvements in data reduction over previous works such as that by *Müller-Wodarg et al.* [2008] (hereafter referred to as MW08) and *Cui et al.* [2009] (hereafter referred to as C09). We present

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the main results of this paper in section 3, where several distinctive questions on the  $CH_4$  structure in Titan's upper atmosphere are raised and their answers provided based on the reanalysis of the INMS data. Especially, we conclude that with the current knowledge of the eddy mixing profile and neutral temperature, strong  $CH_4$  escape must occur on Titan. Finally, we give conclusions in section 4.

### 2. Data Reduction Algorithms

[5] The CH<sub>4</sub> densities in Titan's upper atmosphere have been extensively measured by the INMS during the Cassini encounters with Titan [*Waite et al.*, 2004]. Systematic analyses of the INMS CH<sub>4</sub> data have been presented in various works [e.g., *Yelle et al.*, 2006; Y08; MW08; C09; *Magee et al.*, 2009; *Bell et al.*, 2010a, 2011]. For this study, we combine the INMS neutral measurements from 32 Titan flybys, from T5 to T71. The data are obtained from the Planetary Plasma Interactions (PPI) node of the NASA Planetary Data System (PDS) public archives (http://ppi.pds. nasa.gov) and are reduced in a way similar to MW08 and C09. Nevertheless, several improvements in the INMS data reduction algorithms have been implemented in this study, which we detail in sections 2.1–2.3. A comparison with results from previous analyses is given in section 2.4.

## 2.1. Sensitivities and Wall Effects

[6] The conversion from the INMS raw count rates to number densities relies on the choice of the sensitivity values. For a given neutral species, the sensitivity values used for the data analysis are usually parameterized with a peak sensitivity and a cracking pattern (C09). Preliminary sensitivity values have been reported in C09, based on the calibrations made with either the flight unit (FU) or the refurbished engineering unit (REU) [see also *Magee et al.*, 2009]. Later, the REU sensitivities have been recalculated following updated REU calibration campaigns, but reporting peak values only (D. A. Gell et al., Characterization of the Cassini Ion Neutral Mass Spectrometer (INMS): Revision of sensitivity values and implications for previous publications of INMS neutral densities and mixing ratios, manuscript in preparation, 2012, hereafter referred to as G12).

[7] Throughout this study, we adopt FU peak sensitivities and cracking patterns for all species with FU calibrations. For other species, we use the updated G12 peak sensitivities but still use the C09 cracking patterns. The updated REU calibrations do not necessarily affect the analysis of major neutral species such as N2 and CH4, since their sensitivities are based on FU calibration (C09). The situation for <sup>40</sup>Ar is more complicated, though the FU calibration results are used for this species. As illustrated in Y08, a proper determination of the <sup>40</sup>Ar densities requires a decoupling between <sup>40</sup>Ar and other minor species, especially CH<sub>3</sub>C<sub>2</sub>H. However, we will show below that in practice the decoupling depends on the  $CH_3C_2H$  cracking pattern rather than its peak sensitivity (see sections 2.3 for details). This means the updated REU calibrations do not affect the <sup>40</sup>Ar density determination as well. The <sup>40</sup>Ar density profile is critical for this study since as an inert and nonescaping species, it is useful for separating eddy mixing and molecular diffusion.

[8] An additional multiplicative factor, which is not implied by the updated REU calibrations, has to be adopted to account for the difference in total density between INMS and other instruments. This factor is assumed to be common to all species, but its exact value is subject to uncertainty. A comparison between the INMS total densities and the Cassini Ultraviolet Imaging Spectrograph (UVIS) values for the T41 flyby suggests a multiplicative factor of 2.9 [Koskinen et al., 2011], whereas a slightly lower value of 2.6 is inferred by matching the INMS total densities to the values from the Huygens Atmosphere Structure Instrument (HASI) and the Cassini Attitude and Articulation Control Subsystem (AACS) [Strobel, 2010]. A calibration factor of 2.9, common to all species, is adopted throughout this study (thus, all INMS peak sensitivities are divided by 2.9), but in practice, any value in the range of 2.6–3.2 is acceptable.

[9] Some portions of the INMS densities should be used with caution due to wall contamination, which primarily influences outbound densities but leaves inbound densities almost unaffected. Such an instrumental effect refers to adsorption/desorption or surface chemistry occurring on the INMS chamber walls [*Vuitton et al.*, 2008; C09]. Accordingly, throughout this study we focus on the N<sub>2</sub> and CH<sub>4</sub> densities from inbound only. For <sup>40</sup>Ar as a nonreactive species, wall contamination is not relevant, and both the inbound and outbound data are used.

### 2.2. Extraction of the N<sub>2</sub> and CH<sub>4</sub> Density Profiles

[10] For a given mass channel, the INMS records count rates in a primary counter (C1) as well as a low gain secondary counter (C2) [*Waite et al.*, 2004]. The latter is used only when the counts in the former are saturated. Due to dissociative ionization of neutral molecules by the INMS electron guns [*Waite et al.*, 2004], the density of a given species could be derived simultaneously from several channels. Specific strategies have to be designed to ensure that the densities from different channels are consistent and that the counts used are not affected by saturation [e.g., MW08; C09; *Magee et al.*, 2009].

[11] The N<sub>2</sub> and CH<sub>4</sub> densities are calculated following the scheme of MW08. In that work, the N<sub>2</sub> densities at most altitudes were obtained from C1 counts of either channel 28 or channel 14, depending on where C1 counts of channel 28 become saturated. Near the closest approach (CA) where C1 counts are saturated for both channels, C2 counts of channel 28 were used instead. The CH<sub>4</sub> densities were obtained from C1 counts of channel 16, but near CA where they become saturated, C1 counts of channel 12 were used. Channel 12 was chosen because it is not contaminated by <sup>13</sup>CH<sub>4</sub>.

[12] There are a few potential problems with the above approach. First, the transition level for the limit of saturation was set to where the count reaches  $10^5$  per integration period (IP, 0.031 s) or  $3.2 \times 10^6$  s<sup>-1</sup> based on visual inspection of the INMS data from individual flybys, but a more careful inspection combining the data from all 32 flybys reveals that the C1 counter becomes saturated at a significantly lower level. However, this does not necessarily mean that the C1 count rates should be used in a more conservative manner. In contrast, we will show below that the transition level can in practice be extended to higher count rates by allowing for nonlinear conversion. Second, assuming a clear-cut transition between different channels usually leads to a rapid change in the characteristics of the INMS data at the specified transition levels, and consequently a discontinuity in the derived  $N_2$  or  $CH_4$  density profile. This naturally introduces an artificial jump in the neutral temperature profile, which is derived from the density gradient. It will be shown below that these artificial density jumps can be largely removed by introducing continuously varying weighting functions for different channels. The improvements that we apply to the data reduction algorithms in this study are detailed as follows.

[13] First, we extend the transition levels to higher count rates by applying a correction for counter saturation in the region where the saturation is slight. An example is shown in Figure 1a where we plot the C1 count rate of channel 14,  $C_1^{(14)}$ , as a function of the C1 count rate of channel 28,  $C_1^{(28)}$ , both with dead time correction for detector fatigue [*Magee et al.*, 2009]. The INMS data from all 32 flybys have been included. The contributions of CH<sub>4</sub> and <sup>14</sup>N<sup>15</sup>N to channel 14 have been subtracted, so both count rates in Figure 1a should measure the N<sub>2</sub> densities. For  $C_1^{(28)} < 2 \times 10^6 \text{ s}^{-1}$ , the two count rates are linearly correlated, suggesting that the C1 counters for both channels are not saturated and give reasonable measurements of the N<sub>2</sub> density. Above ~2 ×  $10^6 \text{ s}^{-1}$ ,  $C_1^{(28)}$  curves up, indicative of counter saturation in channel 28. Up to ~(4–5) ×  $10^6 \text{ s}^{-1}$ , the relation between the two count rates can be described empirically by  $C_1^{(14)} = a_0 C_1^{(28)} \exp \left\{ \tan \left[ (a_1 C_1^{(28)})^{a_2} \right] \right\}$ , with  $a_0, a_1$  and  $a_2$  being free parameters to be constrained by the data. The C1 count rates of channel 28 corrected for saturation,  $\hat{C}_1^{(28)}$ , should satisfy  $C_1^{(14)} = a_0 \hat{C}_1^{(28)}$  as long as  $C_1^{(14)}$  is not saturated. Thus, we get

$$\hat{C}_1 = C_1 \exp\left\{ \tan\left[ (a_1 C_1)^{a_2} \right] \right\},\tag{1}$$

where we have dropped the superscript (28) because similar expressions are used to correct for the saturation of the C1 count rates of channels 14 and 16, as illustrated in Figures 1b and 1c, respectively.

[14] The free parameters,  $a_0$ ,  $a_1$  and  $a_2$ , are listed in Table 1 for reference. Note that  $a_0$  is not used for correcting for saturation but instead used for ensuring that the densities derived from different channels and/or counters are consistent (see also section 2.4). These issues have been discussed in sections A3 and A1.2 of C09 in terms of the C1/C2 ratio and the calibration of the N<sub>2</sub>/CH<sub>4</sub> cracking patterns. In previous analyses, the values for each of the above parameters were different from flyby to flyby, whereas in the present study, they are taken to be constant (see section 2.4 for details). The cutoff levels listed in Table 1 refer to the highest count rates for which equation (1) is applicable. Count rates above these cutoff levels are not used in our analysis. In practice, all C1 count rates of channel 16 can be safely used so that no cutoff level is given for this channel. By utilizing the count rates that are slightly saturated, the above procedure increases the signal-to-noise ratio of the density data near the transition regions as compared to early INMS analysis works.

[15] Second, the clear-cut transition at  $4.2 \times 10^6 \text{ s}^{-1}$  from one channel to another (see Table 1) may cause density discontinuities in the derived N<sub>2</sub> profiles. To remove such features, the N<sub>2</sub> densities are calculated with

 $W_1^{(28)}(z)N_1^{(28)}(z) + W_1^{(14)}N_1^{(14)}(z) + W_2^{(28)}N_2^{(28)}$  where  $N_1^{(28)}(z)$ ,  $N_1^{(14)}(z)$  and  $N_2^{(28)}$  represent N<sub>2</sub> densities from C1 of channel 28, C1 of channel 14 and C2 of channel 28, respectively,  $W_1^{(28)}$ ,  $W_2^{(28)}$  and  $W_1^{(14)}$  are predefined weighting functions constructed from hyperbolic tangents

$$W_1^{(28)}(t) = 1 - \frac{1}{2} \tanh\left[\frac{t - t_i^{(28)}}{\Delta t}\right] + \frac{1}{2} \tanh\left[\frac{t - t_o^{(28)}}{\Delta t}\right],$$
 (2)

$$W_{2}^{(28)}(t) = \frac{1}{2} \tanh\left[\frac{t - t_{i}^{(14)}}{\Delta t}\right] - \frac{1}{2} \tanh\left[\frac{t - t_{o}^{(14)}}{\Delta t}\right], \quad (3)$$

$$W_1^{(14)}(t) = 1 - W_1^{(28)} - W_2^{(28)}.$$
 (4)

In equations (2)–(4), t is time from CA,  $t_i^{(28)}(t_i^{(14)})$  and  $t_o^{(28)}(t_o^{(14)})$  correspond to where  $C_1^{(28)}(C_1^{(14)})$  reaches 4.2 × 10<sup>6</sup> s<sup>-1</sup> during the inbound and outbound portions of a given flyby, and  $\Delta t$  is the timescale for the transition taken to be 10 s in this work. An example of these weighting functions is given in Figure 1d, assuming  $t_i^{(28)} = -225$  s,  $t_o^{(28)} = +225$  s,  $t_i^{(14)} = -100$  s and  $t_o^{(14)} = +100$  s. The choice of the timescale for the transition,  $\Delta t$ , is not unique. Several values have been tested, but give identical N<sub>2</sub> density profiles.

[16] Finally, we note that the sampling of the INMS data is nonuniform. The data points from an individual flyby are often grouped in batches covering a very small time interval but with sequential groups separated by a much larger gap. Therefore as a third improvement, we average together all data points obtained within 1.5 s of each other, since they are expected to sample essentially the same portion of Titan's atmosphere. With a typical spacecraft velocity of 6 km s<sup>-1</sup>, this time interval covers a length scale of ~9 km along the spacecraft trajectory. In practice, the procedure described above replaces each tightly packed group with a single data point with higher precision.

# 2.3. Extraction of the <sup>40</sup>Ar Density Profile

[17] As an inert and nonescaping species, the density profile of <sup>40</sup>Ar is unique for constraining the eddy mixing coefficients on Titan, which can then be used to infer the CH<sub>4</sub> escape flux [e.g., Y08; *Bell et al.*, 2011]. The <sup>40</sup>Ar atoms produce peak signals at mass channel 40, but the counts in this channel are also contributed significantly by CH<sub>3</sub>C<sub>2</sub>H. To illustrate the necessity of decoupling their cracking patterns, an example is provided in Figure 2 for the T18 flyby. We show with the solid circles the total count rate in channel 40 as a function of time from CA. The contributions from <sup>40</sup>Ar and CH<sub>3</sub>C<sub>2</sub>H are given separately by different symbols. The algorithm used for estimating these contributions is based on our nominal choice, which is explained in detail below. Figure 2 shows that without a proper decoupling, the outbound <sup>40</sup>Ar densities would be overestimated by a factor of ~2.

[18] There are several complexities. First, the  $CH_3C_2H$  densities are usually obtained from counts in channels 37–39, but these channels are also contributed by  $C_6H_6$  and



**Figure 1.** (a) The C1 count rate of channel 14  $(C_1^{(14)})$  as a function of the C1 count rate of channel 28  $(C_1^{(28)})$ , both contributed by N<sub>2</sub> only. (b) The C2 count rate of channel 28  $(C_2^{(28)})$  as a function of the C1 count rate of channel 14  $(C_1^{(14)})$ , both contributed by N<sub>2</sub> only. (c) The C1 count rate of channel 12  $(C_1^{(12)})$  as a function of the C1 count rate of channel 16  $(C_1^{(16)})$ , both contributed by CH<sub>4</sub> only. The INMS data from all 32 flybys have been included. In Figures 1a–1c, the dashed line gives the linear correlation obtained from regions where both count rates are not saturated, and the solid line represents the nonlinear empirical relation used to correct for saturation up to the cutoff level given in Table 1. (d) The weighting functions for count rates in C1 of channel 28  $(W_1^{(28)}, \text{ solid}), \text{ C2 of channel 28 } (W_2^{(28)}, \text{ dotted})$  and C1 of channel 14  $(W_1^{(14)}, \text{ dashed})$ , as a function of time from CA. These weighting functions are used for calculating the N<sub>2</sub> densities without instantaneous transition near the cutoff levels.

CH<sub>3</sub>CN (C09). Their densities can be determined from counts in channels 77–78 and 41, respectively. Second, another relevant species is  $C_3H_6$  that has not been included in our previous works. This can be seen from Figure 3 of C09, showing that the singular value decomposition (SVD) analysis has underpredicted the count rate in mass channel

42, the main peak of the  $C_3H_6$  cracking pattern. Finally, it is also important that the contributions from background signals are subtracted before the count rates are converted to densities [C09; *Magee et al.*, 2009]. The background counts are estimated in a way similar to C09.

Table 1. Empirical Relations Between the Count Rates From Two Different Channels/Counters but Associated With the Same Ambient Species  $(N_2 \text{ or } CH_4)^a$ 

Species	Empirical Relation	$a_0$	$a_1$	<i>a</i> <sub>2</sub>	Cutoff Level
N <sub>2</sub>	$C_1^{(14)} = a_0 C_1^{(28)} \exp\left\{ \tan\left[ \left( a_1 C_1^{(28)} \right)^{a_2} \right] \right\}$	0.0300	$1.27 \times 10^{-7} \mathrm{s}$	3.05	$4.2\times10^6~{\rm s}^{-1}$
$N_2$	$C_2^{(28)} = a_0 C_1^{(14)} \exp\left\{ \tan\left[ \left( a_1 C_1^{(14)} \right)^{a_2} \right] \right\}$	0.00536	$1.12 \times 10^{-7} \mathrm{s}$	2.23	$4.2 \times 10^{6} \ s^{-1}$
$\mathrm{CH}_4$	$C_1^{(12)} = a_0 C_1^{(16)} \exp\left\{ \tan\left[ \left( a_1 C_1^{(16)} \right)^{a_2} \right] \right\}$	0.00791	$1.54 \times 10^{-7} \text{ s}$	2.77	N/A

<sup>a</sup>Also shown are the free parameters in these relations. Specifically,  $a_1$  and  $a_2$  are used to correct for saturations, whereas  $a_0$  is used to ensure that the densities from different channels/counters are consistent. The cutoff level refers to the highest count rate for which the empirical expression is applicable. N/A, not available.



**Figure 2.** The count rate in mass channel 40 as a function of time from CA for the T18 flyby. Different symbols stand for the total count rates, the count rates contributed by  $^{40}$ Ar and CH<sub>3</sub>C<sub>2</sub>H, respectively. The relative contributions of different species are calculated with the nominal algorithm (see text for details). The apparent asymmetry in CH<sub>3</sub>C<sub>2</sub>H is an indication of the wall chemistry effect.

[19] Among the neutral species mentioned above,  $CH_3C_2H$  and  $C_6H_6$  have not been calibrated preflight. The updated REU calibration has inferred their peak sensitivities  $\sim$ 30% lower than the C09 values. For C<sub>3</sub>H<sub>6</sub>, neither FU nor REU calibration is available, leading to considerable uncertainty in evaluating its contributions to channels 37-39. Using the cracking pattern from the chemistry reference data of the National Institute of Standards and Technology (NIST, http://webbook.nist.gov/chemistry/) suggests that the C<sub>3</sub>H<sub>6</sub> contribution to channel 39 is relatively small as compared to the other two channels. Therefore for our nominal choice, we derive the CH<sub>3</sub>C<sub>2</sub>H densities based on counts in channel 39 only, to minimize the uncertainty in the C<sub>3</sub>H<sub>6</sub> cracking pattern. Especially, we notice that the CH<sub>3</sub>C<sub>2</sub>H densities from channels 37 and 38 are sometimes negative even near CA, implying that the NIST sensitivities of  $C_3H_6$  for these two channels are probably higher than those appropriate to the INMS.

[20] We compare in Table 2 the  $^{40}$ Ar number densities derived with several different algorithms. For each case, we combine the data from all 32 flybys in our sample, and the results for three different altitude ranges are presented. The first case corresponds to our nominal choice, i.e., with C<sub>3</sub>H<sub>6</sub>, C<sub>6</sub>H<sub>6</sub> and CH<sub>3</sub>CN included, with background subtracted, and with CH<sub>3</sub>C<sub>2</sub>H densities from channel 39 only. Alternative algorithms in Table 2 include the case without background subtraction, the case without  $C_3H_6$ , the case without  $C_3H_6$ , the case without  $CH_3CN$ , and the case with  $CH_3C_2H$  densities calculated as the average results of channels 37–39. The other aspects of these alternative algorithms remain the same as the nominal case.

[21] As compared to the nominal algorithm, the <sup>40</sup>Ar densities are overestimated by  $\sim 5\%$ -10% if the background counts are not subtracted, underestimated by  $\sim 6\%$  if C<sub>3</sub>H<sub>6</sub> is not included, and underestimated by nearly  $\sim 15\%$  if neither C<sub>3</sub>H<sub>6</sub> nor C<sub>6</sub>H<sub>6</sub> is included. We emphasize that we consider C<sub>3</sub>H<sub>6</sub> and C<sub>6</sub>H<sub>6</sub> in our nominal analysis not because their direct contributions to channel 40 counts are significant. Instead, they are included to calculate more accurately the CH<sub>3</sub>C<sub>2</sub>H densities, thus representing an indirect influence to the <sup>40</sup>Ar density extraction as illustrated in Figure 2. Table 2 also shows that ignoring CH<sub>3</sub>CN does not make any appreciable change to the derived <sup>40</sup>Ar densities. Finally, different channels used for determining the CH<sub>3</sub>C<sub>2</sub>H densities may lead to an uncertainty in <sup>40</sup>Ar at the level of ~5%-10%.

[22] As mentioned in section 2.1, <sup>40</sup>Ar is a chemically inert species and not contaminated by any wall chemistry effect. This implies that the globally averaged inbound and outbound density profiles of <sup>40</sup>Ar should be roughly identi-cal as long as the sample is sufficiently large [e.g., C09]. This fact could be used to evaluate a specific  ${}^{40}$ Ar extraction algorithm since any imperfect decoupling of  ${}^{40}$ Ar from other species, all of which are subject to wall contamination, may lead to an <sup>40</sup>Ar asymmetry between inbound and outbound. Several examples are given in Figure 3. For our nominal choice, the symmetry between inbound and outbound is maintained at all altitudes. This is also true for the case without background subtraction but more likely because the background signals are themselves symmetric about CA [see C09, Figures 33 and 34]. In contrast, there are clear differences between the inbound and outbound <sup>40</sup>Ar densities for the case without  $C_3H_6$  and  $C_6H_6$  included, as well as the case with CH<sub>3</sub>C<sub>2</sub>H densities from the averages of channels 37-39. The above comparison justifies, though indirectly, our nominal choice of the  $^{40}$ Ar extraction algorithm in this study.

### 2.4. Comparisons With Previous Results

[23] We present in this section a comparison between the  $N_2$ ,  $CH_4$  and  $^{40}Ar$  densities obtained here and those from previous works [e.g., MW08; C09] multiplied by the additional calibration factor of 2.9 (see section 2.1).

[24] In the  $N_2/CH_4$  data reduction algorithms described in section 2.2, we have adopted a correcting function that varies for different channels (see Table 1). In contrast, it has been assumed in our previous analysis (C09; Y08; MW08)

**Table 2.** The <sup>40</sup>Ar Number Densities Calculated From Different Algorithms (See Text for Details) and Averaged Over Several Selected Altitude Bins Including All Flybys in Our Sample

Algorithm	960–980 km (cm <sup>-3</sup> )	980–1000 km (cm <sup>-3</sup> )	1000–1100 km (cm <sup>-3</sup> )
Nominal	$3.5 \times 10^{5}$	$2.4 \times 10^{5}$	$1.0  imes 10^5$
No background subtraction	$3.8  imes 10^5$	$2.6  imes 10^5$	$1.1  imes 10^5$
No C <sub>3</sub> H <sub>6</sub>	$3.3  imes 10^5$	$2.3  imes 10^5$	$9.5  imes 10^4$
No $C_3H_6$ and $C_6H_6$	$3.0  imes 10^5$	$2.0  imes 10^5$	$8.8  imes 10^4$
No CH <sub>3</sub> CN	$3.5  imes 10^5$	$2.5  imes 10^5$	$1.1 \times 10^{5}$
CH <sub>3</sub> C <sub>2</sub> H from mean of channels 37–39	$3.8 \times 10^5$	$2.5 \times 10^{5}$	$9.7  imes 10^4$



**Figure 3.** A comparison between the globally averaged inbound (solid) and outbound (dashed) density profiles of <sup>40</sup>Ar, obtained from several algorithms including (a) the nominal case, (b) the case without background subtraction, (c) the case without both  $C_3H_6$  and  $C_6H_6$ , and (d) the case with  $CH_3C_2H$  densities from the averages of channels 37–39. For a reasonable scheme of <sup>40</sup>Ar density extraction, an asymmetry between the inbound and outbound profiles is not expected as <sup>40</sup>Ar is an inert species and is free from any wall chemistry effect.

that the saturation is due to the overload of the INMS detector system and thus the saturation characteristics are species independent. The early assumptions are incorrect as revealed by Figure 4, where we show the C2 count rates as a function of the C1 count rates for different channels. The data points from all 32 flybys have been included. The C1-C2 relations for channels 15 and 16, which are primarily contributed by CH<sub>4</sub>, are nearly identical and both are indicated by blue in Figure 4. Another group of relations, black for channel 14, red for channel 28 and green for channel 29, all of which are primarily contributed by N<sub>2</sub> or <sup>14</sup>N<sup>15</sup>N, is different from the relations for CH<sub>4</sub>. This strongly suggests that saturation is species dependent, though a rigorous interpretation based on physical arguments is currently lacking.

[25] When compared with MW08 and C09, the improvements in data reduction adopted here do not significantly alter the N<sub>2</sub> and CH<sub>4</sub> densities in regions where the C1 counts of channels 28 and 16 are not saturated, but the density differences in the saturated regions are not negligible. If we considered the T16 flyby (on 22 July 2006) as an example, we find that the N<sub>2</sub> densities reported here are  $\sim 3\%$ -5% higher than C09 near CA, and the CH<sub>4</sub> densities are higher by  $\sim$ 15%–20%. These differences could be explained with the following arguments: The  $a_0$ 's parameters in Table 1 are related to the C1/C2 ratio and the calibration factors of channels 14 and 12 (C09). The latter were introduced in C09 to ensure that the N2 and CH4 densities from different channels are consistent. It is easily verified that the C1/C2 ratio is identical to the inverse of the multiplication of  $a_0$ 's for channels 28 and 14, which is  $\sim$ 6219 based on Table 1. The same ratio has been derived in our previous works as  $\sim$ 5976 for T16. The lower C1/C2 ratio in previous works, due to an overestimated saturation level, accounts for the N2 density

difference reported above. Similarly, the CH<sub>4</sub> calibration factor for channel 12 is identical to the inverse of the multiplication of  $a_0$  for channel 16 in Table 1 and 0.00636, the ratio of the channel 12 to channel 16 sensitivities for CH<sub>4</sub>. This factor is ~0.683 for T16 from our previous analysis and ~0.804 here which is common to all flybys. The difference of ~18% for this calibration factor is responsible for the CH<sub>4</sub> density difference between this work and C09.



**Figure 4.** The C2 count rates as a function of the C1 count rates, for channels 14, 15, 16, 28 and 29. The data points from all flybys in our sample have been included. The C1-C2 relations indicate that the saturation characteristics are species dependent.

[26] The underestimates of the C09 and MW08 N<sub>2</sub> densities at relatively low altitudes are primarily associated with the early choice of the transition level  $(3.2 \times 10^6 \text{ s}^{-1})$ , which was based on an investigation of the  $C_1^{(28)} - C_1^{(14)}$  relation for any given flyby. In practice, when including the data from only one flyby, the relatively large scattering of the  $C_1^{(28)} - C_1^{(14)}$  relation makes it uncertain to characterize counter saturation, especially based on visual inspection. The improperness of the early choice of the transition level is clearly revealed by Figure 1a, which indicates that the  $C_1^{(28)} - C_1^{(14)}$  relation shows noticeable deviation from linearity for  $C_1^{(28)} < 3.2 \times 10^6 \text{ s}^{-1}$ . In this work, it is the combination of the data from all flybys that helps to constrain better the saturation characteristics. The underestimates of the C09 and MW08 CH<sub>4</sub> densities at low altitudes can be explained in a similar way. It is also worth emphasizing that the definition of the transition level here is different from that in previous works. In C09 and MW08, the transition level refers to where saturation occurs. In contrast, the definition of the transition level in this work is based on where the nonlinear relation, as described in section 2.2, starts to deviate from the data points. In both cases, the transition level corresponds to where the C1 counts can no longer be reliably used.

[27] As compared to the C09 results (multiplied by the calibration factor of 2.9), the  $^{40}$ Ar densities reported here are generally decreased by  $\sim 10\%$ . The difference partly comes from the additional inclusion of C<sub>3</sub>H<sub>6</sub> in this work. Also, the previous algorithms relied on a simultaneous fitting of counts in channels 37-39, whereas in this study we use channel 39 only, for the reason addressed in section 2.3. The recalibration of the REU sensitivities is not an issue since in both works the FU peak sensitivity is used for <sup>40</sup>Ar and the same cracking patterns are used for the other species involved, thus not changing their relative contributions to mass channel 40. To illustrate the update in <sup>40</sup>Ar density, we repeat our analysis on a sample identical to that of C09, i.e., up to T37, and we obtain at an altitude of 980 km an average  $^{40}$ Ar density of  $\sim 3.9 \times 10^5$  cm<sup>-3</sup> for the nominal case and  $\sim 4.2 \times 10^5$  cm<sup>-3</sup> for the case without C<sub>3</sub>H<sub>6</sub> and with CH<sub>3</sub>C<sub>2</sub>H densities from the average results of channels 37-39. The latter is identical to the value quoted by C09 when multiplied by 2.9.

[28] The INMS densities have also been calculated independently by *Magee et al.* [2009]. Their average values are  $\sim 8.9 \times 10^9$  cm<sup>-3</sup> for N<sub>2</sub>,  $\sim 2.0 \times 10^8$  cm<sup>-3</sup> for CH<sub>4</sub> and  $\sim 1.2 \times 10^5$  cm<sup>-3</sup> for <sup>40</sup>Ar between 1000 and 1100 km when multiplied by 2.9. Taking into account the difference in peak sensitivities, the *Magee et al.* [2009] N<sub>2</sub>, CH<sub>4</sub> and <sup>40</sup>Ar densities are about 15%, 10% and 20% lower than our nominal values obtained from an identical sample, i.e., from T18 to T43. The 1000–1100 km altitude range is typically where the C1 counts of channels 14 and 16 start to be saturated; thus, the difference in N<sub>2</sub> and CH<sub>4</sub> densities must be due to the respective methods used to correct for the saturation characteristics. The difference in <sup>40</sup>Ar densities cannot be traced back easily, as some of the details in their data reduction are not available to us. But we do note that for the algorithms listed in Table 2, the case without C<sub>3</sub>H<sub>6</sub> and C<sub>6</sub>H<sub>6</sub> reproduces the *Magee et al.* [2009] value most closely. It is

also noteworthy that despite of the 10–20% difference in absolute density, the  $^{40}$ Ar mixing ratios from the two works are consistent.

[29] To end this section, we summarize the key issues of the updated  $N_2/CH_4/^{40}Ar$  data reduction algorithms: (1) comparisons with the total densities from other Cassini/ Huygens instruments suggest that the absolute densities of all species have been underestimated by a factor of ~2.9 in previous analysis [e.g., C09; Y08; MW08; *Cui et al.*, 2008; *Magee et al.*, 2009]; (2) the N<sub>2</sub> and CH<sub>4</sub> densities near CA have been revised due to a more appropriate treatment of the saturation characteristics; (3) the instantaneous transitions in N<sub>2</sub> and CH<sub>4</sub> density profiles near regions where saturation occurs have been carefully removed in this study; and (4) the <sup>40</sup>Ar densities have been updated by including C<sub>3</sub>H<sub>6</sub> in the decoupling and by restricting CH<sub>3</sub>C<sub>2</sub>H density extraction to channel 39 only.

[30] Finally, it should be remembered that the Cassini measurements of Titan's lower atmosphere have revealed seasonal variations [e.g., *West et al.*, 2011]; thus, the change in the globally averaged density profile of any species observed by the INMS is partly due to Titan's long-term thermospheric evolution over the time when the data were acquired. For example, with our updated data reduction algorithms and an averaging between 1000 and 1100 km, the N<sub>2</sub>, CH<sub>4</sub> and <sup>40</sup>Ar densities drop by about 15%, 10% and 25% from the C09 sample (from 16 April 2005 to 19 November 2007) to the present sample including all available flybys (from 16 April 2005 to 7 July 2010).

# 3. Reanalysis of the CH<sub>4</sub> Structure in Titan's Upper Atmosphere

[31] Based on the improved reduction of the INMS data presented in section 2, several distinctive questions on the  $CH_4$  structure in Titan's upper atmosphere are discussed below. In particular, our aim is to solve the discrepancy in the interpretation of the  $CH_4$  data between existing works [e.g., Y08; *Bell et al.*, 2011].

[32] The mixing ratio profile of a minor species, *i*, in Titan's atmosphere is readily modeled with the one-dimensional, steady state diffusion equation:

$$F_i = -(D_i + K)n_a \frac{dX_i}{dr} - D_i n_a X_i \left(\frac{1}{H_i} - \frac{1}{H_a} + \frac{\alpha_i}{T} \frac{dT}{dr}\right), \quad (5)$$

to derive the eddy mixing coefficient and the diffusion flux (Y08). In equation (5),  $F_i$ ,  $X_i$ ,  $H_i$ ,  $D_i$ , and  $\alpha_i$  are the flux, mixing ratio, density scale height, and molecular diffusion coefficient of species *i*;  $n_a$  and  $H_a$  are the number density and density scale height of the background atmosphere; *T* is the neutral temperature; *K* is the eddy mixing coefficient; and *r* is the radial distance from Titan's center. In equation (5), we implicitly assume a common temperature profile for all atmospheric constituents.

[33] The results presented throughout this section are obtained within the framework of the fluid approach through equation (5), but we also note that the validity of such an approach has recently been questioned when compared to results from kinetic model calculations [e.g., *Tucker and Johnson*, 2009; *Tucker et al.*, 2012; *Volkov et al.*, 2011],



**Figure 5.** The diffusive equilibrium model fitting of the INMS and GCMS <sup>40</sup>Ar mixing ratios (solid circles) as a function of altitude throughout Titan's atmosphere. The INMS values are derived with the nominal choice of the <sup>40</sup>Ar data reduction algorithm (see section 2.3 for details). For illustrative purpose, the GCMS result is placed at 200 km, but the actual measurements were made at ~75–140 km [*Niemann et al.*, 2010]. The best fit model is given by the solid line, with an asymptotic eddy mixing coefficient,  $K_{\infty} \approx 2 \times 10^7$  cm<sup>2</sup> s<sup>-1</sup>. Models with other choices of  $K_{\infty}$  are also indicated, including the case with  $K_{\infty} \approx 2.2 \times 10^9$  cm<sup>2</sup> s<sup>-1</sup> that implies globally averaged CH<sub>4</sub> distribution under diffusive equilibrium.

especially in the transition region between strong collisional and collisionless.

### 3.1. How Important Is Eddy Mixing on Titan?

[34] It has been shown by *Yelle et al.* [2006, 2008] that the INMS CH<sub>4</sub> density profile can be interpreted by either the combination of diffusive equilibrium (i.e.,  $F_i = 0$ ) and an eddy mixing profile significantly larger than in any other solar system body or the combination of a large escape rate and an ordinary eddy mixing profile. To separate the above two effects, we first derive the eddy mixing coefficient as a function of altitude from the <sup>40</sup>Ar data.

[35] Eddy mixing in Titan's atmosphere is the summed effect of large-scale mixing by dynamics and small-scale mixing by turbulence [*Müller-Wodarg and Yelle*, 2002]. The former can only be obtained from time-dependent, full three-dimensional global circulation models [e.g., *Müller-Wodarg et al.*, 2000; *Bell et al.*, 2010b], and the latter is usually not resolved in these calculations. The analysis presented in this section is based on the steady state, one-dimensional calculations to be compared with the globally averaged <sup>40</sup>Ar data. This has the advantage of parameterizing the summed effect of all mixing processes, irrespective of the detailed mechanisms driving it.

[36] We adopt the empirical eddy mixing profile given by equation (4) of Y08, i.e.,  $K(z) = K_0(p_0/p)^{\gamma}K_{\infty}/[K_0(p_0/p)^{\gamma} + K_{\infty}]$ , where *p* is atmospheric pressure,  $p_0 = 1.43 \times 10^5$  dyn cm<sup>-2</sup> (note the value of 1.43 dyn cm<sup>-2</sup> given by Y08 is erroneous),

 $K_0 = 3 \times 10^2 \text{ cm}^2 \text{ s}^{-1}$ ,  $\gamma = 0.9$  and  $K_\infty$  is the asymptotic value of the eddy mixing coefficient. Such a functional form treats  $K_\infty$ as the only free parameter to be constrained by the data with a diffusive equilibrium model for <sup>40</sup>Ar. To constrain rigorously the eddy mixing profile, we combine the INMS <sup>40</sup>Ar data obtained above ~950 km and the tropospheric <sup>40</sup>Ar mixing ratio of ~3.39 × 10<sup>-5</sup> measured by the Huygens Gas Chromatograph Mass Spectrometer (GCMS) below ~140 km [*Niemann et al.*, 2010].

[37] The interpolation of the <sup>40</sup>Ar mixing ratio profile to low altitudes using equation (5) requires a background model atmosphere to be constructed all the way from the top of the atmosphere down to the lower stratosphere. Several post-Cassini background models are available from the literature, including the model based on the HASI measurements made during the Huygens descending phase [Fulchignoni et al., 2005], the model from Y08, and the standard chemical model of Strobel [2012]. These background models are denoted as HASI, RVY08, and DFS12, respectively. The HASI densities above 1000 km are systematically higher than the actual globally averaged values due to the oblateness of Titan's upper atmosphere (MW08), as the HASI data were acquired at the equatorial regions. The RVY08 model, which is based on previous INMS results, clearly underestimates the true atmospheric densities in the upper thermosphere by a factor of  $\sim 2.9$  due to the uncertainty in absolute calibration (see section 2.1). The DFS12 model is the favored one for this study, as it is consistent with both the updated INMS total density profile and the range of Titan's average thermospheric temperature [e.g., C09; Westlake et al., 2011].

[38] In Figure 5 we show the globally averaged INMS <sup>40</sup>Ar mixing ratio as a function of altitude. Such a profile is obtained by interpolating to a common altitude grid the observed <sup>40</sup>Ar mixing ratios based on the nominal data reduction algorithm described in section 2.3, which are then averaged over all flybys in our sample, both inbound and outbound. Also shown in Figure 5 is the best fit diffusive equilibrium model, with  $K_{\infty} \approx 2 \times 10^7$  cm<sup>2</sup> s<sup>-1</sup>, as well as models calculated with other choices of  $K_{\infty}$ . Especially, the dash-dotted line gives the model with  $K_{\infty} \approx 2.2 \times 10^9$  cm<sup>2</sup> s<sup>-1</sup>, required by the condition of CH<sub>4</sub> being in diffusive equilibrium (see below). This model shows considerable departure from the INMS data. For all cases, the background atmosphere is taken from the DFS12 standard chemical model, and the lower boundary condition is taken to

**Table 3.** Asymptotic Eddy Mixing Coefficient,  $K_{\infty}$ , and the CH<sub>4</sub> Homopause Level,  $z_{\text{hom}}$  (CH<sub>4</sub>), Calculated From Several Different Choices of the Background Model Atmosphere and the Input INMS <sup>40</sup>Ar Density Profile

Background Atmosphere	INMS <sup>40</sup> Ar Input	$K_{\infty} (\mathrm{cm}^2 \mathrm{s}^{-1})$	$z_{\rm hom} ({\rm CH_4})$ (km)
DFS12 Nominal		$2.0 \times 10^{7}$	855
	No C <sub>3</sub> H <sub>6</sub> /C <sub>6</sub> H <sub>6</sub>	$1.6 \times 10^{7}$	845
	No background subtraction	$2.2 \times 10^7$	860
RVY08	Nominal	$5.0 \times 10^7$	875
	No C <sub>3</sub> H <sub>6</sub> /C <sub>6</sub> H <sub>6</sub>	$4.1 \times 10^{7}$	865
	No background subtraction	$5.5 \times 10^7$	880
HASI	Nominal	$1.6 \times 10^7$	840
	No $C_3H_6/C_6H_6$	$1.3 \times 10^{7}$	825
	No background subtraction	$1.8 \times 10^7$	850



Figure 6. The CH<sub>4</sub> diffusion model profiles in Titan's upper atmosphere compared with the globally averaged INMS CH<sub>4</sub> densities from the updated data reduction algorithms. The density uncertainties due to counting statistics are too small to be visible at the scale shown. Five models are indicated, falling into two groups: (1) The gray and blue lines represent models calculated throughout the entire atmosphere and match the GCMS CH<sub>4</sub> mixing ratio of 1.48% deep in the lower stratosphere [Niemann et al., 2010]. The former gives the best fit model with a loss rate of  $3.8 \times 10^{27} \text{ s}^{-1}$  and the latter gives the diffusive equilibrium (DE) model. (2) The red, magenta and green lines represent models calculated in the 1200-1600 km altitude range, matching the INMS CH<sub>4</sub> mixing ratio of 4.6% at the lower boundary. The red line gives the best fit model with a loss rate of  $3 \times 10^{27}$  s<sup>-1</sup>, and the remaining two represent diffusive equilibrium models with different input background atmospheres (either DFS12 or isothermal at 140 K).

be consistent with the GCMS result [*Niemann et al.*, 2010]. Detailed in Table 3 are the  $K_{\infty}$  values for several test runs with different choices of the background model atmosphere and different inputs of the INMS <sup>40</sup>Ar mixing ratio. These test runs give  $K_{\infty}$  in the range of  $\sim (1-6) \times 10^7$  cm<sup>2</sup> s<sup>-1</sup>, comparable to the values in the upper atmospheres of other solar system bodies such as Mars [e.g., *Rodrigo et al.*, 1990] and Venus [e.g., *von Zahn et al.*, 1979]. For all cases the corresponding CH<sub>4</sub> homopause level is well below the 1000 km level suggested by *Bell et al.* [2011]. Our calculations indicate that above  $\sim 1200$  km, the eddy mixing coefficient is at least 2 orders of magnitude lower than the molecular diffusion coefficient for CH<sub>4</sub>. In section 3.2 we show that this has important impacts on the inference of CH<sub>4</sub> escape on Titan.

<sup>[39]</sup> Bell et al. [2011] used a simultaneous fitting to the <sup>14</sup>N<sup>15</sup>N and <sup>40</sup>Ar density data to constrain the eddy mixing profile, but we will not attempt this because the change in  $K_{\infty}$  has a larger impact on the <sup>40</sup>Ar mixing ratio than on the <sup>14</sup>N<sup>15</sup>N mixing ratio, which makes <sup>40</sup>Ar a more sensitive diagnostic of eddy mixing. This could be seen from Bell et al. [2011, Figure 6], who show that enhanced eddy mixing leads to a factor of 2 increase in <sup>40</sup>Ar mixing ratio but only a 5% decrease in <sup>14</sup>N/<sup>15</sup>N ratio at 1200 km.

[40] For further illustration, we use equation (5) to calculate the <sup>14</sup>N/<sup>15</sup>N ratio as a function of altitude in Titan's upper atmosphere, with different choices of the temperature profile and eddy mixing coefficient. A fixed lower boundary condition of 167.7 is adopted, based on the updated GCMS result of *Niemann et al.* [2010]. For the DFS12 temperature profile and over the  $K_{\infty}$  range of  $1 \times 10^7$  to  $1 \times 10^8$  cm<sup>2</sup> s<sup>-1</sup> (i.e., from 1/5 to 5 times the nominal value), we find a range in <sup>14</sup>N/<sup>15</sup>N of ~200–220 at 1200 km. For the RVY08 and HASI temperature profiles, the corresponding ranges are ~210–230 and ~190–210, respectively. Thus, it is clear that <sup>40</sup>Ar is a more powerful and preferred constraint on eddy mixing as a combined result of (1) the uncertainty in temperature and (2) the insensitivity of <sup>14</sup>N/<sup>15</sup>N ratio to  $K_{\infty}$ .

### 3.2. Does Strong CH<sub>4</sub> Escape Occur on Titan?

[41] As soon as the eddy mixing profile is known, the CH<sub>4</sub> distribution is readily modeled with equation (5), treating the CH<sub>4</sub> escape rate as the only free parameter. For a preliminary test of the model validity, we show with the light solid line in Figure 6 the model profile obtained by integrating equation (5) upward from the lower stratosphere where the CH<sub>4</sub> mixing ratio is set as 1.48% based on the GCMS result [*Niemann et al.*, 2010]. A CH<sub>4</sub> loss rate,  $L(CH_4)$ , of  $3.8 \times 10^{27} \text{ s}^{-1}$  is used for constructing the model. The neutral temperature profile is taken from the DFS12 background atmosphere, and  $K_{\infty} \approx 2 \times 10^7 \text{ cm}^2 \text{ s}^{-1}$  is adopted for self-consistency (see Table 3). The model adequately reproduces the INMS CH<sub>4</sub> data in the 1200–1600 km altitude range but systematically overestimates the data both below and above.

[42] The departure below  $\sim 1200$  km comes from the fact that the chemical destruction of CH<sub>4</sub> molecules has been ignored. In Titan's upper atmosphere, CH<sub>4</sub> photolysis typically peaks at ~850 km [Lavvas et al., 2011]. and the effects of magnetospheric destruction may vary considerably in response to the plasma environment [e.g., Rymer et al., 2009]. Strobel [2009] has recently shown that the CH<sub>4</sub> loss rate derived from the INMS data may differ by  $\sim 20\%$  with or without ionospheric chemistry included. It is also likely that the specific functional form of the eddy mixing profile adopted in this study has some impact on the model CH<sub>4</sub> mixing ratios below  $\sim 1200$  km. We note that in the analysis of Y08, the lower boundary for CH model fitting is placed at  $\sim$ 950 km, which is the lowest altitude probed by the INMS. The choice of the lower boundary at 1200 km is in fact a quite significant difference between the two works. The present choice lessens the sensitivity of the model results to both CH<sub>4</sub> photochemical destruction and eddy mixing, whose influences tend to diminish with increasing altitude.

[43] Above ~1600 km, the Knudsen number,  $K_n$ , defined as the ratio between the particle mean free path and the atmospheric scale height, becomes sufficiently high that a kinetic model should be used instead [e.g., *Volkov et al.*, 2011]. *Bird* [1994] argued that the fluid description is only valid with  $K_n < 0.2$ , which corresponds to a typical altitude of ~1400 km for CH<sub>4</sub> on Titan. However, Figure 6 indicates that the diffusion model can in practice be extended upward by at least 200 km and still with satisfactory results.

[44] Based on the above discussions, we use the INMS  $CH_4$  densities in the 1200–1600 km range for the data-model comparison to ensure that the effect of chemical destruction is negligible, that the exact form of the eddy mixing profile is not

**Table 4.** The Best Fit  $CH_4$  Loss Rates for Different Input Parameters of the Asymptotic Eddy Mixing Coefficient,  $K_{\infty}$ , and Isothermal Neutral Temperature,  $T^a$ 

Model	$K_{\infty} (\mathrm{cm}^2 \mathrm{s}^{-1})$	<i>T</i> (K)	$L(CH_4) (s^{-1})$
1	$2 \times 10^7$	DFS12	$3.0 \times 10^{27}$
2	$2.2 \times 10^{9}$	DFS12	DE
3	$2 \times 10^7$	140	$4.5 \times 10^{27}$
4	$2 \times 10^7$	150	$2.7 \times 10^{27}$
5	$2.6 \times 10^{9}$	145	DE
6	$2 \times 10^7$	165	DE

<sup>a</sup>Diffusive equilibrium (DE) is obtained for some extreme choices of the model input.

important, and that the fluid description is valid. The corresponding best fit CH<sub>4</sub> diffusion model is indicated by the red line in Figure 6, with a CH<sub>4</sub> loss rate of  $\sim 3.0 \times 10^{27} \text{ s}^{-1}$  or a CH<sub>4</sub> upward flux of  $\sim 3.6 \times 10^9 \text{ cm}^{-2} \text{ s}^{-1}$  referred to the surface, in agreement with the early results of Y08 and *Strobel* [2008, 2009]. Here the DFS12 background atmosphere and a nominal eddy mixing coefficient of  $K_{\infty} \approx 2 \times 10^7 \text{ cm}^2 \text{ s}^{-1}$  have been used. The CH<sub>4</sub> flux inferred above accounts for  $\sim 65\%$  of the CH<sub>4</sub> limiting flux well below Titan's homopause.

[45] Table 4 lists the results from model runs with different input profiles of the eddy mixing coefficient and neutral temperature. All models are calculated with a fixed CH<sub>4</sub> mixing ratio of 4.6% at the lower boundary (1200 km), based on the updated INMS data reduction algorithms. For models 1–2, the temperature profile is taken from the DFS12 background atmosphere, whereas for the other models isothermal condition is assumed. The diffusive equilibrium solutions for several model inputs are illustrated in Figure 6 for comparison. The change in the best fit CH<sub>4</sub> loss rate with continuously varying eddy mixing coefficient,  $K_{\infty}$ , and isothermal temperature, *T*, is illustrated in Figure 7. Some extreme models are able to reproduce the INMS CH<sub>4</sub> data without invoking a large CH<sub>4</sub> loss rate. If we restrict temperature in the 140–150 K range as implied by existing INMS analyses, the eddy mixing coefficient,  $K_{\infty}$ , has to be  $\sim(2-3) \times 10^9$  cm<sup>2</sup> s<sup>-1</sup> to suppress the CH<sub>4</sub> loss rate below the typical nonthermal level [e.g., *De La Haye et al.*, 2007]. If we use  $K_{\infty}$  values consistent with the INMS and GCMS <sup>40</sup>Ar data, the neutral temperature has to be  $\sim165$  K to maintain CH<sub>4</sub> diffusive equilibrium. Occasionally the neutral temperature in Titan's upper atmosphere reaches such a high level [*Westlake et al.*, 2011], but this only occurs for particular flybys and cannot be used as the globally averaged value.

[46] We conclude that strong  $CH_4$  escape does occur on Titan, with a globally averaged loss rate of  $\sim 3 \times 10^{27} \text{ s}^{-1}$ which is many orders of magnitude higher than the Jeans rate. We reach this conclusion by combining our knowledge of (1) the <sup>40</sup>Ar structure throughout the entire atmosphere based on the INMS and GCMS data and (2) the CH<sub>4</sub> structure in the 1200-1600 km range based on the INMS data only. The inclusion of the GCMS <sup>40</sup>Ar data (obtained well below the homopause) is essential for constraining the eddy mixing profile since the INMS <sup>40</sup>Ar mixing ratio (obtained well above the homopause) is not sensitive to  $K_{\infty}$  when  $K \ll D_i$ . In contrast, we do not require that the CH<sub>4</sub> model profiles reproduce the GCMS CH<sub>4</sub> mixing ratio of 1.48% [Niemann et al., 2010]. For example, the gray solid line in Figure 6, when extrapolated downward with equation (5), approaches asymptotically 1.25% in the lower stratosphere. We expect that the difference in the stratospheric CH<sub>4</sub> mixing ratio could be compensated for by including chemical destruction terms in the model calculations [Strobel, 2012].

### 3.3. How Variable Is CH<sub>4</sub> Escape on Titan?

[47] In this section, we investigate the variability of  $CH_4$  escape and search for potential trends with solar and/or magnetospheric conditions. We derive for each flyby the best fit  $CH_4$  loss rate with the one-dimensional, steady state



**Figure 7.** (left) The best fit CH<sub>4</sub> loss rate as a function of asymptotic eddy mixing coefficient,  $K_{\infty}$ , and isothermal neutral temperature, *T*. (top right) The variation of the CH<sub>4</sub> loss rate with  $K_{\infty}$  when *T* is fixed to 145 K (bottom right) the CH<sub>4</sub> loss rate with *T* when  $K_{\infty}$  is fixed to 2 × 10<sup>7</sup> cm<sup>2</sup> s<sup>-1</sup>. The inference of strong CH<sub>4</sub> escape on Titan is based on the optimal range of these two parameters, as constrained by our current knowledge of the N<sub>2</sub> and <sup>40</sup>Ar density structures.

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Flyby	Date (Earth Day)	LAT LON	SZA	LST	Т	(K)	$L(CH_4)$ (10 <sup>27</sup> s <sup>-1</sup> )	e 0.6 eV to 5 MeV	Ions 1 eV to 50 keV	<i>p</i> * 27–255 keV
T5	-1578	67°N	355°	$108^{\circ}$	17:40	$156\pm2$	$3.8\pm0.5$	Plasma sheet	Plasma sheet	Medium
T18	-1053	75°N	111°	102°	06:50	$121 \pm 2$	<1.9	Lobe-like	Lobe-like	High
T21	-973	$60^{\circ}N$	229°	132°	22:41	$157\pm2$	$2.0\pm0.5$	Mixed	Mixed	High
T23	-941	52°N	$20^{\circ}$	67°	12:34	$147\pm2$	<1.2	Plasma sheet	Plasma sheet	Medium
T25	-901	5°N	$25^{\circ}$	172°	23:58	$171\pm3$	$2.2\pm0.3$	Unidentified	Unidentified	Low
T26	-885	7°N	$11^{\circ}$	166°	00:52	$143\pm2$	$2.4\pm0.2$	Bimodal	Heavy-riched	Medium
T28	-854	25°N	13°	164°	00:41	$143\pm2$	<0.9	Mixed	Mixed	High
T29	-838	34°N	$14^{\circ}$	$157^{\circ}$	00:32	$157\pm3$	$2.0\pm0.4$	Plasma sheet	Plasma sheet	Medium
T30	-822	42°N	$17^{\circ}$	$150^{\circ}$	00:19	$155\pm2$	$2.5\pm0.3$	Mixed	Mixed	Medium
T32	-790	57°N	$24^{\circ}$	135°	23:47	$131 \pm 2$	< 0.9	Magnetosheath	Magnetosheath	High
T36	-679	49°S	63°	93°	19:10	$180\pm4$	$2.9\pm0.2$	Plasma sheet	Plasma sheet	High
T39	-600	$75^{\circ}S$	71°	83°	18:31	$120\pm3$	< 0.7	Plasma sheet	Plasma sheet	High
T40	-584	$20^{\circ}S$	$104^{\circ}$	63°	16:16	$138\pm2$	$1.2\pm0.3$	Bimodal	Heavily enriched	Medium
T42	-504	39°S	127°	46°	14:32	$158\pm2$	$1.5\pm0.4$	Magnetosheath	Magnetosheath	High
T43	-456	3°N	114°	$50^{\circ}$	15:15	$107\pm3$	<2.2	Lobe-like	Mixed	High/Medium
T50	-186	58°S	328°	$120^{\circ}$	00:17	$138\pm3$	$-2.5\pm0.8$	Mixed	Mixed	High
T56	-67	$7^{\circ}S$	164°	160°	22:47	$122\pm 6$	<1.6	Mixed	-	High
T57	-51	$17^{\circ}S$	163°	155°	22:48	$151\pm5$	$4.1\pm1.0$	Mixed	-	High/Medium
T58	-35	$27^{\circ}S$	$162^{\circ}$	$148^{\circ}$	22:48	$149\pm4$	$5.7\pm0.7$	Plasma sheet	-	Medium
T59	-19	36°S	161°	$140^{\circ}$	22:52	$141 \pm 1$	$-1.2\pm0.3$	Mixed	-	Medium
T65	153	58°S	$20^{\circ}$	112°	03:17	$146\pm2$	<1.9	-	-	-
T71	329	$44^{\circ}S$	341°	$105^{\circ}$	04:58	$140\pm1$	$2.5\pm0.3$	-	-	-

**Table 5.** The Best Fit CH<sub>4</sub> Loss Rate Calculated From the Diffusion Model Fitting to the Updated INMS CH<sub>4</sub> Data for Each Flyby in Our Sample<sup>a</sup>

<sup>a</sup>Also listed are the date of observation in units of Earth days before (indicated by negative) or after (indicated by positive) equinox (on 11 August 2009), latitude (LAT), longitude (LON), solar zenith angle (SZA), local solar time (LST), as well as the characteristics of the ambient plasma following the classification schemes of *Rymer et al.* [2009], *Németh et al.* [2011] and *Garnier et al.* [2010]. Heavy-riched means events enriched with heavy ions. The geophysical parameters are given for a reference altitude of 1400 km;  $p^*$  indicates energetic protons. The uncertainties of *T* and *L*(CH<sub>4</sub>) as well as the upper limits for *L*(CH<sub>4</sub>) are evaluated with a Monte Carlo approach which takes into account the effects of both counting statistics and density fluctuations due to wave structures.

diffusion model based on a common eddy mixing profile with  $K_{\infty} \approx 2 \times 10^7 \text{ cm}^2 \text{ s}^{-1}$ . Using different  $K_{\infty}$  values gives very similar results as eddy mixing is unimportant at the altitudes involved in the model fitting. This is justified by Figure 7 (top right), which shows that over the range of possible  $K_{\infty}$  values (several  $10^7 \text{ cm}^2 \text{ s}^{-1}$ ), the impact of eddy mixing is small. The neutral temperature is obtained from the hydrostatic fitting to the N<sub>2</sub> densities for each flyby, assuming isothermal.

[48] More specifically, we evaluate the best fit temperature and CH<sub>4</sub> loss rate, as well as their uncertainties, with a Monte Carlo approach [e.g., Pang, 2006]. For a given flyby, we obtain the large-scale trends for N<sub>2</sub> and CH<sub>4</sub> in Titan's upper atmosphere based on the third-order polynomial fittings to the logarithmic N<sub>2</sub>/CH<sub>4</sub> densities as a function of altitude. We then generate 1000 random realizations of the N<sub>2</sub> and CH<sub>4</sub> profiles of this flyby that encompass the apparent wiggles in the INMS data around the large-scale trends. This is accomplished by artificially placing random fluctuations around the polynomial fits with altitude dependent magnitudes equal to the measured density variations along the spacecraft trajectory. For each random realization, we apply isothermal fitting to N<sub>2</sub> and diffusion model fitting to CH<sub>4</sub>. The averages (standard deviations) of the random temperature and loss rate values are then taken to be their respective best fit values (uncertainties). The wiggles in the data are contributed not only by counting statistics but also by gravity wave perturbations which are persistently seen in Titan's upper atmosphere [e.g., Fulchignoni et al., 2005; Müller-Wodarg et al., 2006; Koskinen et al., 2011]. Variations due to counting statistics are  $\sim (1-2)\%$  at a reference altitude of 1400 km (C09) and the wave amplitudes are typically 10% of the mean densities [*Müller-Wodarg et al.*, 2006]. In practice, the uncertainty due to density wiggles is more important than that due to counting statistics and that due to finite temperature gradient. The latter justifies the isothermal assumption adopted throughout this section.

[49] The best fit CH<sub>4</sub> loss rates and neutral temperatures are detailed in Table 5. Nearly 1/3 flybys have been excluded either due to the insufficient coverage of the INMS data in the 1200–1600 km altitude range, or due to large variations of the INMS densities around the empirical trend that lead to significant uncertainties in the derived temperatures and loss rates. The former is primarily caused by INMS ram angles too large to allow accurate density determination, and the latter, as seen in the T37, T48 and T61 flybys, might be indicative of large amplitude wave structures in the ambient atmosphere. Since Table 5 only gives a portion of the available INMS sample, the average of the listed CH<sub>4</sub> loss rates is not exactly identical to the value of  $3.0 \times 10^{27} \text{ s}^{-1}$  reported in section 3.2. Also note that the neutral temperatures listed in the table are not exactly equal to those of *Westlake et al.* [2011] due to different altitude ranges used for isothermal fitting.

[50] Several examples of the INMS CH<sub>4</sub> mixing ratio profiles are presented in Figure 8 between 1200 and 1600 km. The diffusive equilibrium models are indicated by the dashed lines for comparison. Figure 8 reveals a large variability in the pattern of CH<sub>4</sub> bulk flow. The T5, T29 and T71 plots correspond to cases with strong CH<sub>4</sub> outflow at the level of several  $10^{27}$  s<sup>-1</sup>. The T23 and T39 plots show cases with CH<sub>4</sub> distributions under approximate diffusive equilibrium. The inference of diffusive equilibrium for a specific flyby is made based on the criterion that the actual best fit flux is less than 3



**Figure 8.** The INMS  $CH_4$  mixing ratio profiles for several example flybys and categories with different solar and/or magnetospheric conditions. For comparison, the dashed line gives the diffusive equilibrium (DE) model. A considerable variability in $CH_4$  structure is revealed and suggests that  $CH_4$  escape on Titan is more likely to be sporadic rather than steady. Specifically, cases with strong escape include T5, T29, T71, T50, the nightside (night) category and the plasma sheet (PS) category, whereas the data from T23, T39, the dayside (day) category and the lobe-like (lobe) category are reasonably described by diffusive equilibrium.

times the flux uncertainty. The T50 plot is an example with the best fit  $CH_4$  flux being inward. Cases with  $CH_4$  outflow are seen in 12 out of 22 flybys in our sample ( $\sim$ 55%). The diffusive equilibrium cases are seen in eight flybys ( $\sim 36\%$ ). and for each of them we provide in Table 5 the corresponding  $3\sigma$  upper limit of the CH<sub>4</sub> outflow rate. Finally, cases with CH<sub>4</sub> inflow are seen in only two flybys. The variability of CH<sub>4</sub> bulk flow revealed by Table 5 is considerably larger than that for H<sub>2</sub>, which remains roughly constant among different flybys [Cui et al., 2011]. The INMS data used for this study have been acquired primarily under solar minimum conditions, with  $\sim 10\%$  variance in solar activities based on either the F10.7 cm or 121.6 nm solar irradiance, as reported by the space weather prediction center of the National Oceanic and Atmospheric Administration (NOAA). Not surprisingly, it would be difficult to explain the variability of CH<sub>4</sub> bulk flow as solar-driven only.

[51] Table 5 also shows that the CH<sub>4</sub> flow in Titan's upper atmosphere is preferentially outward. If the flows from individual flybys were eventually associated with horizontal transport rather than escape [*Tucker and Johnson*, 2009], a considerable portion of the flybys with inward flow would be expected in our sample. But the INMS data do not support this. In the following we will interpret the CH<sub>4</sub> flux derived for any individual flyby as an escape flux, except for the two flybys with best fit CH<sub>4</sub> flux being negative. This means we assume the true sinks of  $CH_4$  molecules reside far away in the interplanetary space rather than some horizontally connected regions on Titan [see also *Yelle et al.*, 2006]. A rigorous evaluation of such an issue will be presented in a future paper (I. C. F. Müller-Wodarg et al., The role of thermospheric winds on the distribution of  $CH_4$  and <sup>40</sup>Ar in Titan's upper atmosphere, manuscript in preparation, 2012). It is also worth mentioning that the observed variability in  $CH_4$  structure could be either spatial or temporal. If the latter is dominant, the variability reported here is not necessarily indicative of horizontal transport.

[52] One of the prominent features revealed by Table 5 is that strong CH<sub>4</sub> escape preferentially occurs on the nightside. We note that for the five flybys with dayside trajectories (defined here as SZA < 90° at a reference altitude of 1400 km), three (T23, T39 and T50) show CH<sub>4</sub> distributions under approximate diffusive equilibrium, and two of the remaining flybys (T40 and T42) are characterized by relatively small CH<sub>4</sub> loss rates of ~1.2 × 10<sup>27</sup> s<sup>-1</sup> and ~1.5 × 10<sup>27</sup> s<sup>-1</sup>. In contrast, all the three flybys with the largest CH<sub>4</sub> escape rates (>3 × 10<sup>27</sup> s<sup>-1</sup>) occur deep in the nightside. The above difference is clearly seen in Figure 8 (third column), where we compare the diffusive equilibrium distribution for CH<sub>4</sub> with the INMS profile averaged over all measurements made on the dayside or nightside. This is obviously in conflict with the expectations of any

**Table 6.** Mean CH<sub>4</sub> Loss Rates and Neutral Temperatures for Different Categories of Titan Flybys<sup>a</sup>

Category	Neutral Temperature (K)	$CH_4$ Loss Rate (s <sup>-1</sup> )	Flybys Included
Dayside	148	DE	T23, T40, T41, T42, T43, T48
Nightside	150	$2.1 \times 10^{27}$	T21, T25, T26, T28, T29, T30, T32, T50, T55, T56, T57, T58, T59
Equatorial	145	$2.1 \times 10^{27}$	T25, T26, T28, T37, T40, T43, T48, T55, T56, T57, T58, T61
Polar	153	$3.1 \times 10^{27}$	T5, T16, T18, T19, T39, T49, T64
Sub-Saturn	152	$2.3 \times 10^{27}$	T5, T23, T25, T26, T28, T29, T30, T32, T50, T64, T65, T71
Anti-Saturn	140	$3.3 \times 10^{27}$	T16, T48, T49, T51, T55, T56, T57, T58, T59, T61
Ramside	157	$2.0 \times 10^{27}$	T21
Wakeside	150	$2.0 \times 10^{27}$	T18, T19, T36, T37, T39, T40, T41, T42, T43
Preequinox	153	$2.3 \times 10^{27}$	all flybys up to T59
Postequinox	139	$2.2 \times 10^{27}$	T61, T64, T65, T71
Plasma sheet	159	$3.3 \times 10^{27}$	T5, T19, T23, T29, T36, T39, T49, T51, T55, T58
Lobe-like	115	DE	T18, T41, T43, T61
Bimodal	141	$1.9 \times 10^{27}$	T26, T40
High proton flux	151	$2.0 \times 10^{27}$	T18, T19, T21, T28, T32, T36, T39, T42, T50, T51, T56
Medium proton flux	151	$1.9 \times 10^{27}$	T5, T23, T26, T29, T30, T37, T40, T49, T58, T59
Low proton flux	171	$2.2 \times 10^{27}$	T25

<sup>a</sup>Also shown are the flybys included in each category. The diffusive equilibrium (DE) model provides reasonable description of the  $CH_4$  data on the dayside and for lobe-like plasma conditions.

solar-driven model. Other features consistent with this include the nondetection of appreciable difference in  $CH_4$  loss rate between the equatorial region and the polar region, or between preequinox and postequinox. Both meridional and seasonal trends might be present if  $CH_4$  loss from Titan is primarily solar-driven, analogous to the findings of the variation of N<sub>2</sub>/CH<sub>4</sub> densities and neutral temperature with latitude (MW08), as well as the decrease in altitude of the detached haze layer from before to after the equinox [*West et al.*, 2011].

[53] The above discussions motivate us to investigate the magnetospheric response of  $CH_4$  escape on Titan. Ideally, varying plasma conditions are encountered for different zonal sectors. The actual situation is however more complicated, and a better categorization can be made in terms of the varying levels of electron precipitation in the 0.6 eV to 5 MeV range [*Rymer et al.*, 2009], ion precipitation in the 1 eV to 50 keV range [*Németh et al.*, 2011], or energetic proton precipitation in the 27–255 keV range [*Garnier et al.*, 2010]. Following these works, we list in Table 5 the characteristics of Titan's plasma environment for reference.

[54] Table 5 reveals that there is no systematic trend in CH<sub>4</sub> loss rate with longitude, and there is no evidence for elevated CH<sub>4</sub> escape with enhanced energetic proton precipitation or with the presence of enriched water group ions peaking at  $\sim 4400$  eV [Németh et al., 2011]. The latter is indicated by the e classification of bimodal in Table 5. However, we do identify a tentative trend with magnetospheric electron precipitation. This is illustrated in Figure 8 (fourth column), where we compare the INMS  $CH_4$  mixing ratio profiles averaged over the plasma sheet and lobe-like categories with the respective diffusive equilibrium profiles. It is clear that strong CH<sub>4</sub> escape does occur for plasma sheet conditions, characterized by a relatively high peak electron flux of  $\sim 3.5 \times 10^5$  to  $1.2 \times 10^6$  cm<sup>-2</sup> s<sup>-1</sup> sr<sup>-1</sup> in the 120– 600 eV energy range [Rymer et al., 2009]. We note that among the six flybys in our sample that belong to this category, four show strong CH<sub>4</sub> escape on Titan. Especially, this category includes two of the three flybys with the largest CH<sub>4</sub> loss rates in Table 5. In contrast, for each of the two lobe-like flybys in our sample, the INMS CH<sub>4</sub> distribution is

reasonably described by diffusive equilibrium. According to *Rymer et al.* [2009], lobe-like conditions are characterized by an incident electron flux a factor of 10 lower than the plasma sheet value in a similar energy range. The magnetosheath category (not shown in Figure 8) also includes two flybys: one under diffusive equilibrium and the other one with a relatively low CH<sub>4</sub> loss rate of  $\sim 1.5 \times 10^{27} \text{ s}^{-1}$ . The incident electron flux for this category is comparable with the plasma sheet category but shifts to lower energies peaking at  $\sim 50 \text{ eV}$ . Thus, if electron precipitation drives CH<sub>4</sub> escape on Titan, then the relevant electron energy range is more likely at the level of several hundred eV or above.

[55] In Table 6 we summarize the mean  $CH_4$  loss rates for all categories that we consider above, along with the corresponding mean neutral temperatures. These are obtained from the isothermal and diffusion model fittings to the N<sub>2</sub> and CH<sub>4</sub> density profiles averaged over each category, rather than simply taking the averages over values in Table 5. The interpretation of the results in Table 6 deserves some caution. For most of the categories, the variations in CH<sub>4</sub> loss and neutral temperature are so large that comparisons between different categories do not lead to conclusive results. Thus, some of the tendencies revealed by Table 6, such as the preferential occurrence of strong CH<sub>4</sub> escape at the anti-Saturn side, are not statistically significant. The most rigorous conclusions that we can draw for the variability in CH<sub>4</sub> escape are probably the diurnal difference and the trend with varying electron precipitation, as the dayside and lobe-like categories are the only two cases in Table 6 with CH<sub>4</sub> distribution under diffusive equilibrium. The implications of these features have already been discussed above.

[56] The recent INMS investigation of *Westlake et al.* [2011] has revealed a trend of enhanced neutral temperature in Titan's upper atmosphere when exposed to elevated electron precipitation. Thus,  $CH_4$  escape and neutral heating tend to occur under similar conditions. This may imply a potential correlation between the  $CH_4$  loss rate and the neutral temperature, but the scattering of such a relation is quite large, as indicated in Figure 9. Indeed, Table 6 shows that a similar temperature is derived for both the dayside and



**Figure 9.** The CH<sub>4</sub> loss rate,  $L(CH_4)$ , as a function of the neutral temperature, *T*, for all flybys with strong CH<sub>4</sub> escape confirmed at >3 $\sigma$  significance level (see text for details). No rigorous correlation can be identified between the two quantities.

nightside categories, but the  $CH_4$  escape rates for the two categories are significantly different.

[57] At the face value, the variability in CH<sub>4</sub> escape revealed by Table 6 implies that CH<sub>4</sub> escape on Titan is more likely to be magnetospherically driven rather than solar driven. However, one important consideration complicates the above argument: In response to varying solar and/or magnetospheric conditions, the change in CH<sub>4</sub> distribution occurs within the diffusion timescale,  $\tau_{\text{diff}} \sim H_i^2/D_i \approx 2$  h, where we have used a CH<sub>4</sub> scale height,  $H_i$ , of ~200 km and a CH<sub>4</sub> molecular diffusion coefficient,  $D_i$ , of  $\sim 5 \times 10^{10}$  cm<sup>2</sup> s<sup>-1</sup> referred to 1400 km. For comparison, the timescale over which solar inputs vary,  $\tau_{solar}$ , is about half a Titan day, i.e.,  $\tau_{solar} \approx 200$  h. This is significantly longer than  $\tau_{\text{diff}}$ , ensuring that the solar response of CH<sub>4</sub> escape on Titan, if present, can in principle be observed in the INMS data. However, this is not necessarily the case for magnetospheric variations. Simon et al. [2010] have shown that on the nightside of Titan, the timescale for magnetic field variability could be as long as 5 h, whereas on the dayside, the timescale is typically  $10^2$  s. Thus, the timescale for magnetospheric variations is either comparable with or much shorter than  $\tau_{\text{diff}}$ . For such cases, the time response of the CH<sub>4</sub> structure is not fast enough to leave an observable effect during a Titan encounter, and accordingly the apparent trend of CH<sub>4</sub> escape with magnetospheric electron precipitation may simply be a coincidence.

### 4. Concluding Remarks

[58] The inbound INMS data from 32 Cassini flybys with Titan are analyzed in this work, focusing on the  $CH_4$  structure in the upper atmosphere of the satellite. Several updates in the data reduction algorithms have been implemented, including the improved treatment of the counter saturation characteristics, the removal of instantaneous transition in the N<sub>2</sub> and  $CH_4$  density profiles, as well as the appropriate

decoupling between <sup>40</sup>Ar and other minor species. The analysis presented here is aimed at (1) solving the inconsistency in the interpretation of the CH<sub>4</sub> data between existing works [e.g., Y08; *Bell et al.*, 2011] and (2) investigating the variability of CH<sub>4</sub> escape among different flybys. Several questions raised in this paper are listed below along with our findings.

[59] 1. How important is eddy mixing on Titan? We use a diffusive equilibrium model to describe the <sup>40</sup>Ar mixing ratio profile, combining both the INMS data in the upper atmosphere and the GCMS data in the lower stratosphere [*Niemann et al.*, 2010]. The globally averaged asymptotic eddy mixing coefficient is  $K_{\infty} \approx 2 \times 10^7$  cm<sup>2</sup> s<sup>-1</sup>, based on the standard chemical model of *Strobel* [2012] as the input background atmosphere. The corresponding homopause level is at ~850 km, consistent with the early result of Y08 but in conflict with the 1000 km level suggested by *Bell et al.* [2011]. Over the altitude range probed by the INMS, molecular diffusion is significantly more important than eddy mixing. This has important impacts on the interpretation of the INMS CH<sub>4</sub> data.

[60] 2. Does strong  $CH_4$  escape occur on Titan? With the current knowledge of eddy mixing (derived from the <sup>40</sup>Ar data) and neutral temperature (derived from the  $N_2$  data), we conclude that strong CH<sub>4</sub> escape must occur on Titan. The nominal CH<sub>4</sub> loss rate is  $\sim 3 \times 10^{27} \text{ s}^{-1}$  or 80 kg s<sup>-1</sup> in a globally averaged sense, in general agreement with the early results of Y08 and Strobel [2008, 2009]. The CH<sub>4</sub> loss rate is not a linear response of the ambient atmospheric parameters, as revealed by Figure 7. In practice, the CH<sub>4</sub> loss rate can only be reliably inferred when it is near or above the level of  $10^{27}$  s<sup>-1</sup>. This is fortunately the case for Titan's upper atmosphere, making it possible to constrain the globally averaged CH<sub>4</sub> loss rate with a diffusion model. The strong CH<sub>4</sub> escape implied by the INMS data makes only a small contribution to the CH<sub>4</sub> budget on Titan, with the bulk of the CH<sub>4</sub> molecules supplied from Titan's interior photochemically converted to more complex hydrocarbons [Strobel, 2009]. The main uncertainty in the derived globally averaged CH<sub>4</sub> loss rate is associated with the choice of the temperature profile. The possible range of CH<sub>4</sub> loss rate is  $\sim$ (2.7–4.5)  $\times$  10<sup>27</sup> s<sup>-1</sup> in accord with the range of average temperature reported in existing works [e.g., Y08; C09; Westlake et al., 2011].

[61] 3. How variable is CH<sub>4</sub> escape on Titan? *Cui et al.* [2011] have shown that the H<sub>2</sub> escape remains roughly stable from flyby to flyby, but the analysis in this work reveals a large variability of CH<sub>4</sub> escape on Titan. Specifically, about half of the flybys show evidences for strong CH<sub>4</sub> escape at the level of several  $10^{27}$  s<sup>-1</sup>, whereas for most of the other flybys, the CH<sub>4</sub> structures are reasonably described by diffusive equilibrium. This suggests that CH<sub>4</sub> escape on Titan is more likely a sporadic rather than a steady process. CH<sub>4</sub> inflow may also occur on Titan, though only occasionally. We search for systematic trends in CH<sub>4</sub> escape with varying solar and/or magnetospheric conditions. We find that strong CH<sub>4</sub> escape preferentially occurs on the nightside, in conflict with the expectations of any solar-driven model. However, no rigorous connection can be identified between the CH<sub>4</sub> loss rate and the precipitation of various magnetospheric species, except for an apparent trend of elevated CH<sub>4</sub> escape for plasma sheet conditions as compared to

lobe-like conditions. But this may simply be a coincidence as the time response of the  $CH_4$  structure to magnetospheric inputs is not fast enough to leave an observable effect during a Titan encounter. The main uncertainties in the  $CH_4$  loss rates derived for individual flybys are associated with the density fluctuations around the large-scale trends, presumably due to wave structures in the ambient atmosphere.

[62] In a more general context, how magnetospheric particle precipitation influences the structure of Titan's neutral atmosphere has recently drawn significant attention. This is a highly complicated and variable process, which may leave a variety of observational signatures. Elevated neutral temperature has been found to preferentially, but not always, occur under plasma sheet conditions [Westlake et al., 2011]. Thus, neutral heating and CH<sub>4</sub> escape may represent intermediate processes of a complex interaction between Titan's upper atmosphere and magnetosphere, if the enhanced CH<sub>4</sub> escape associated with plasma sheet (see section 3.3) is realistic. The relative importance of particle precipitation depends on the depth in the atmosphere, with different magnetospheric species depositing most of their energies at different altitude levels, either above or below where solar EUV/FUV radiation dominates[e.g., Michael and Johnson, 2005; Cravens et al., 2008, Smith et al., 2009]. The access of incident charged particles, especially electrons, into Titan's atmosphere is also strongly controlled by the ambient magnetic field configuration, which could be either a barrier or a gate [e.g., Galand et al., 2006; Ma et al., 2009; *Richard et al.*, 2011]. Due to the above complexities, it is by no means possible to obtain any conclusive result based on a simple comparison between broad categories, as done in this work. Simulations of Titan's plasma-atmosphere interactions on a flyby-to-flyby basis and with realistic model inputs are required to eventually pin down the role of magnetospheric inputs on Titan's neutral atmosphere.

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