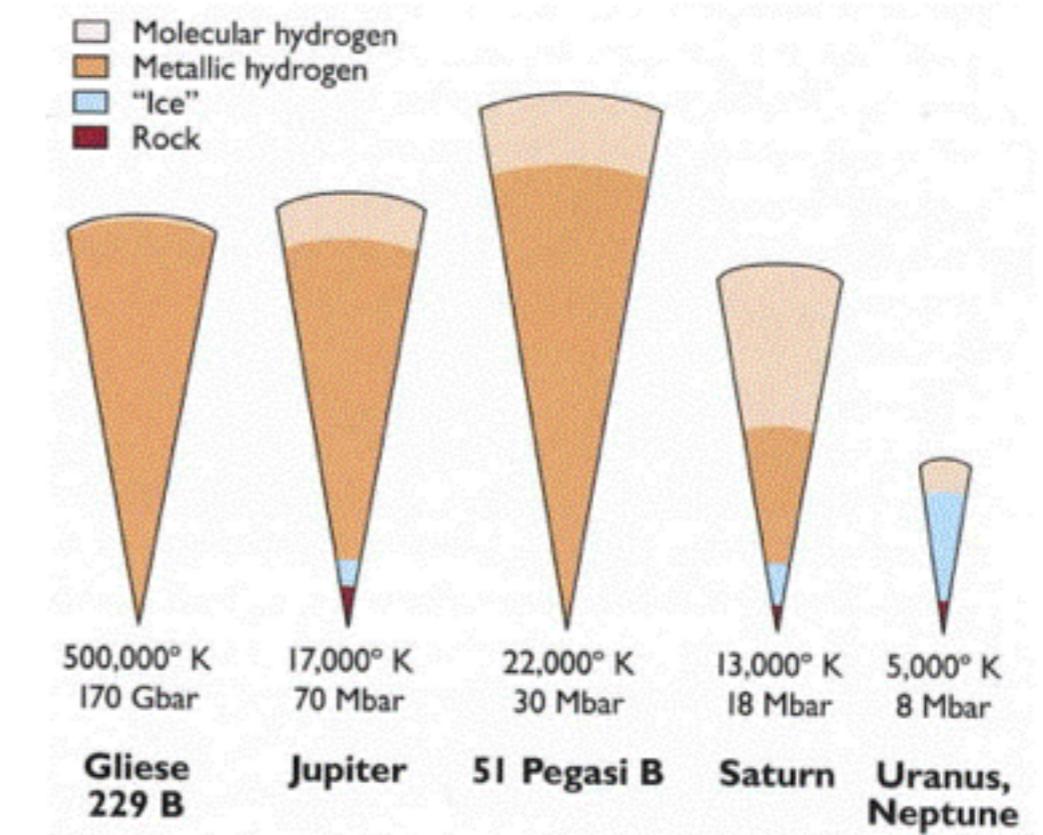
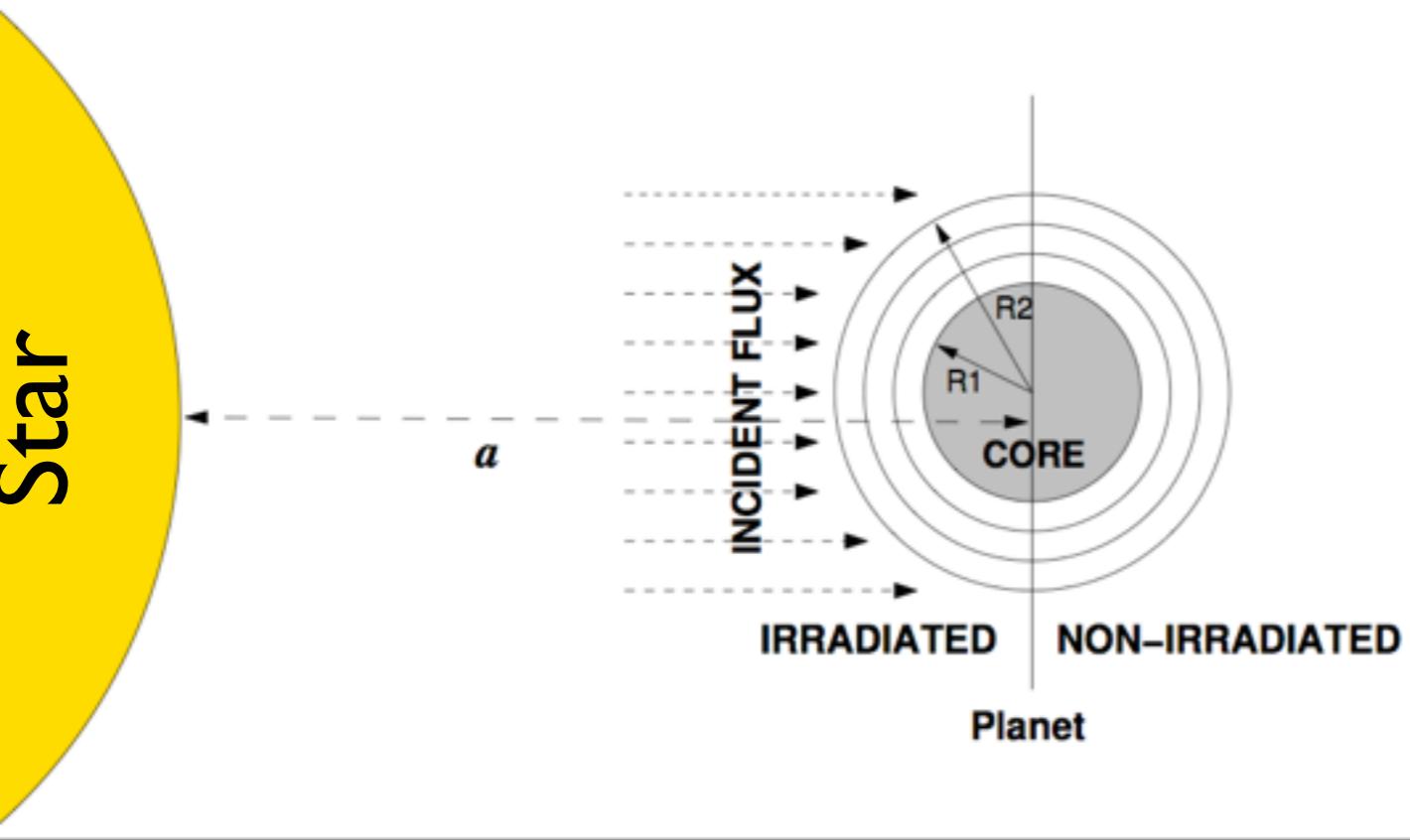


# Exoplanet Atmospheres

- Motivation (brown dwarfs, observations ,etc.)
- equilibrium and non-equilibrium chemistry
- radiative transfer, opacities, and spectra
- simplified model atmosphere problems
- retrieval techniques

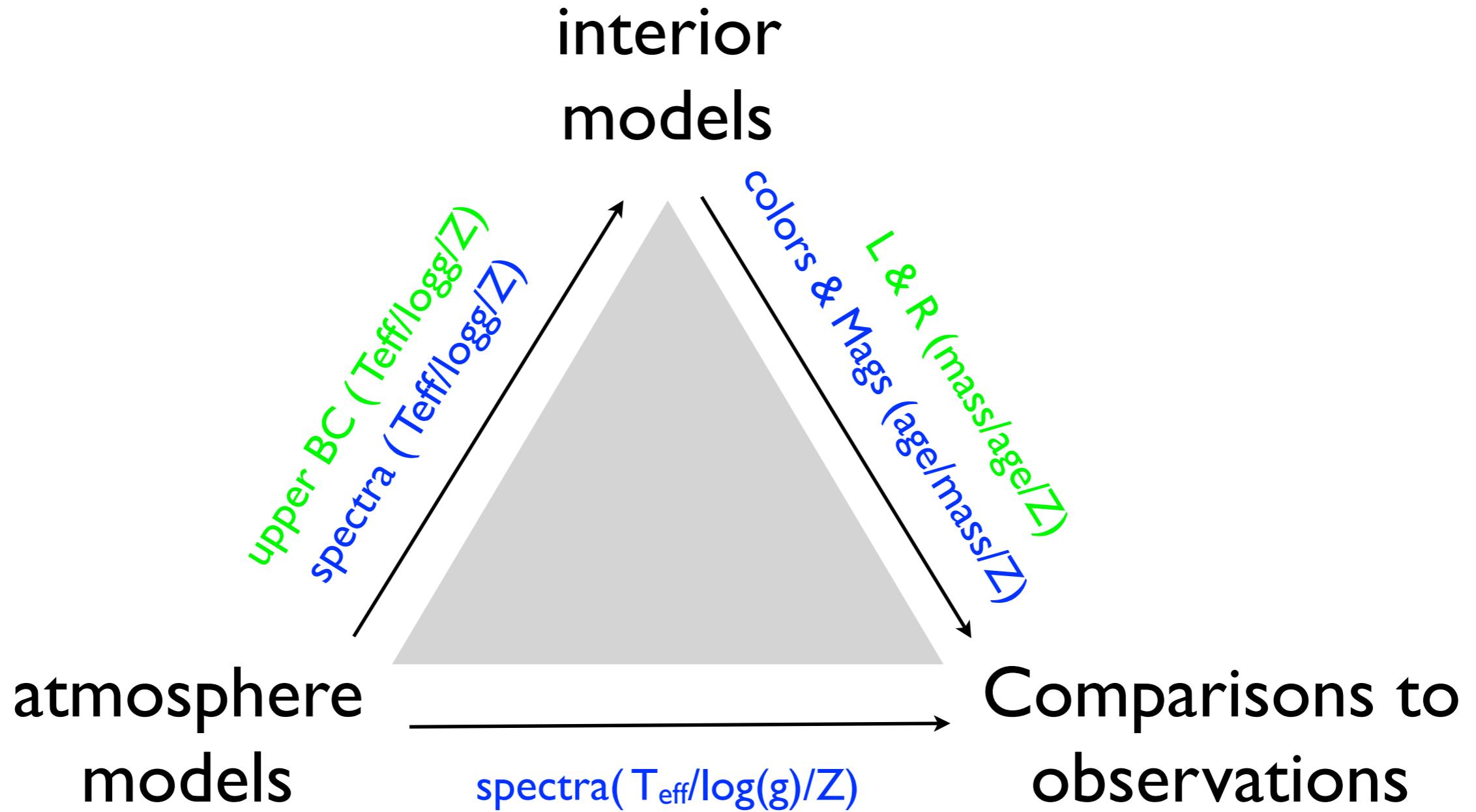
**Atmosphere:** Hydrogen & Helium, or other stuff.

**Interior:** solid (rock, ice) or convective fluid (Hydrogen, Helium)

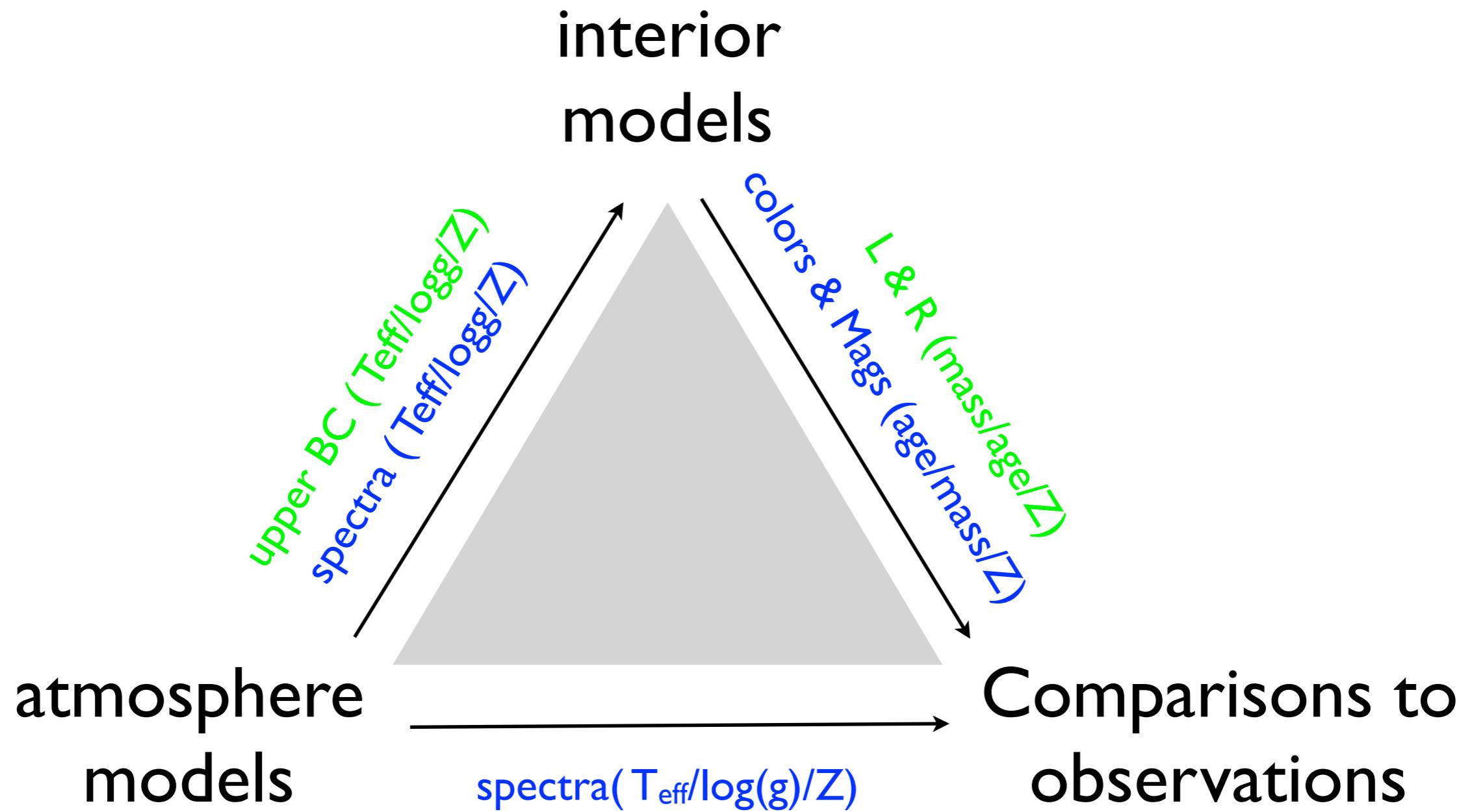


**Bottom Layer:** abrupt solid/liquid surface or deep continuous transition region.

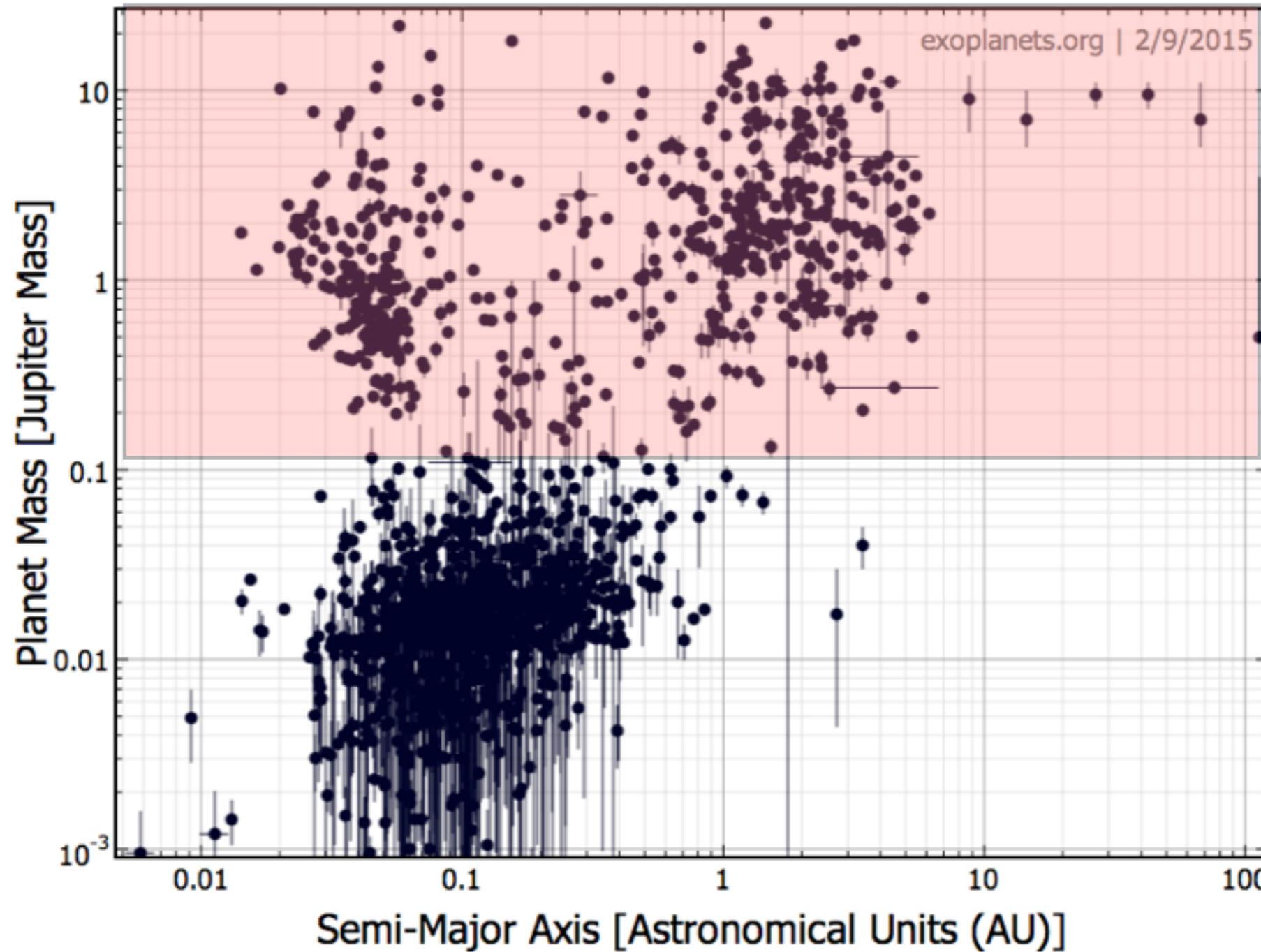
**Atmosphere [noun]:**  
“a transition region between the stellar interior  
and the interstellar medium” (Grey 1992)



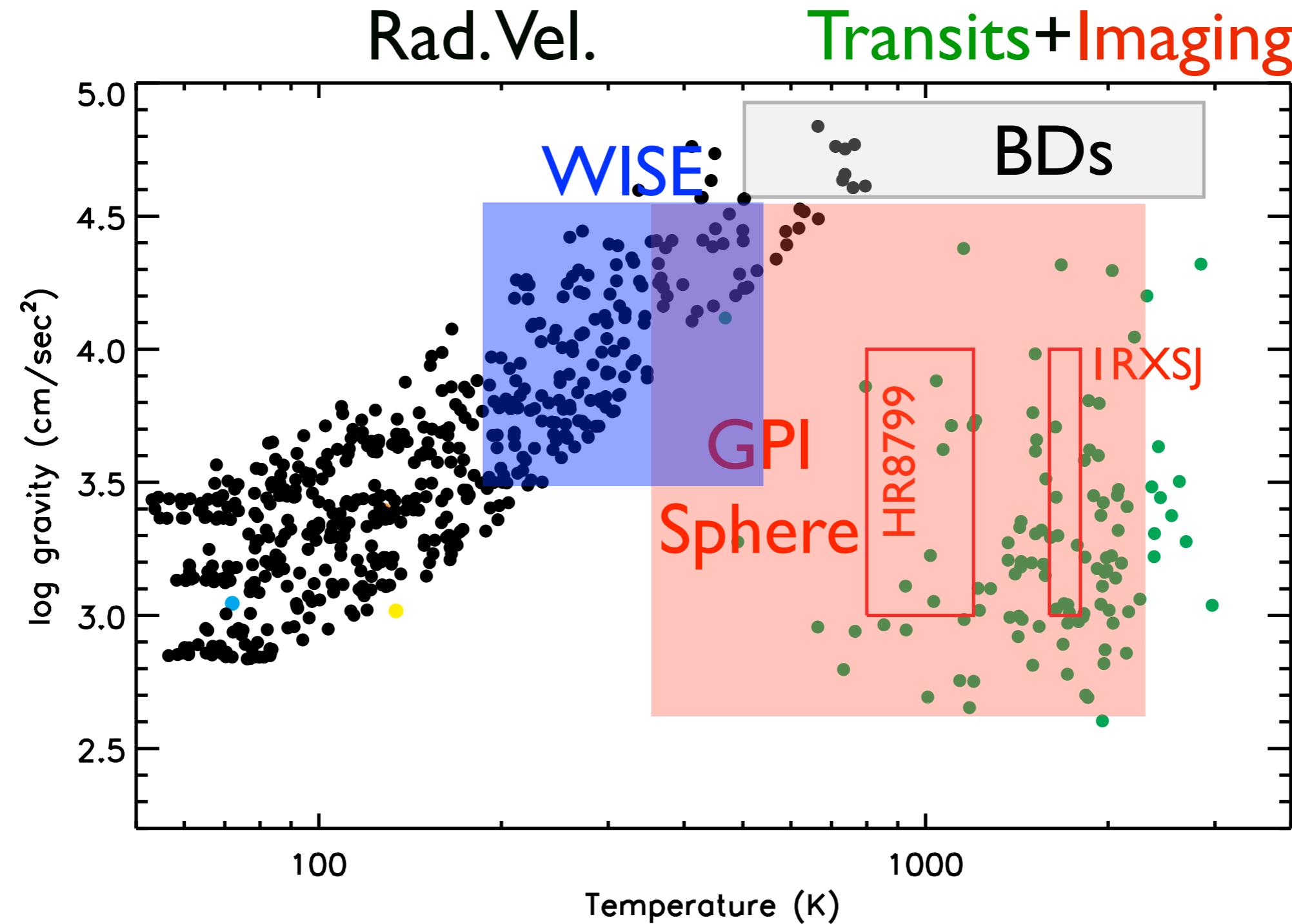
**Atmosphere [noun]:**  
a transition region between the planet interior  
and the interplanetary medium



# We will focus first on giants



The atmospheres we can study are generally warm to hot



$$\sigma T_{\text{eff}}^4 = \int F_\nu d\nu$$

# Lessons Learned from Brown Dwarfs ( $\sim 500\text{K} < T_{\text{eff}} < 2500\text{K}$ )

- $M/M_{\text{Jup}} > 80$  (Star)
- $13 < M/M_{\text{Jup}} < 80$  (Brown Dwarf)
- $M/M_{\text{Jup}} < 13$  (planet)

# Lessons Learned from Brown Dwarfs ( $\sim 500\text{K} < T_{\text{eff}} < 2500\text{K}$ )

- observable atmosphere:  
 $T_{\text{gas}} \sim 1000\text{K}$ ,  $P_{\text{gas}} \sim 0.1$  to 1 bar.
- relatively thin atmospheres ( $H_p \sim 12$  km)
- Major sources of opacity: Water, CIA,  
“dust”, Alkali (Na, K) doublets

# Giant Planet / Brown Dwarf overlap:

- mass:  $\sim 1$  to  $< 80 \times M_{\text{jupiter}}$
- radius:  $\sim 1$  to  $< 5 R_{\text{jupiter}}$
- ages:  $\sim$  millions to billions of years old
- gravity:  $\sim$  2 orders of magnitude
- effective temperature:  $\sim 100\text{K}$  to  $2500\text{K}$
- clouds: broad range of grains, ices (complex mixtures)
- non-equilibrium chemistry
- dynamics and “weather”
- BUT: different formation ... (composition & early evolution)

# “Solar Abundances” (Asplund et al. 2009)

- solar abundances defines our baseline elemental composition
- solar C,N,O are often debated values (check the reference!)
- starting point for equilibrium chemistry calculations
- the relative values are “initial conditions” of atmosphere models (and usually conserved quantities).

Z	Element	Photosphere	Meteorites	Z	Element	Photosphere	Meteorites
1	H	12.00	8.22 ± 0.04	44	Ru	1.75 ± 0.08	1.76 ± 0.03
2	He	[10.93 ± 0.01]	1.29	45	Rh	0.91 ± 0.10	1.06 ± 0.04
3	Li	1.05 ± 0.10	3.26 ± 0.05	46	Pd	1.57 ± 0.10	1.65 ± 0.02
4	Be	1.38 ± 0.09	1.30 ± 0.03	47	Ag	0.94 ± 0.10	1.20 ± 0.02
5	B	2.70 ± 0.20	2.79 ± 0.04	48	Cd		1.71 ± 0.03
6	C	8.43 ± 0.05	7.39 ± 0.04	49	In	0.80 ± 0.20	0.76 ± 0.03
7	N	7.83 ± 0.05	6.26 ± 0.06	50	Sn	2.04 ± 0.10	2.07 ± 0.06
8	O	8.69 ± 0.05	8.40 ± 0.04	51	Sb		1.01 ± 0.06
9	F	4.56 ± 0.30	4.42 ± 0.06	52	Te		2.18 ± 0.03
10	Ne	[7.93 ± 0.10]	-1.12	53	I		1.55 ± 0.08
11	Na	6.24 ± 0.04	6.27 ± 0.02	54	Xe	[2.24 ± 0.06]	-1.95
12	Mg	7.60 ± 0.04	7.53 ± 0.01	55	Cs		1.08 ± 0.02
13	Al	6.45 ± 0.03	6.43 ± 0.01	56	Ba	2.18 ± 0.09	2.18 ± 0.03
14	Si	7.51 ± 0.03	7.51 ± 0.01	57	La	1.10 ± 0.04	1.17 ± 0.02
15	P	5.41 ± 0.03	5.43 ± 0.04	58	Ce	1.58 ± 0.04	1.58 ± 0.02
16	S	7.12 ± 0.03	7.15 ± 0.02	59	Pr	0.72 ± 0.04	0.76 ± 0.03
17	Cl	5.50 ± 0.30	5.23 ± 0.06	60	Nd	1.42 ± 0.04	1.45 ± 0.02
18	Ar	[6.40 ± 0.13]	-0.50	62	Sm	0.96 ± 0.04	0.94 ± 0.02
19	K	5.03 ± 0.09	5.08 ± 0.02	63	Eu	0.52 ± 0.04	0.51 ± 0.02
20	Ca	6.34 ± 0.04	6.29 ± 0.02	64	Gd	1.07 ± 0.04	1.05 ± 0.02
21	Sc	3.15 ± 0.04	3.05 ± 0.02	65	Tb	0.30 ± 0.10	0.32 ± 0.03
22	Ti	4.95 ± 0.05	4.91 ± 0.03	66	Dy	1.10 ± 0.04	1.13 ± 0.02
23	V	3.93 ± 0.08	3.96 ± 0.02	67	Ho	0.48 ± 0.11	0.47 ± 0.03
24	Cr	5.64 ± 0.04	5.64 ± 0.01	68	Er	0.92 ± 0.05	0.92 ± 0.02
25	Mn	5.43 ± 0.04	5.48 ± 0.01	69	Tm	0.10 ± 0.04	0.12 ± 0.03
26	Fe	7.50 ± 0.04	7.45 ± 0.01	70	Yb	0.84 ± 0.11	0.92 ± 0.02
27	Co	4.99 ± 0.07	4.87 ± 0.01	71	Lu	0.10 ± 0.09	0.09 ± 0.02
28	Ni	6.22 ± 0.04	6.20 ± 0.01	72	Hf	0.85 ± 0.04	0.71 ± 0.02
29	Cu	4.19 ± 0.04	4.25 ± 0.04	73	Ta		-0.12 ± 0.04
30	Zn	4.56 ± 0.05	4.63 ± 0.04	74	W	0.85 ± 0.12	0.65 ± 0.04
31	Ga	3.04 ± 0.09	3.08 ± 0.02	75	Re		0.26 ± 0.04
32	Ge	3.65 ± 0.10	3.58 ± 0.04	76	Os	1.40 ± 0.08	1.35 ± 0.03
33	As		2.30 ± 0.04	77	Ir	1.38 ± 0.07	1.32 ± 0.02
34	Se		3.34 ± 0.03	78	Pt		1.62 ± 0.03
35	Br		2.54 ± 0.06	79	Au	0.92 ± 0.10	0.80 ± 0.04
36	Kr	[3.25 ± 0.06]	-2.27	80	Hg		1.17 ± 0.08
37	Rb	2.52 ± 0.10	2.36 ± 0.03	81	Tl	0.90 ± 0.20	0.77 ± 0.03
38	Sr	2.87 ± 0.07	2.88 ± 0.03	82	Pb	1.75 ± 0.10	2.04 ± 0.03
39	Y	2.21 ± 0.05	2.17 ± 0.04	83	Bi		0.65 ± 0.04
40	Zr	2.58 ± 0.04	2.53 ± 0.04	90	Th	0.02 ± 0.10	0.06 ± 0.03
41	Nb	1.46 ± 0.04	1.41 ± 0.04	92	U		-0.54 ± 0.03
42	Mo	1.88 ± 0.08	1.94 ± 0.04				

Al <sub>2</sub>	Al <sub>2</sub> O	Al <sub>2</sub> O <sub>2</sub>	Al <sub>2</sub> O <sub>3</sub>	AlBO <sub>2</sub>	AlC	AlCl	AlCl <sub>2</sub>	AlClF	AlF
AlF <sub>2</sub>	AlH	AlHO <sub>2</sub>	AlN	AlO	AlO <sub>2</sub>	AlOCl	AlOF	AlOF <sub>2</sub>	AlOH
AlS	B <sub>2</sub>	BC	BCl	BF	BH	BH <sub>2</sub>	BH <sub>3</sub>	BN	BO
BO <sub>2</sub>	BO <sub>2</sub> H <sub>2</sub>	BS	BaCl	BaCl <sub>2</sub>	BaClF	BaF	BaO	BaO <sub>2</sub> H <sub>2</sub>	BaOH
BaS	Be <sub>2</sub> O	Be <sub>3</sub> O <sub>3</sub>	BeBO <sub>2</sub>	BeC <sub>2</sub>	BeCl	BeCl <sub>2</sub>	BeF	BeF <sub>2</sub>	BeH
BeH <sub>2</sub>	BeN	BeO	BeO <sub>2</sub> H <sub>2</sub>	BeOH	BeS	C <sub>2</sub>	C <sub>2</sub> H	C <sub>2</sub> H <sub>2</sub>	C <sub>2</sub> H <sub>4</sub>
C <sub>2</sub> H <sub>6</sub>	C <sub>2</sub> H	<b>CH<sub>4</sub></b>	C <sub>2</sub> N	C <sub>2</sub> N <sub>2</sub>	C <sub>2</sub> O	C <sub>3</sub>	C <sub>3</sub> H	CH	<b>CO</b>
CH <sub>3</sub>	CH <sub>3</sub>		CHCl	CHF	CHP	CN	CNCl	CNO	
CO <sub>2</sub>	COF <sub>2</sub>		CP	CS	CS <sub>2</sub>	Ca(OH) <sub>2</sub>	Ca <sub>2</sub>	CaCl	
CaF	CaF <sub>2</sub>	CaH	CaO	CaOH	CaS	Cl <sub>2</sub>	ClO <sub>2</sub>	ClOH	CoCl
CrH	CrN	CrO	C	<b>H<sub>2</sub></b>			CsF	CsOH	Cu <sub>2</sub>
CuCl	CuF	CuH	C				FeCl <sub>2</sub>	FeF	FeF <sub>2</sub>
FeH	FeO	FeO <sub>2</sub> H <sub>2</sub>	Fe				H <sub>3</sub> BO <sub>3</sub>	HBO	HBO <sub>2</sub>
HBS	HCN	HCO	H				K <sub>2</sub> O <sub>2</sub> H <sub>2</sub>	K <sub>2</sub> SO <sub>4</sub>	KBO <sub>2</sub>
KCN	KCl	KF	KH	KOH	Li <sub>2</sub> O <sub>2</sub> H <sub>2</sub>	LiBO <sub>2</sub>	LiCl	LiF	LiH
LiNaO	LiOCl	LiO		MgCl	MgCl <sub>2</sub>	MgClF	MgF	MgF <sub>2</sub>	MgH
MgN	MgO	MgO		MgS	MnH	MnO	MnS	N <sub>2</sub>	N <sub>2</sub> O
NF	NH	NH <sub>3</sub>		NHO <sub>3</sub>	NO	NO <sub>2</sub>	NO <sub>2</sub> H	NO <sub>3</sub>	NOH
NS	Na <sub>2</sub>	Na <sub>2</sub>	<b>NH<sub>3</sub></b>	Na <sub>2</sub> O <sub>2</sub> H <sub>2</sub>	NaBO <sub>2</sub>	NaCN	NaCl	NaF	NaH
NaO	NaOH	NbO	NiCl	NiCl <sub>2</sub>	NiH	NiO	NiS	O <sub>2</sub>	O <sub>2</sub> H <sub>2</sub>
O <sub>3</sub>	OBF	OCS	OCl	OF	OH	OHF	P <sub>2</sub>	P <sub>4</sub>	PCl
PCl <sub>3</sub>	PF	PF <sub>2</sub>	PH	PH <sub>2</sub>	PH <sub>3</sub>	PN	PO	PO <sub>2</sub>	PS
PSF	RbCl	S <sub>2</sub>	S <sub>2</sub> O	S <sub>2</sub> Cl	SF	SF <sub>6</sub>	SH	SO	SO <sub>2</sub>
SO <sub>3</sub>	ScO	ScS	Si <sub>2</sub>	Si <sub>2</sub> C	Si <sub>2</sub> N	Si <sub>3</sub>	SiC	SiC <sub>2</sub>	SiCl
SiF	SiH	SiH <sub>2</sub>	SiH <sub>2</sub> F <sub>2</sub>	SiH <sub>3</sub>	SiH <sub>3</sub> Cl	SiH <sub>3</sub> F	SiH <sub>4</sub>	SiN	SiO
SiO <sub>2</sub>	SiS	SrCl	SrCl <sub>2</sub>	SrF	SrF <sub>2</sub>	SrH	SrO	SrO <sub>2</sub> H <sub>2</sub>	SrOH
TiO	Cl	TiCl <sub>2</sub>	TiCl <sub>3</sub>	TiCl <sub>4</sub>	TiF	TiF <sub>2</sub>		TiH	TiN
ZrO <sub>2</sub>	TiOCl	TiOCl <sub>2</sub>	TiOF	TiS	VN		VO <sub>2</sub>	ZrCl	
Zr <sub>3</sub>	ZrCl <sub>4</sub>	ZrF	ZrF <sub>2</sub>	ZrF <sub>4</sub>	ZrH		ZrO	ZrO <sub>2</sub>	

**TiO**

zrs

NiS<sub>2</sub>(L)

NiS<sub>2</sub>(cr)

P(L)

P(cr)

P(cr)I

RbCl(L)

RbCl(cr)

S(L)

S(a)

S(b)

Si(L)

Si(cr)

SiC(L)

SiO<sub>2</sub>(L)

SiO<sub>2</sub>(a)

SiO<sub>2</sub>(b)

SiO<sub>2</sub>(c)

Sr(L)

Sr(cr)

SrO(L)

SrO(cr)

Ti(L)

Ti(a)

Ti(b)

Ti<sub>2</sub>O<sub>3</sub>(I)

Ti<sub>2</sub>O<sub>3</sub>(II)

Ti<sub>2</sub>O<sub>3</sub>(L)

Ti<sub>3</sub>O<sub>5</sub>(L)

Ti<sub>3</sub>O<sub>5</sub>(a)

Ti<sub>4</sub>O<sub>7</sub>(L)

Ti<sub>4</sub>O<sub>7</sub>(cr)

TiB(cr)

TiB<sub>2</sub>(L)

TiB<sub>2</sub>(cr)

TiC(L)

TiC(cr)

TiCl(cr)

TiCl<sub>2</sub>(cr)

TiCl<sub>3</sub>(cr)

TiCl<sub>4</sub>(L)

TiN(L)

TiN(cr)

TiO(a)

TiO(b)

TiO(c)

TiO<sub>2</sub>(cr)

V(L)

V(cr)

V<sub>2</sub>O<sub>3</sub>(L)

V<sub>2</sub>O<sub>3</sub>(cr)

V<sub>2</sub>O<sub>4</sub>(I)

V<sub>2</sub>O<sub>4</sub>(II)

V<sub>2</sub>O<sub>4</sub>(L)

V<sub>2</sub>O<sub>5</sub>(L)

V<sub>2</sub>O<sub>5</sub>(cr)

VN(cr)

VO(L)

VO(cr)

Zn(L)

Zn(cr)

Zr(L)

Zr(a)

Zr(b)

ZrO<sub>2</sub>(cr)

**VO**

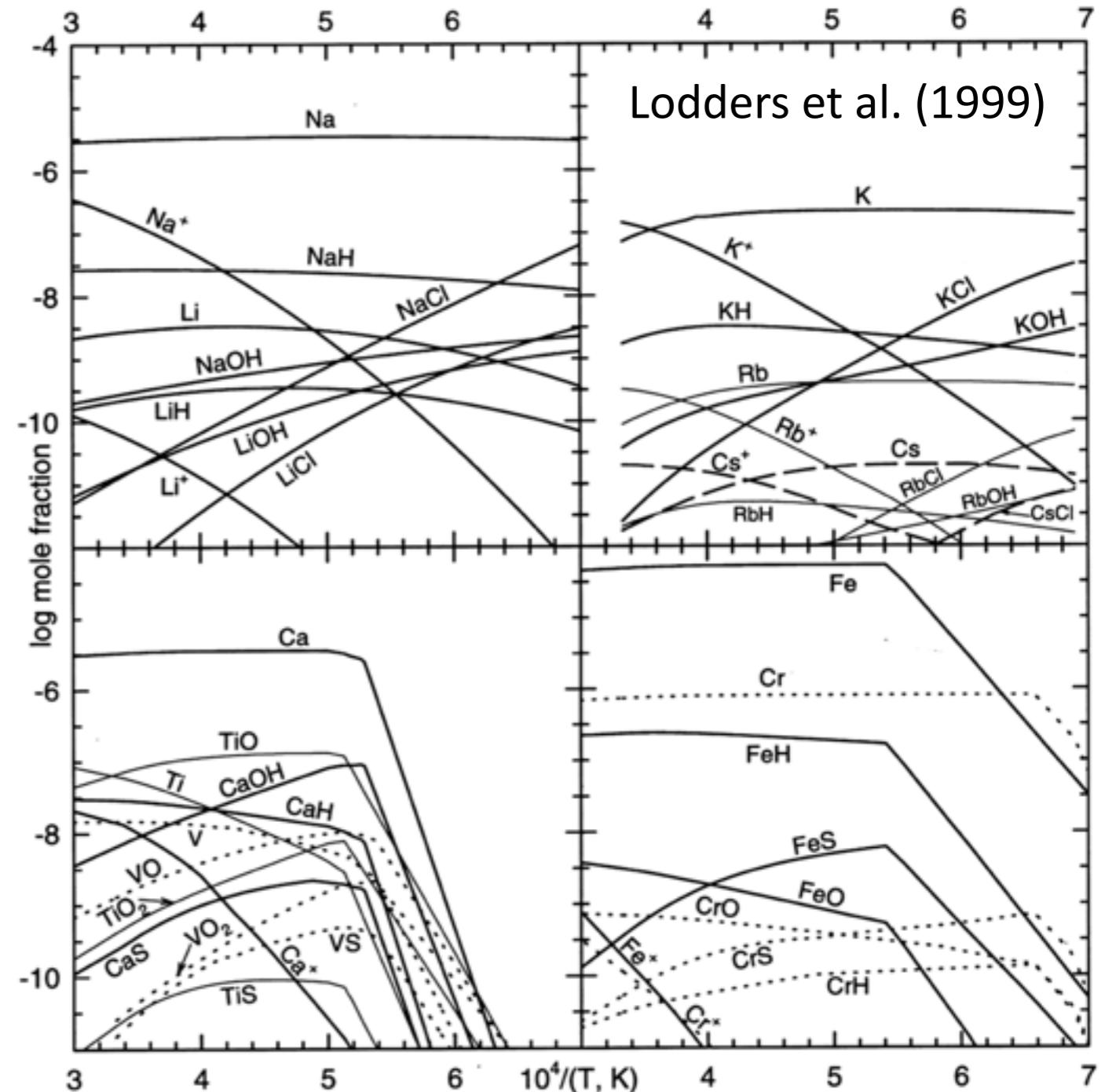
Al <sub>2</sub>	Al <sub>2</sub> O	Al <sub>2</sub> O <sub>2</sub>	Al <sub>2</sub> O <sub>3</sub>	AlBO <sub>2</sub>	AlC	AlCl	AlCl <sub>2</sub>	AlClF	AlF
AlF <sub>2</sub>	AlH	AlHO <sub>2</sub>	AlN	AlO	AlO <sub>2</sub>	AlOCl	AlOF	AlOF <sub>2</sub>	AlOH
AlS	B <sub>2</sub>	BC	BCl	BF	BH	BH <sub>2</sub>	BH <sub>3</sub>	BN	BO
BO <sub>2</sub>	BO <sub>2</sub> H <sub>2</sub>	BS	BaCl	BaCl <sub>2</sub>	BaClF	BaF	BaO	BaO <sub>2</sub> H <sub>2</sub>	BaOH
BaS	Be <sub>2</sub> O	Be <sub>3</sub> O <sub>3</sub>	BeBO <sub>2</sub>	BeC <sub>2</sub>	BeCl	BeCl <sub>2</sub>	BeF	BeF <sub>2</sub>	BeH
BeH <sub>2</sub>	BeN	BeO	BeO <sub>2</sub> H <sub>2</sub>	BeOH	BeS	C <sub>2</sub>	C <sub>2</sub> H	C <sub>2</sub> H <sub>2</sub>	C <sub>2</sub> H <sub>4</sub>
C <sub>2</sub> H <sub>6</sub>	C <sub>2</sub> HCl	C <sub>2</sub> HF	C <sub>2</sub> N	C <sub>2</sub> N <sub>2</sub>	C <sub>2</sub> O	C <sub>3</sub>	C <sub>3</sub> H	CH	CH <sub>2</sub>
CH <sub>3</sub>	CH <sub>3</sub> Cl	CH <sub>3</sub> Cl	CH <sub>3</sub> Cl	CH <sub>3</sub> Cl	CH <sub>3</sub> Cl	CH <sub>3</sub> Cl	CO		
CO <sub>2</sub>	COF <sub>2</sub>	Al(L)	Al(cr)	Al <sub>2</sub> O <sub>3</sub> (L)	A	Al <sub>2</sub> O <sub>3</sub> (a)	Al <sub>2</sub> S <sub>3</sub> (b)	Al <sub>2</sub> SiO <sub>5</sub> (an)	Al <sub>3</sub> F <sub>14</sub> Na <sub>3</sub> (L)
CaF	CaF <sub>2</sub>	Al <sub>4</sub> C <sub>3</sub> (cr)	AlN(cr)	B(L)	I	Ba(Cl <sub>2</sub> )	B <sub>4</sub> Li <sub>2</sub> O <sub>7</sub> (L)	B <sub>4</sub> Na <sub>2</sub> O <sub>7</sub> (L)	B <sub>5</sub> H <sub>9</sub> (L)
CrH	CrN	B <sub>8</sub> K <sub>2</sub> O <sub>13</sub> (L)	BLiO <sub>2</sub> (L)	Ba(L)	Ba(cr)	BaCl <sub>2</sub> (L)	Be(L)	Be(cr)	BeO(L)
CuCl	CuF	BeSO <sub>4</sub> (L)	BeSO <sub>4</sub> (a)	BeSO <sub>4</sub> (b)	BeSO <sub>4</sub> (c)	C(gr)	Ca(L)	Ca(a)	Ca(b)
FeH	FeO	Ca <sub>2</sub> Al <sub>2</sub> SiO <sub>7</sub> (a)	Ca <sub>2</sub> MgSi <sub>2</sub> O <sub>7</sub> (L)	Ca <sub>2</sub> MgSi <sub>2</sub> O <sub>7</sub> (a)	Ca <sub>2</sub> MgSi <sub>2</sub> O <sub>7</sub> (b)	Ca <sub>2</sub> SiO <sub>4</sub> (L)	Ca <sub>2</sub> SiO <sub>4</sub> (a)	Ca <sub>2</sub> SiO <sub>4</sub> (b)	Ca <sub>2</sub> SiO <sub>4</sub> (c)
HBS	HCN	Ca <sub>3</sub> Al <sub>2</sub> O <sub>6</sub> (a)	Ca <sub>3</sub> Al <sub>2</sub> Si <sub>3</sub> O <sub>12</sub> (	Ca <sub>3</sub> MgSi <sub>2</sub> O <sub>8</sub> (a)	Ca <sub>3</sub> N <sub>2</sub> (a)	Ca <sub>3</sub> Si <sub>2</sub> O <sub>7</sub> (a)	Ca <sub>3</sub> SiO <sub>5</sub> (a)	CaAl <sub>2</sub> O <sub>4</sub> (a)	CaAl <sub>2</sub> Si <sub>2</sub> O <sub>8</sub> (a)
KCN	KCl	CaAl <sub>2</sub> SiO <sub>6</sub> (a)	CaAl <sub>4</sub> O <sub>7</sub> (a)	CaB <sub>2</sub> O <sub>4</sub> (L)	CaB <sub>2</sub> O <sub>4</sub> (a)	CaB <sub>4</sub> O <sub>7</sub> (L)	CaB <sub>4</sub> O <sub>7</sub> (a)	CaCl <sub>2</sub> (L)	CaCl <sub>2</sub> (cr)
LiNaO	LiOCl	CaF <sub>2</sub> (L)	CaF <sub>2</sub> (a)	CaF <sub>2</sub> (b)	CaFeSi <sub>2</sub> O <sub>6</sub> (c)	CaH <sub>2</sub> (L)	CaH <sub>2</sub> (a)	CaH <sub>2</sub> (b)	CaMgSi <sub>2</sub> O <sub>6</sub> (L)
MgN	MgO	CaMgSi <sub>2</sub> O <sub>6</sub> (a)	Ca	CaTiO <sub>3</sub> (a)	(b)	CaS(L)	CaS(cr)	CaSO <sub>4</sub> (I)	CaSO <sub>4</sub> (II)
NF	NH	CaSO <sub>4</sub> (L)	Ca	Ca		CaTiSiO <sub>5</sub> (L)	CaTiSiO <sub>5</sub> (a)	Ca <sub>2</sub> Fe(L)	Cl <sub>2</sub> S <sub>2</sub> (L)
NS	Na <sub>2</sub>	Cl <sub>2</sub> Sr(L)	Cl	Cl		Cr(L)	Cr(cr1)	Cr(cr2)	Cr <sub>2</sub> O <sub>3</sub> (L)
NaO	NaOH	Cr <sub>2</sub> O <sub>3</sub> (a)	Cr	Cr		Cs(L)	Cs(cr)	Fe(a)	CsCl(a)
O <sub>3</sub>	OBF	CsCl(b)	Cu(L)	Cu(cr)	Cu <sub>2</sub> O(L)	CuO(cr)	Fe(L)	Fe(b)	
PCl <sub>3</sub>	PF	Fe(c)	Fe <sub>2</sub> O <sub>3</sub> (cr)	Fe <sub>3</sub> O <sub>4</sub> (cr)	FeS(L)	FeS(a)	FeS <sub>2</sub> (cr)	H <sub>2</sub> O(L)	
PSF	RbCl	H <sub>2</sub> O(cr)	K(L)	K <sub>2</sub> SO <sub>4</sub> (I)	K <sub>2</sub> SO <sub>4</sub> (II)	K <sub>2</sub> SO <sub>4</sub> (L)	K <sub>2</sub> Si <sub>2</sub> O <sub>5</sub> (L)	K <sub>2</sub> Si <sub>2</sub> O <sub>5</sub> (a)	K <sub>2</sub> Si <sub>2</sub> O <sub>5</sub> (b)
SO <sub>3</sub>	ScO	K <sub>2</sub> Si <sub>2</sub> O <sub>5</sub> (c)	K <sub>2</sub> SiO <sub>3</sub> (L)	K <sub>2</sub> SiO <sub>3</sub> (cr)	KAlSi <sub>2</sub> O <sub>6</sub> (a)	KAlSi <sub>2</sub> O <sub>6</sub> (b)	KAlSi <sub>3</sub> O <sub>8</sub> (a)	KAlSiO <sub>4</sub> (a)	KAlSiO <sub>4</sub> (b)
SiF	SiH	KBF <sub>4</sub> (L)	KBF <sub>4</sub> (a)	KBF <sub>4</sub> (b)	KBH <sub>4</sub> (a)	KBO <sub>2</sub> (L)	KBO <sub>2</sub> (cr)	KOH(L)	KOH(a)
SiO <sub>2</sub>	SiS	KOH(b)	KOH(c)	Li(L)	Li <sub>2</sub> O(L)	Li <sub>2</sub> O <sub>3</sub> S			
SrS	TiCl	Mg	Mg	Mg	Mg <sub>2</sub> SiO <sub>4</sub> (cr)	Mg <sub>2</sub> Ti	MgSiO <sub>3</sub> (L)	MgSiO <sub>3</sub> (cr)	
TiO	TiO <sub>2</sub>	Mg <sub>2</sub> SiO <sub>4</sub> (cr)	Mg <sub>2</sub> SiO <sub>4</sub> (cr)	MgS(cr)	Mn(a)	Mn(c)	Mn(c)	Mn(c)	
ZrCl <sub>2</sub>	ZrCl <sub>3</sub>	Na	NaCl(L)	NaCl(cr)	NaFeSi <sub>2</sub> O <sub>6</sub> (a)	NaH(L)	NaAlSiO <sub>4</sub> (a)	NaAlSiO <sub>4</sub> (b)	NaAlSiO <sub>4</sub> (c)
ZrS		Na	NbO(L)	Ni(L)	Ni(cr)	Ni <sub>3</sub> S <sub>2</sub> (L)	NaH(cr)	Nb(L)	Nb <sub>2</sub> O <sub>5</sub> (L)
		Na	NiS <sub>2</sub> (L)	NiS <sub>2</sub> (cr)	P(L)	P(cr)	Ni <sub>3</sub> S <sub>2</sub> (a)	Ni <sub>3</sub> S <sub>2</sub> (b)	NiS(a)
		Na	S(a)	S(b)	Si(L)	Si(cr)	P(cr)1	RbCl(L)	RbCl(cr)
		Na	SiO <sub>2</sub> (c)	Sr(L)	Sr(cr)	SrO(L)	SiC(L)	SiO <sub>2</sub> (L)	S(L)
		Na	Ti <sub>2</sub> O <sub>3</sub> (I)	Ti <sub>2</sub> O <sub>3</sub> (II)	Ti <sub>2</sub> O <sub>3</sub> (L)	Ti <sub>3</sub> O <sub>5</sub> (L)	Ti <sub>3</sub> O <sub>5</sub> (a)	Ti <sub>4</sub> O <sub>7</sub> (L)	Ti <sub>4</sub> O <sub>7</sub> (cr)
		Na	TiB <sub>2</sub> (L)	TiB <sub>2</sub> (cr)	TiC(L)	TiC(cr)	TiCl(cr)	TiCl <sub>2</sub> (cr)	TiCl <sub>3</sub> (cr)
		Na	TiN(L)	TiN(cr)	TiO(a)	TiO(b)	TiO(c)	TiO <sub>2</sub> (cr)	TiCl <sub>4</sub> (L)
		Na	V <sub>2</sub> O <sub>3</sub> (L)	V <sub>2</sub> O <sub>3</sub> (cr)	V <sub>2</sub> O <sub>4</sub> (I)	V <sub>2</sub> O <sub>4</sub> (II)	V <sub>2</sub> O <sub>4</sub> (L)	V <sub>2</sub> O <sub>5</sub> (L)	V <sub>2</sub> O <sub>5</sub> (cr)
		Na	VO(L)	VO(cr)	Zn(L)	Zn(cr)	Zr(L)	Zr(a)	VN(cr)
		Na	ZrSiO <sub>4</sub> (cr)				Zr(b)	ZrO <sub>2</sub> (cr)	

## Chemical Equilibrium (in a box)

- independent of time
- independent of box history
- all fluctuations are damped out
- independent of position in box
- $p_i = f(T, P, a_j)$  (partial pressure)

$$p_i = \left( \frac{n_i}{n_{tot}} \right) P_{gas} = x_i P_{gas}$$

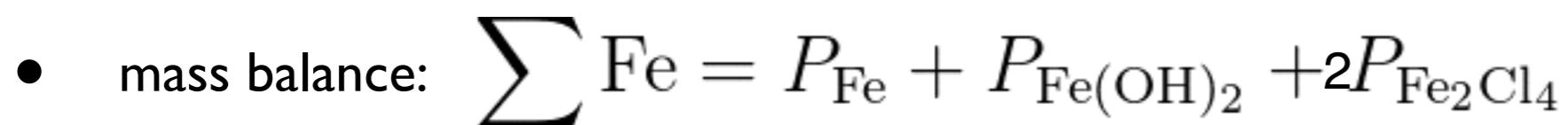
$x_i$  = mole fraction



Important references:  
Fegley & Lodders (1994)  
Burrows & Sharp (1999)

## Equilibrium Chemistry (in a nutshell) More on this later ...

- Simplified example: Iron in Jupiter's atmosphere



- Expressed in terms of thermodynamic quantities:

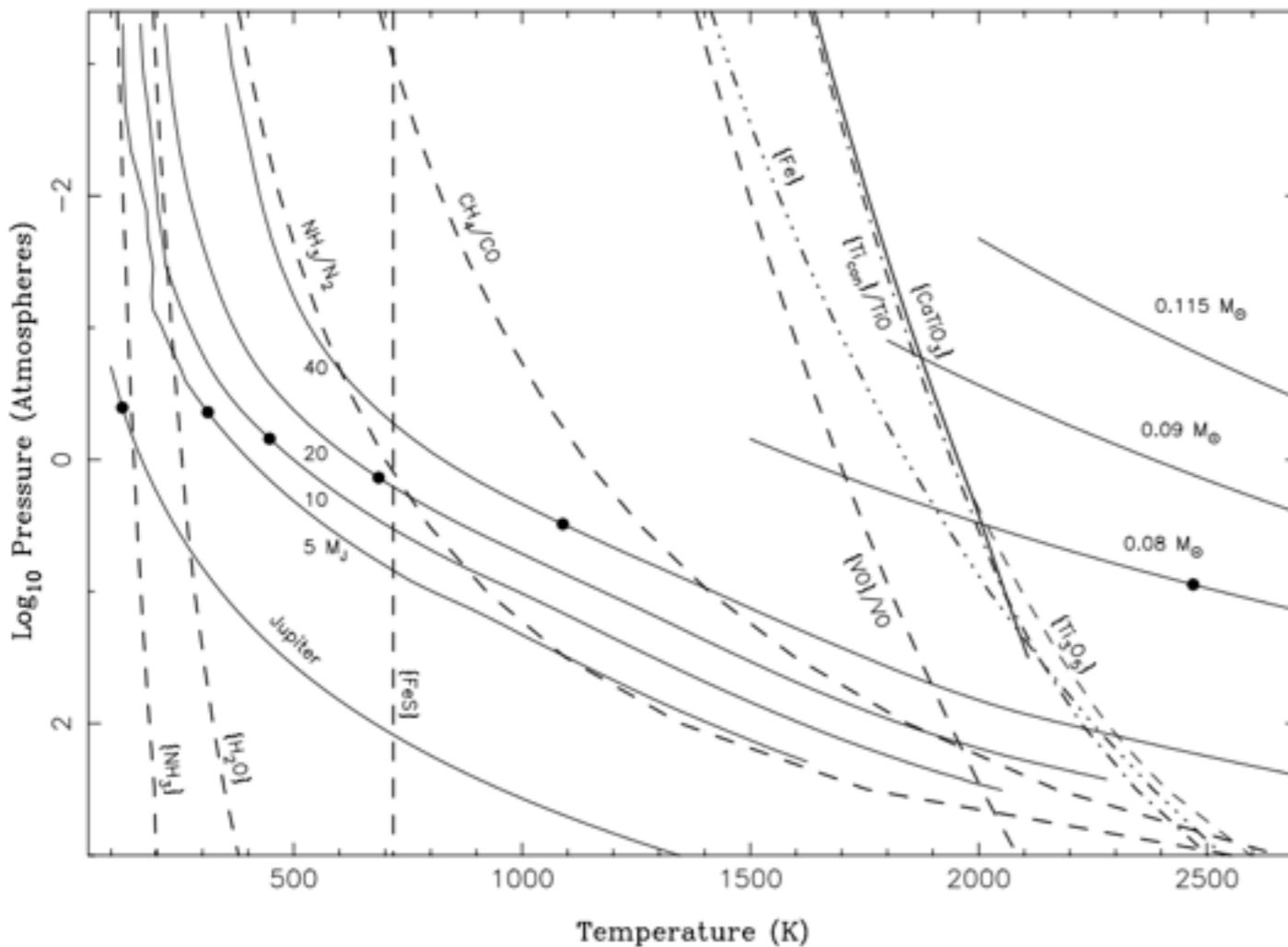
$$\sum \text{Fe} = a_{\text{Fe}} [K_{\text{Fe}} + K_{\text{Fe(OH)}_2}(f_{\text{H}_2})(f_{\text{O}_2}) + 2a_{\text{Fe}}K_{\text{Fe}_2\text{Cl}_4}(f_{\text{Cl}_2})^2]$$

- system of equations for each element (each equation can be very long, e.g., hydrogen can have 100s of terms)

- solved for f, numerically, with some initial guesses and fixed element abundances. Equivalent to minimizing the Gibbs potential

- Alternative methods used (examples discussed later)

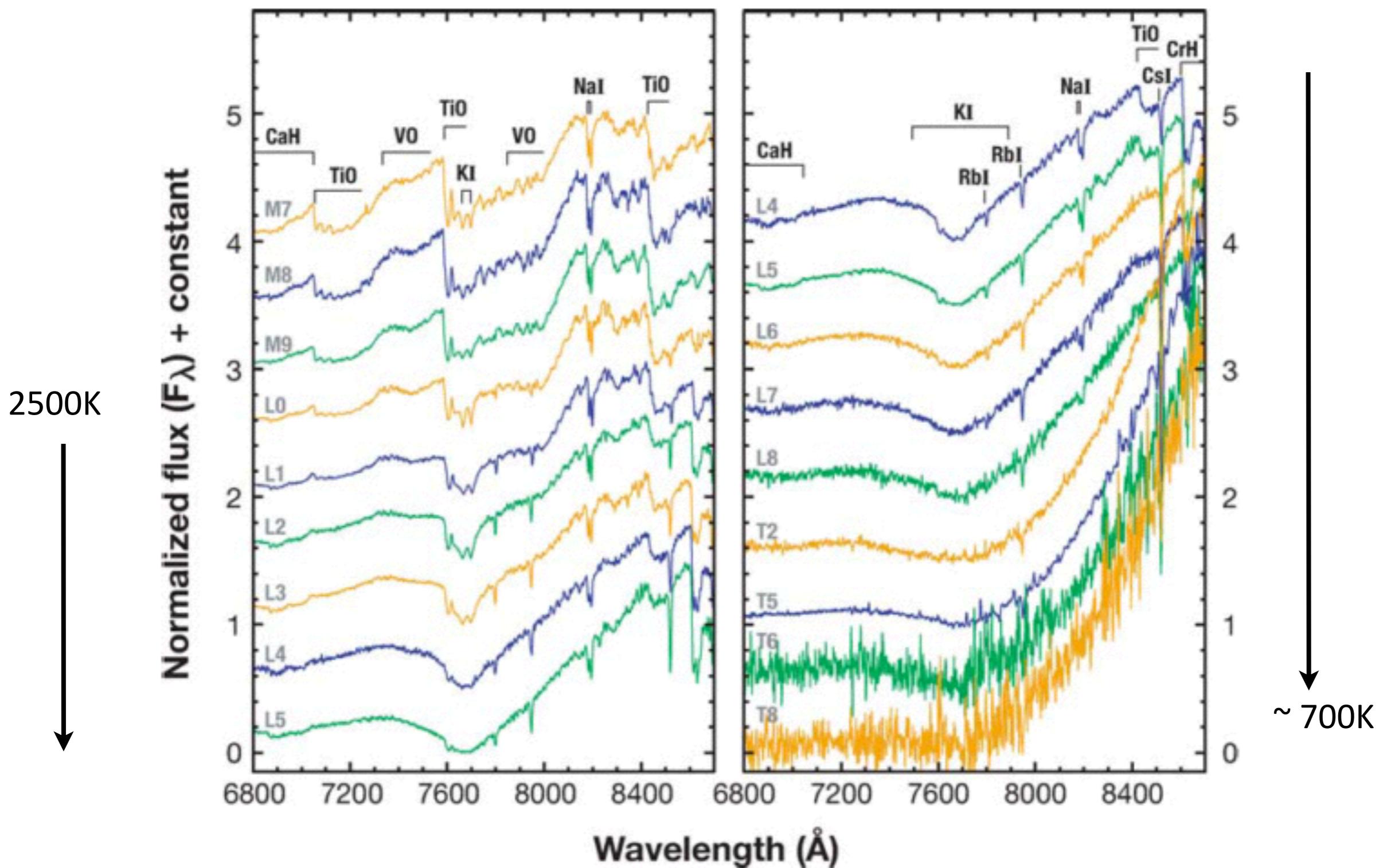
Results of model atmosphere calculations  
(See also Allard et al. 2001)



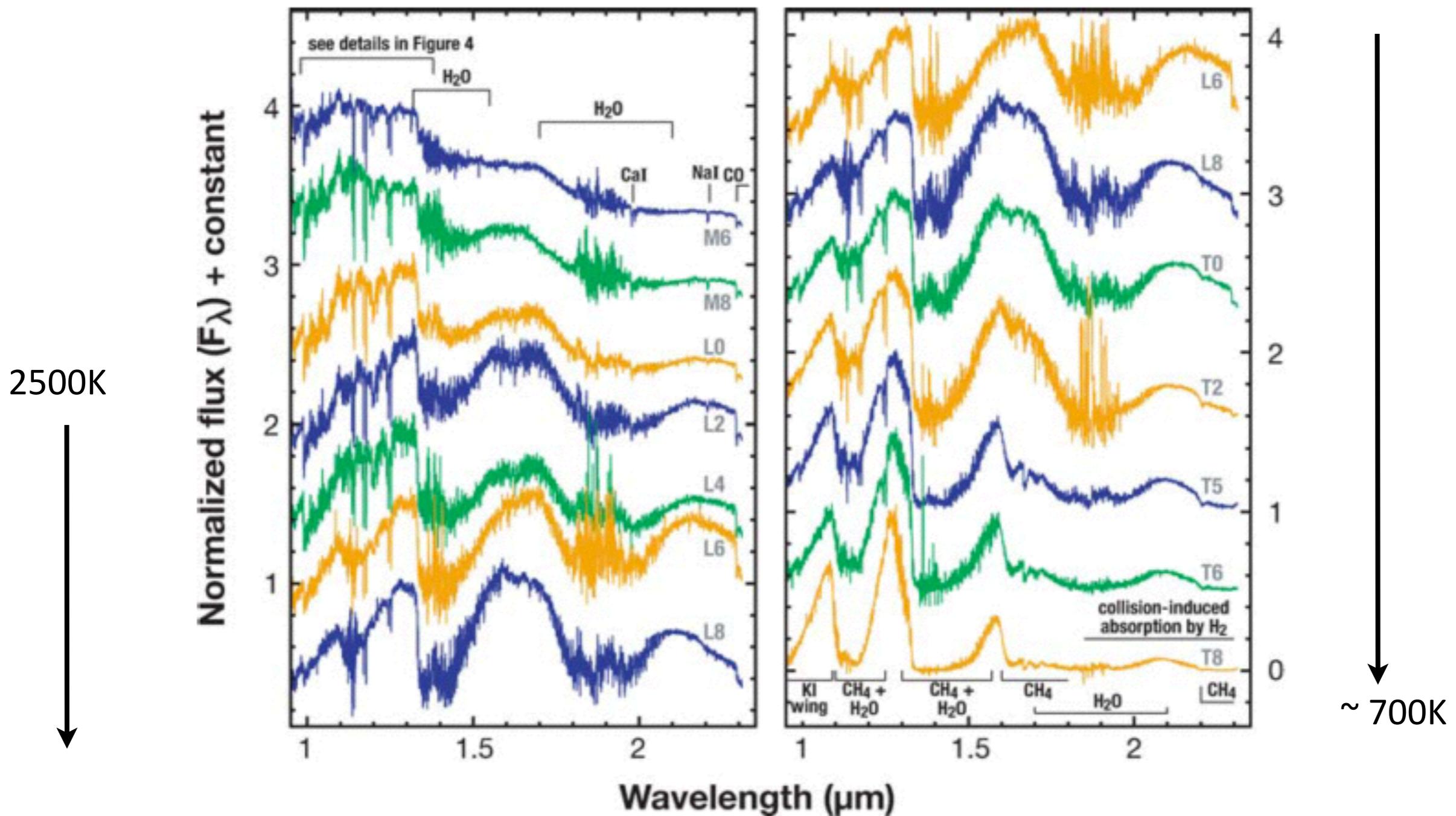
*Temperature Structures* of sub-stellar mass objects:

- chemical equilibrium
- hydrostatic equilibrium
- radiative+convective equilibrium
- one-dimension (radial)
- time-independent
- fixed abundances (e.g. “solar”)

## A quick introduction to *spectral types* of brown dwarfs

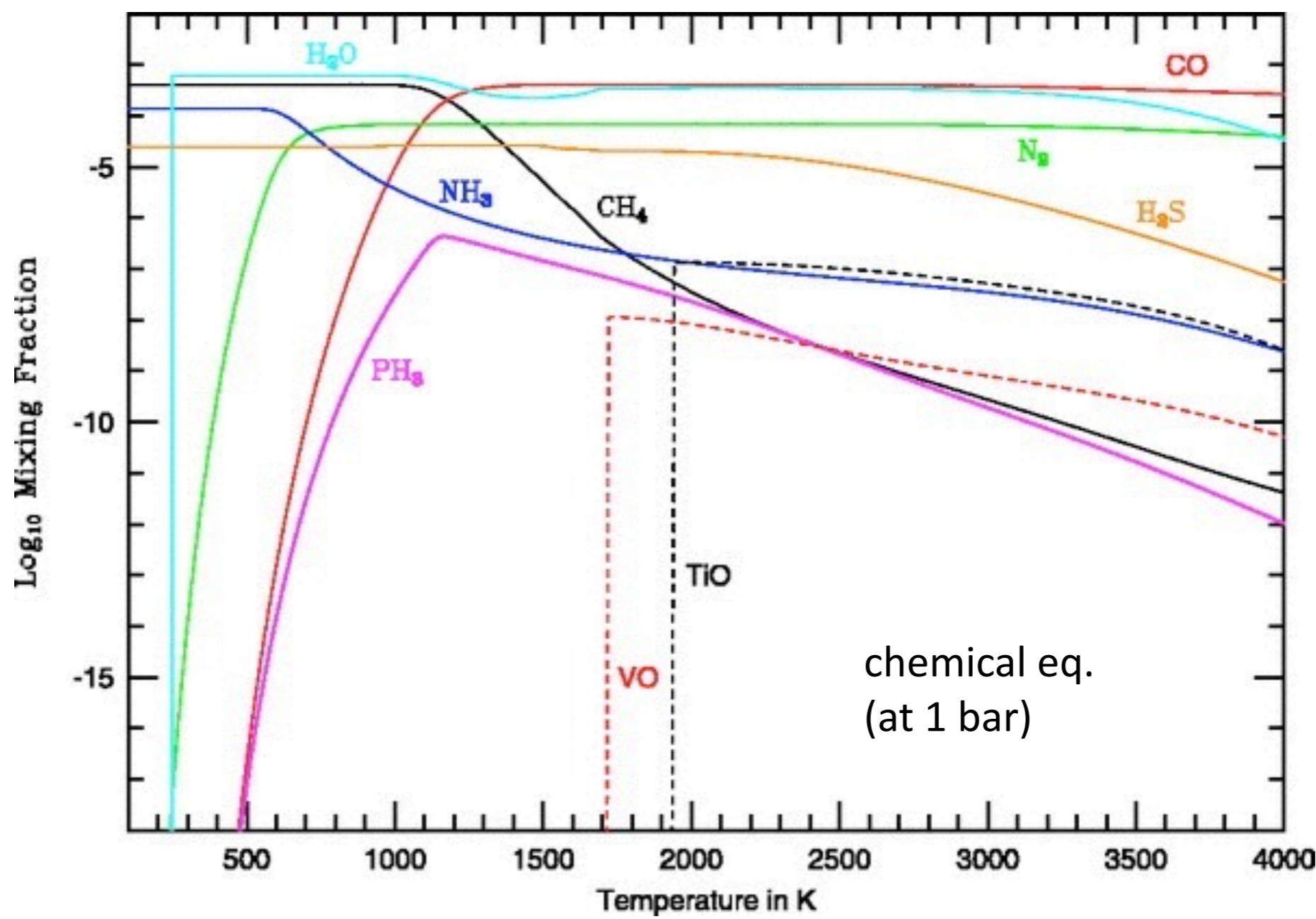
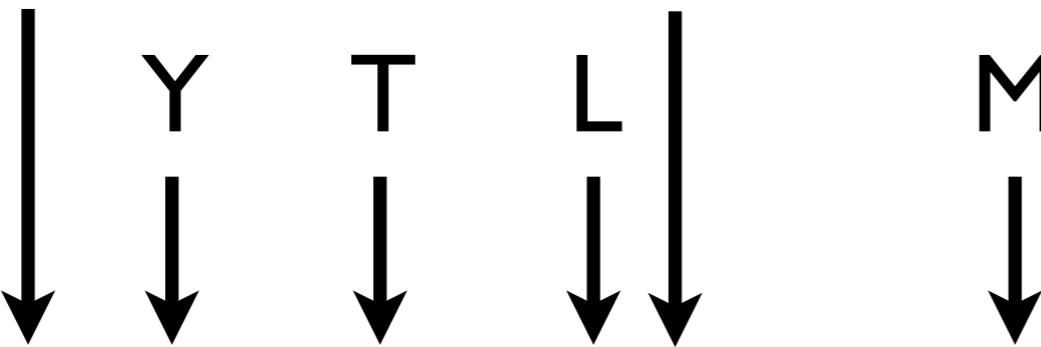


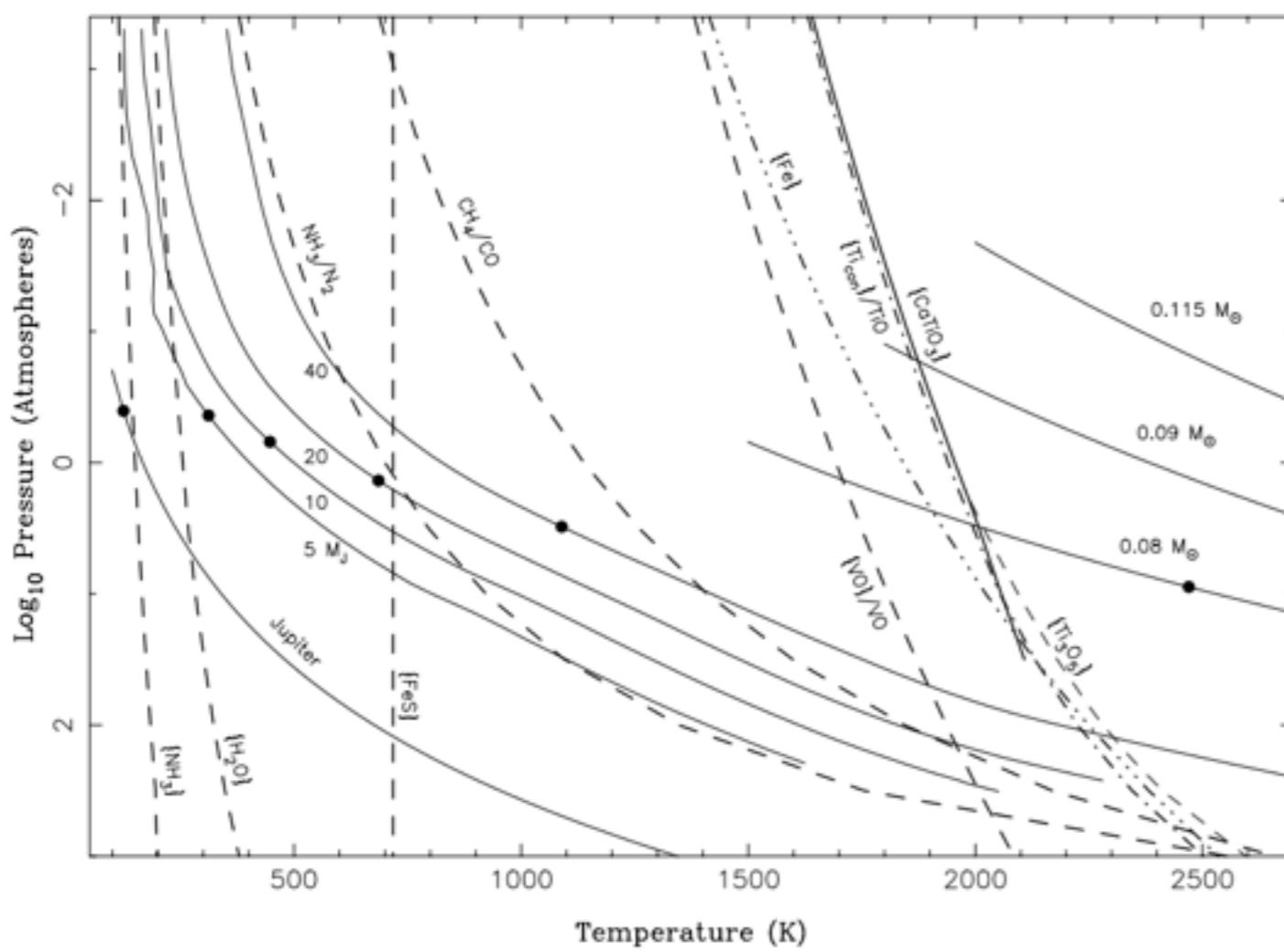
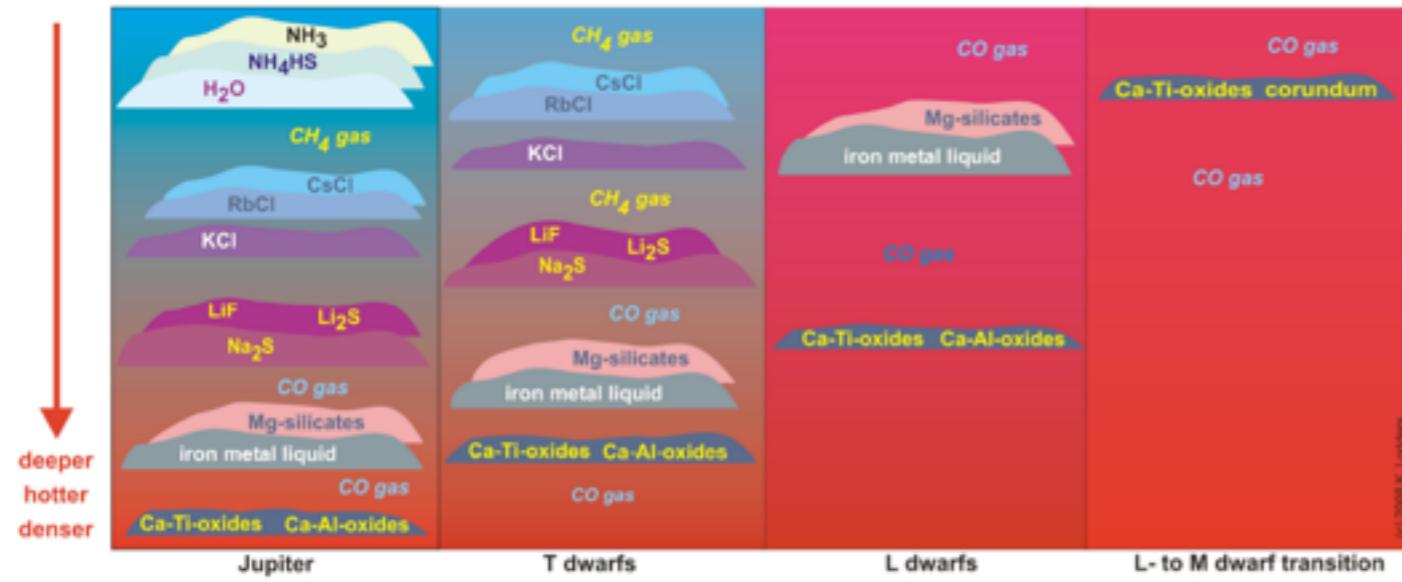
## A quick introduction to *spectral types* of brown dwarfs



Jupiter

HD 189733



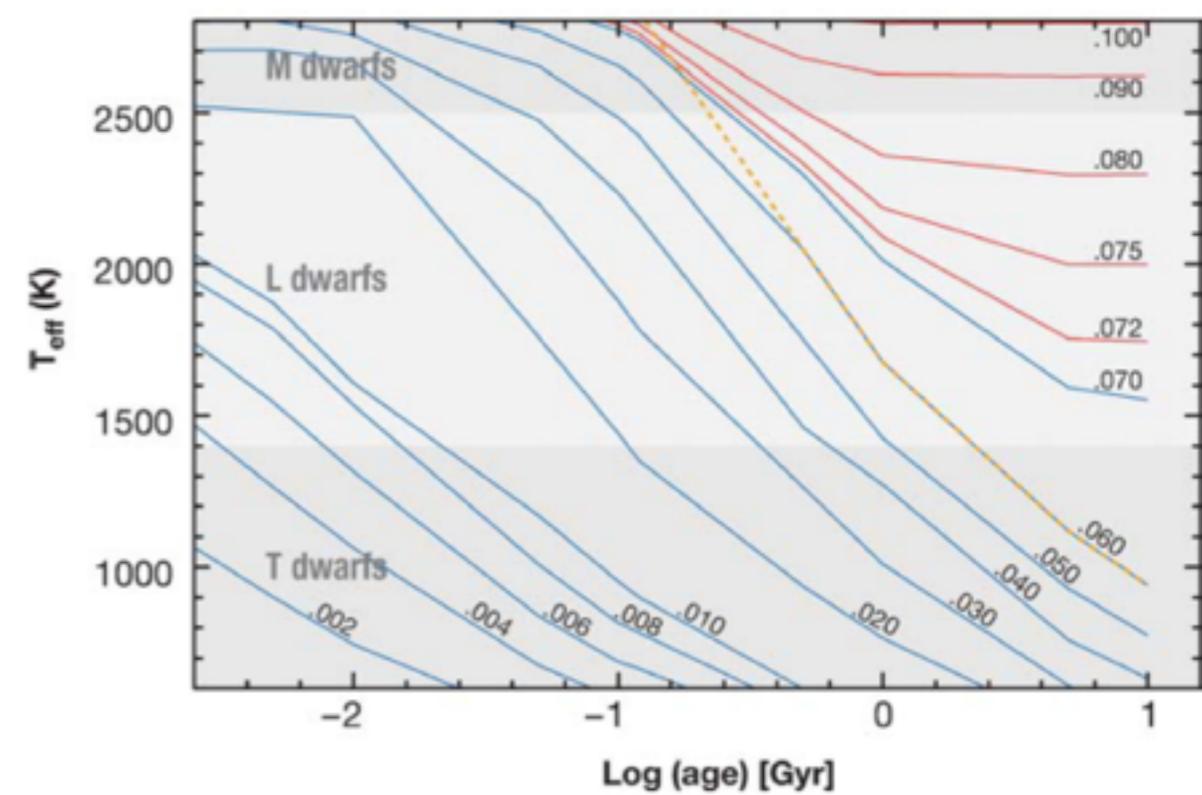
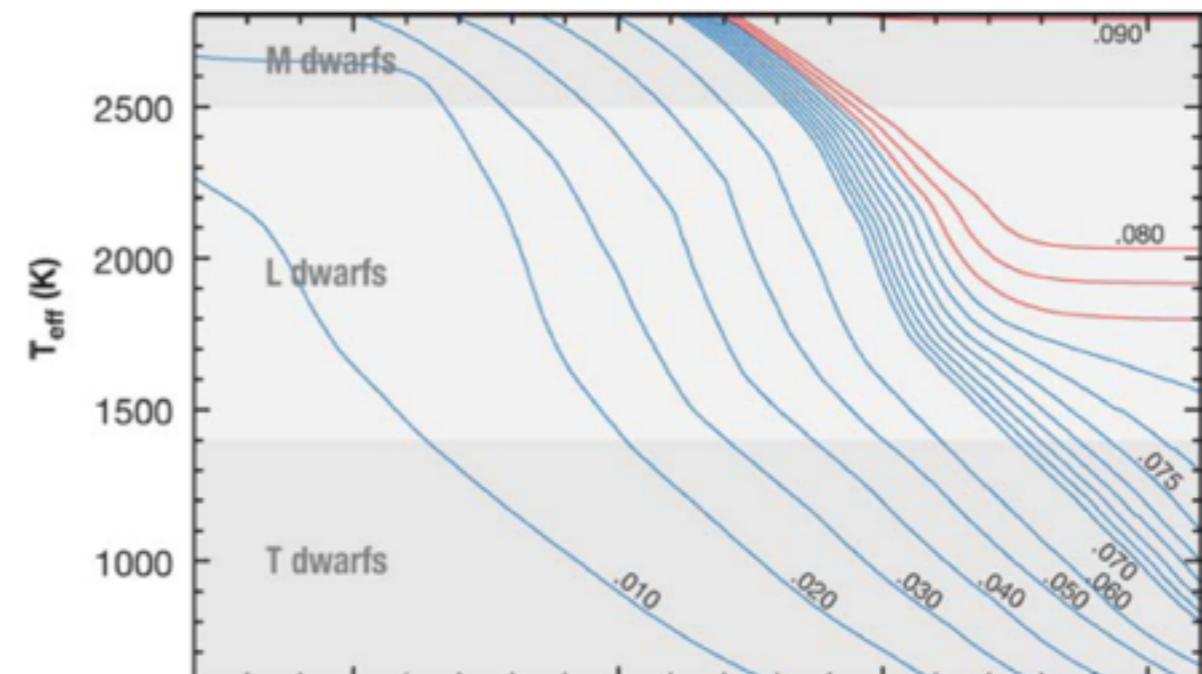
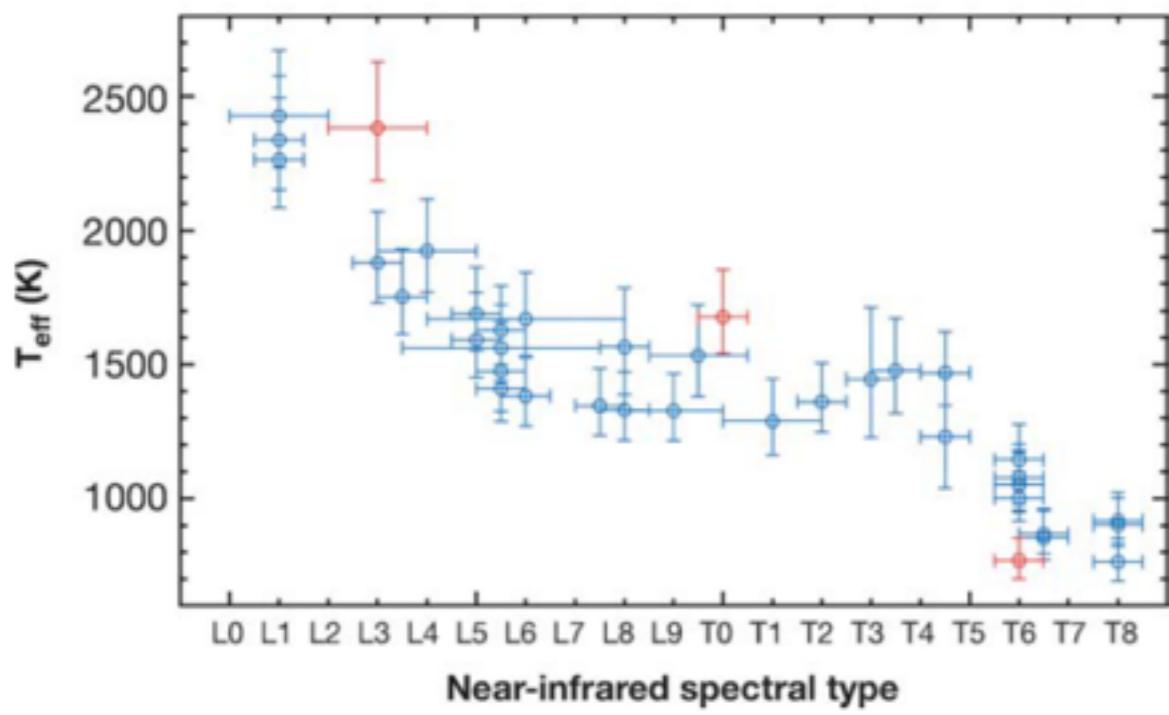
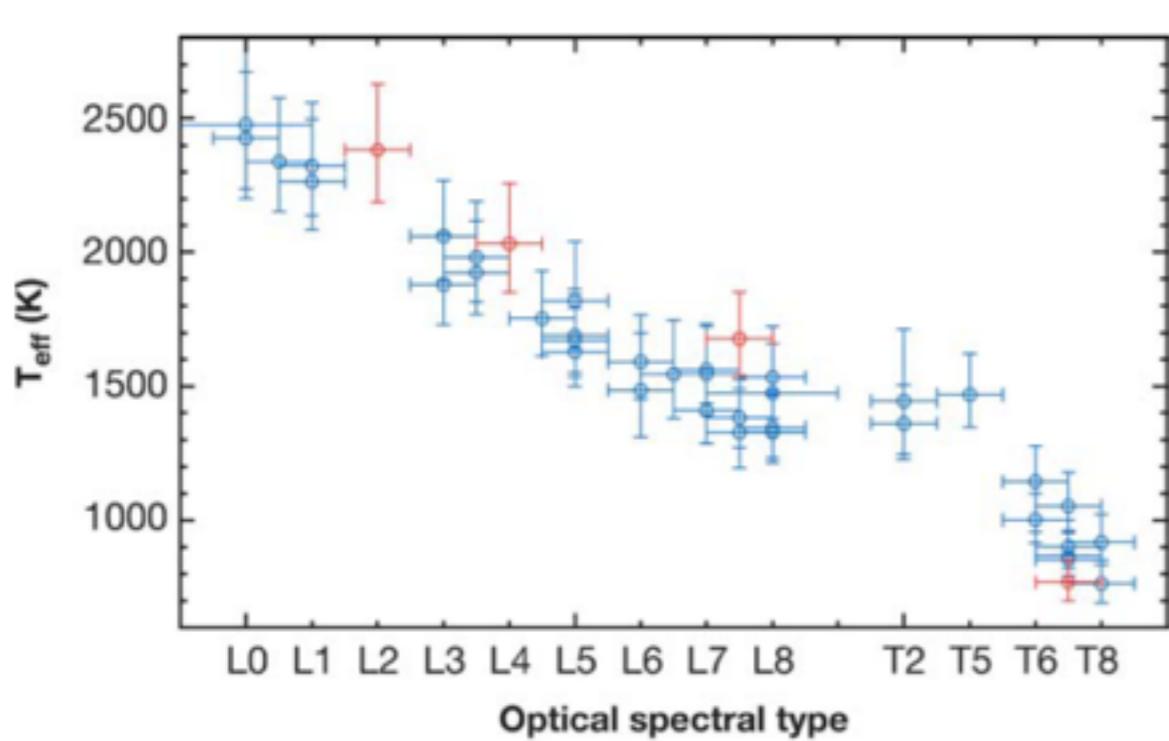


Results of model atmosphere calculations  
(See also Allard et al. 2001)

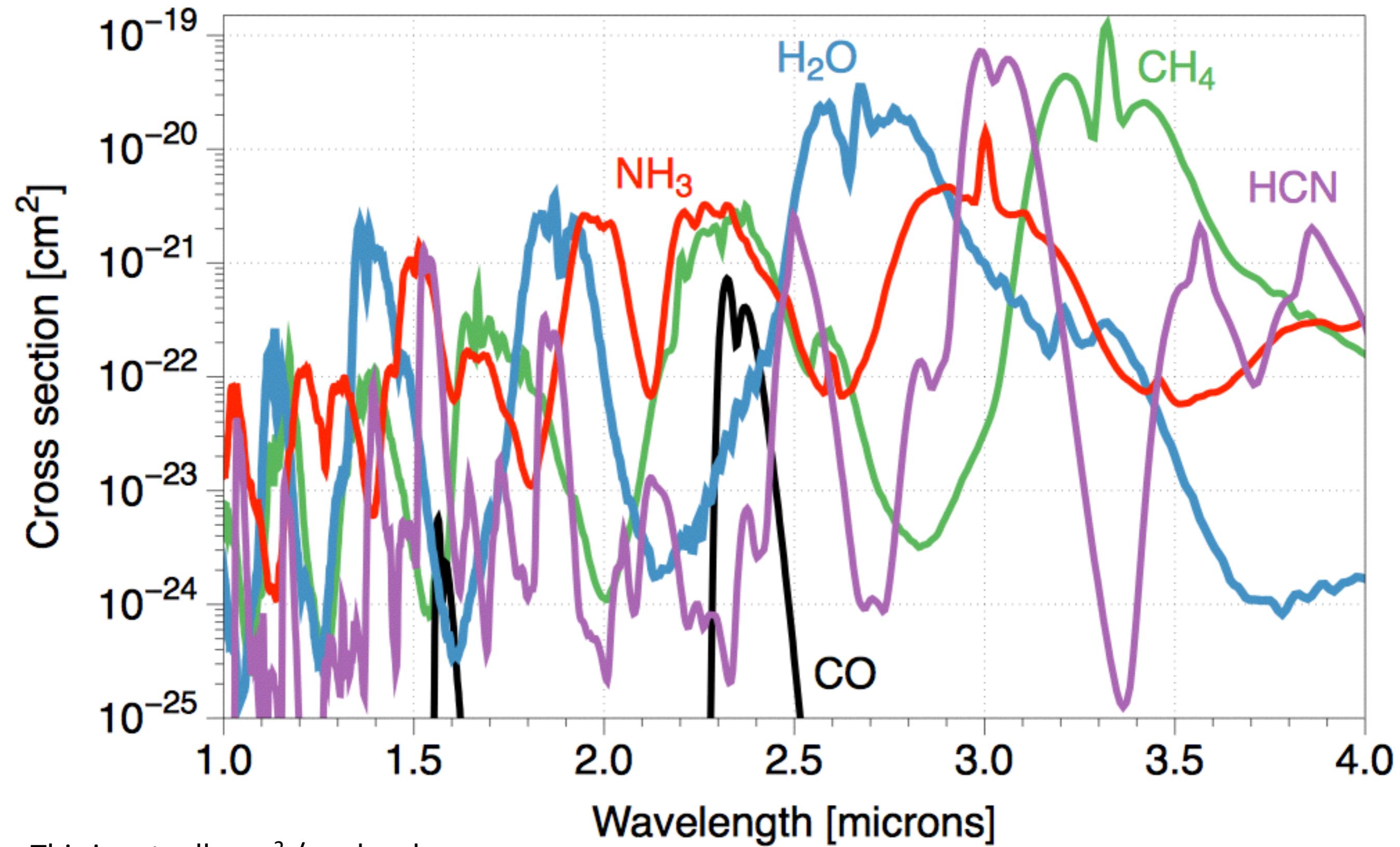
- chemical equilibrium
- hydrostatic equilibrium
- radiative+convective equilibrium
- one-dimension (radial)
- time-independent
- fixed abundances (e.g. “solar”)

*Temperature Structures of sub-stellar mass objects:*

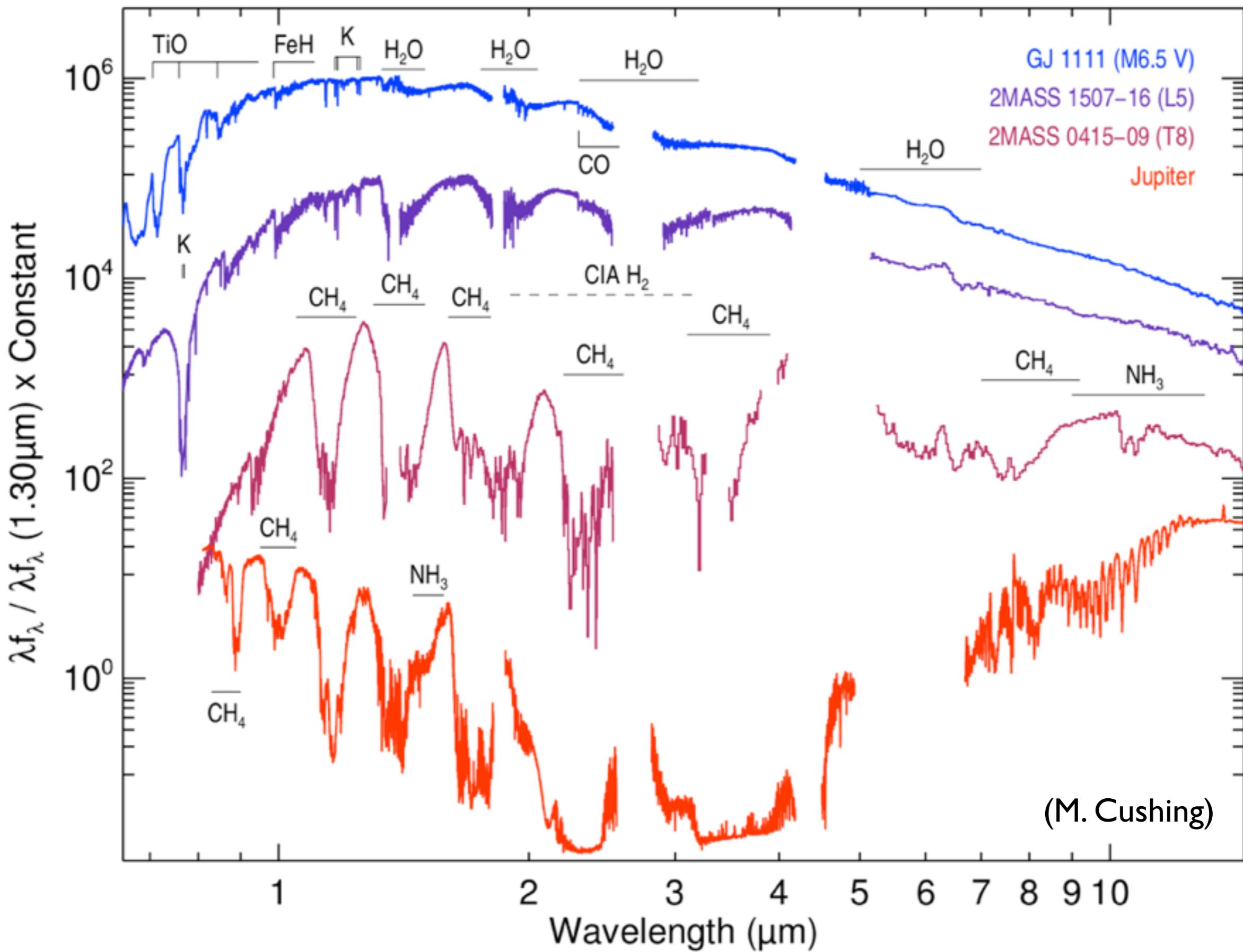
A single object evolves through the Spectral Type  
(SpT(Teff) also not exactly a unique function at low T)



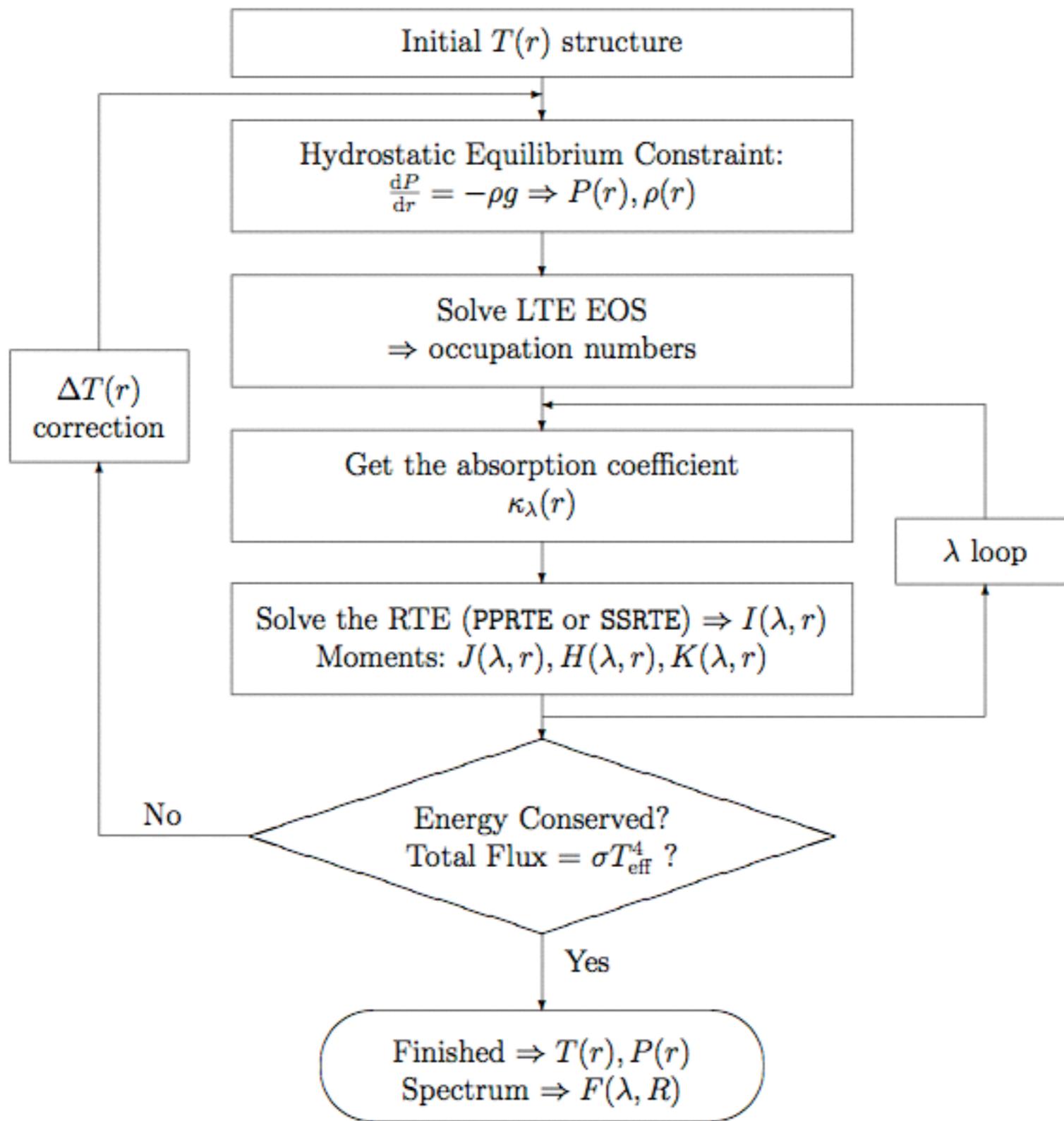
major molecular absorbers  
(NOT “continuous” -- 100s of billions of lines)



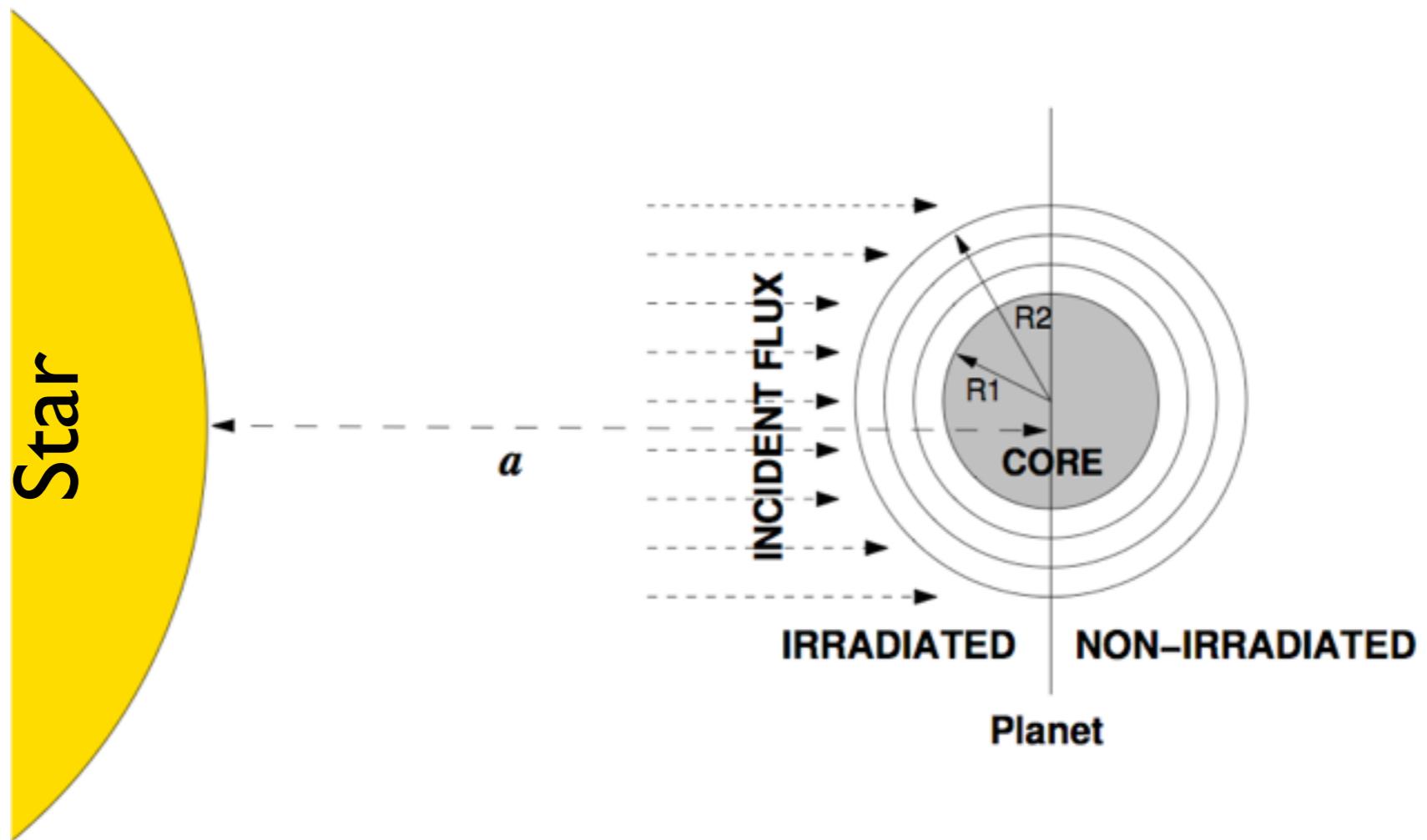
This is actually  $\text{cm}^2 / \text{molecule}$

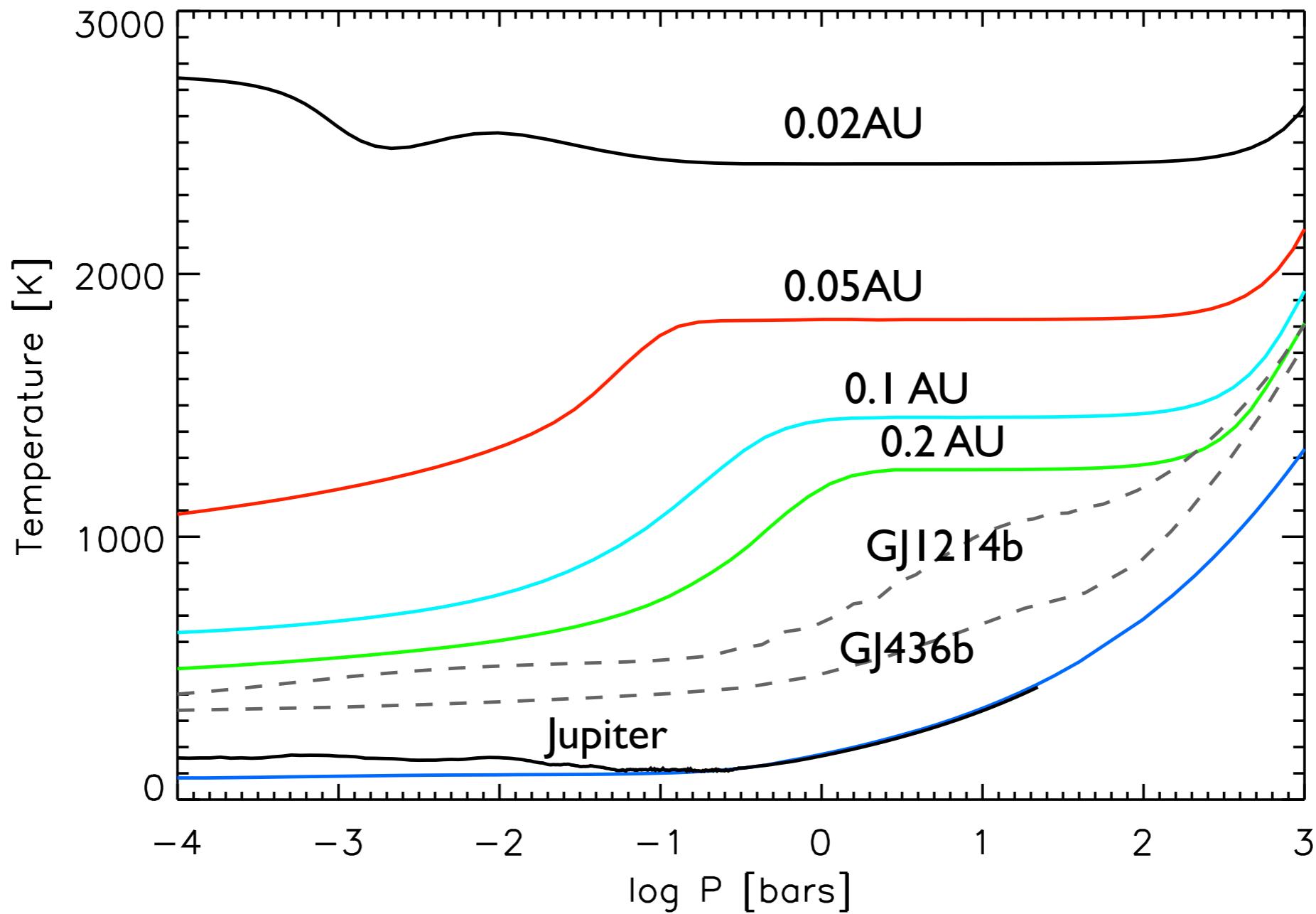


# The basic model atmosphere recipe:

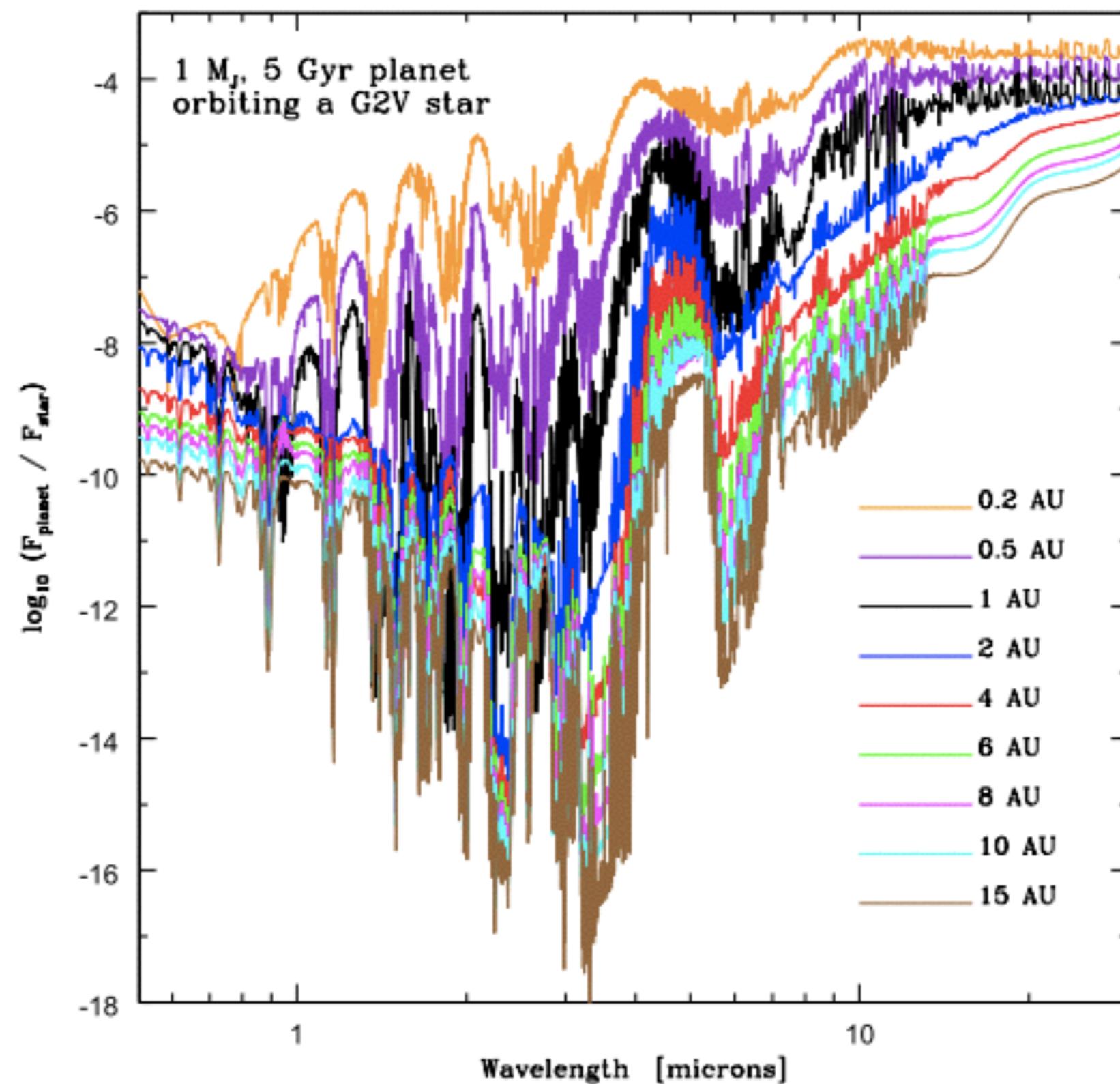


Major distinction between most brown dwarfs  
and giant planets -- incident stellar flux.

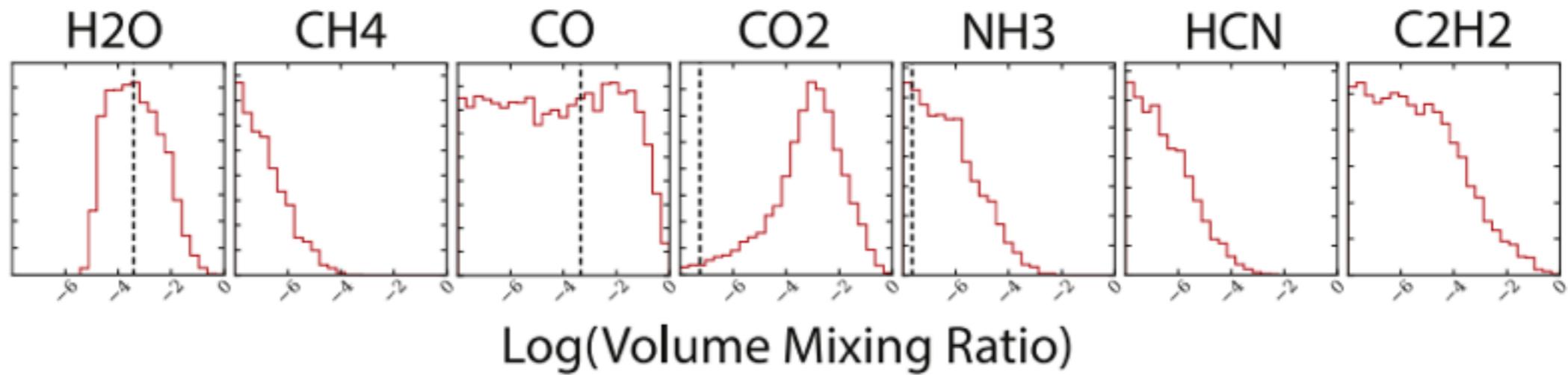
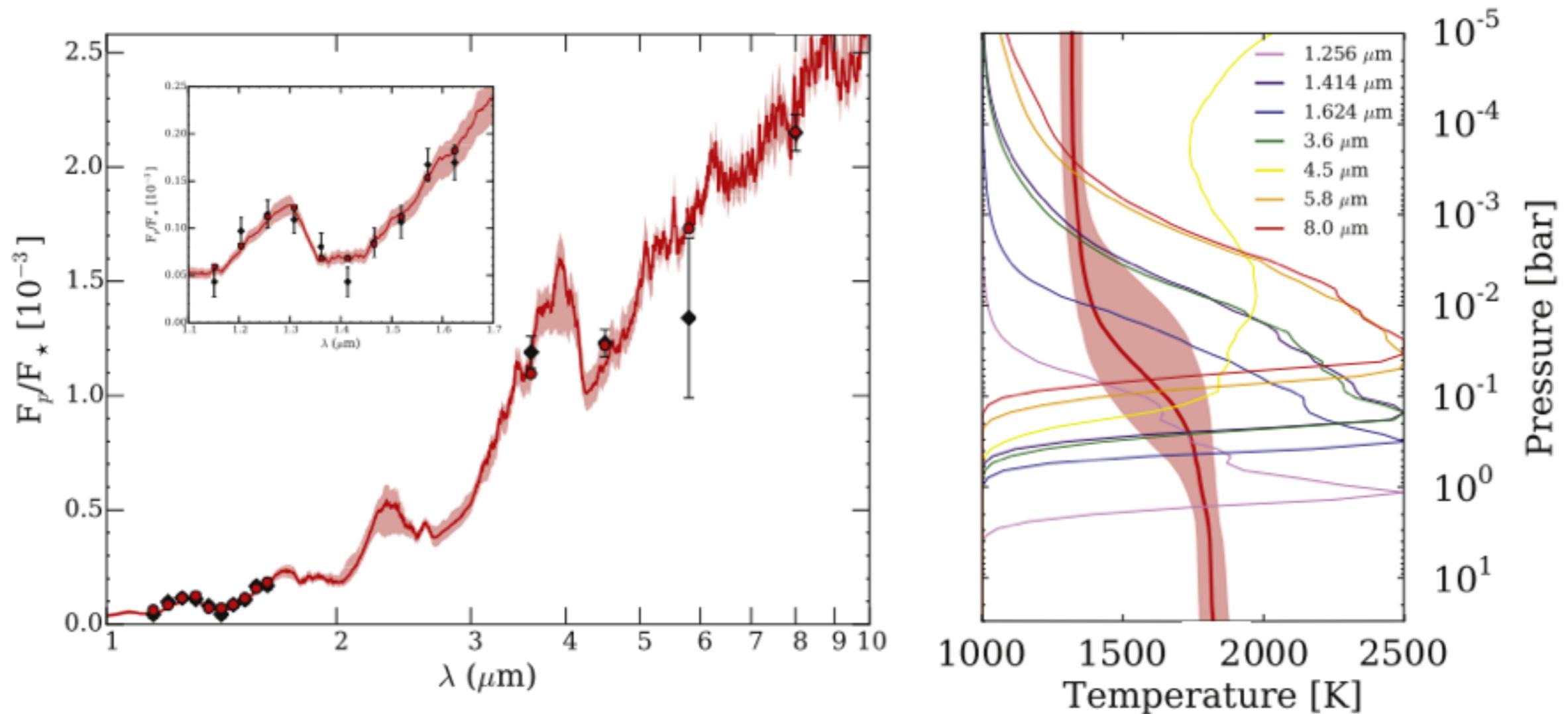


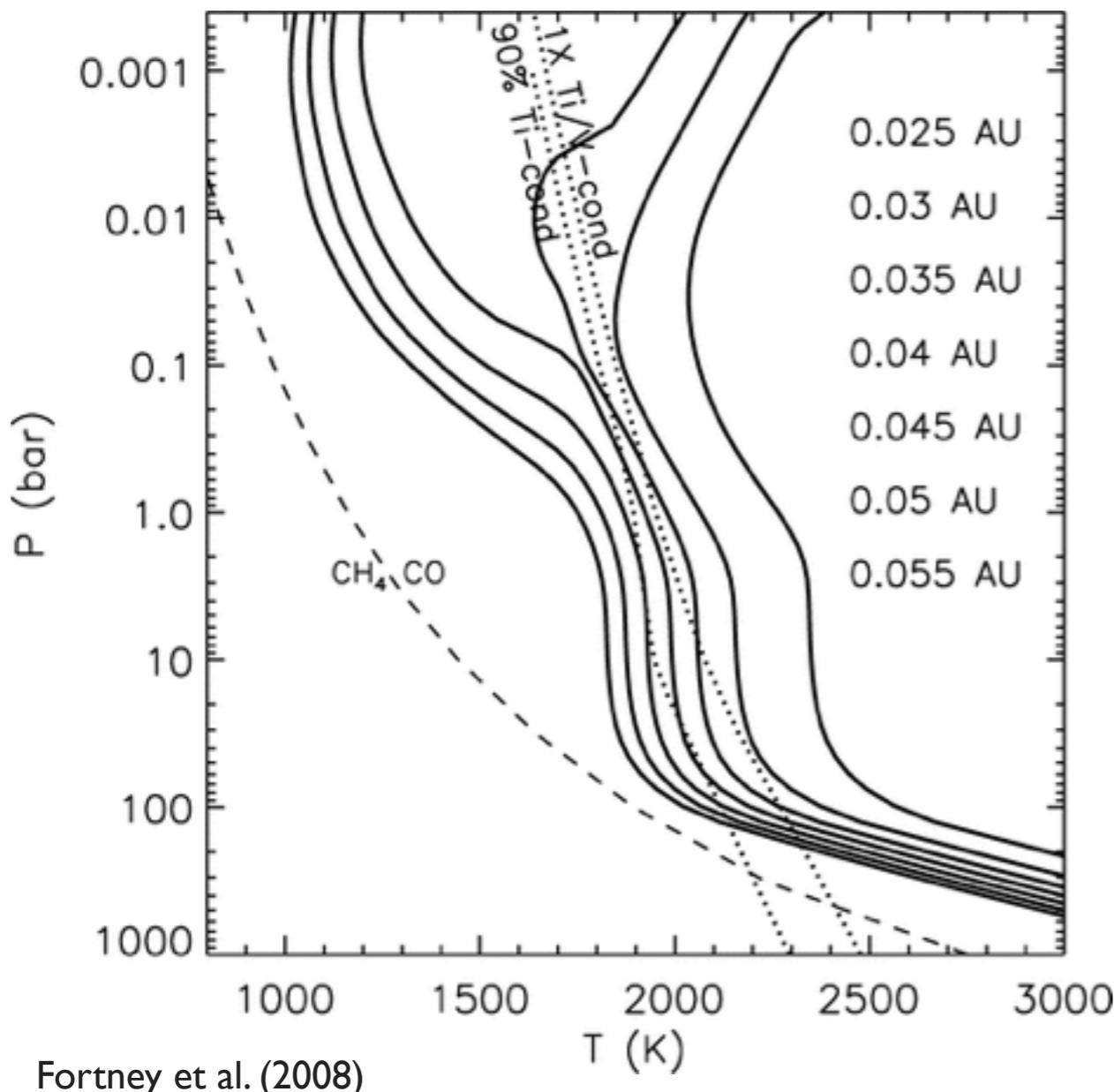


## “Synthetic” Exoplanet Spectra

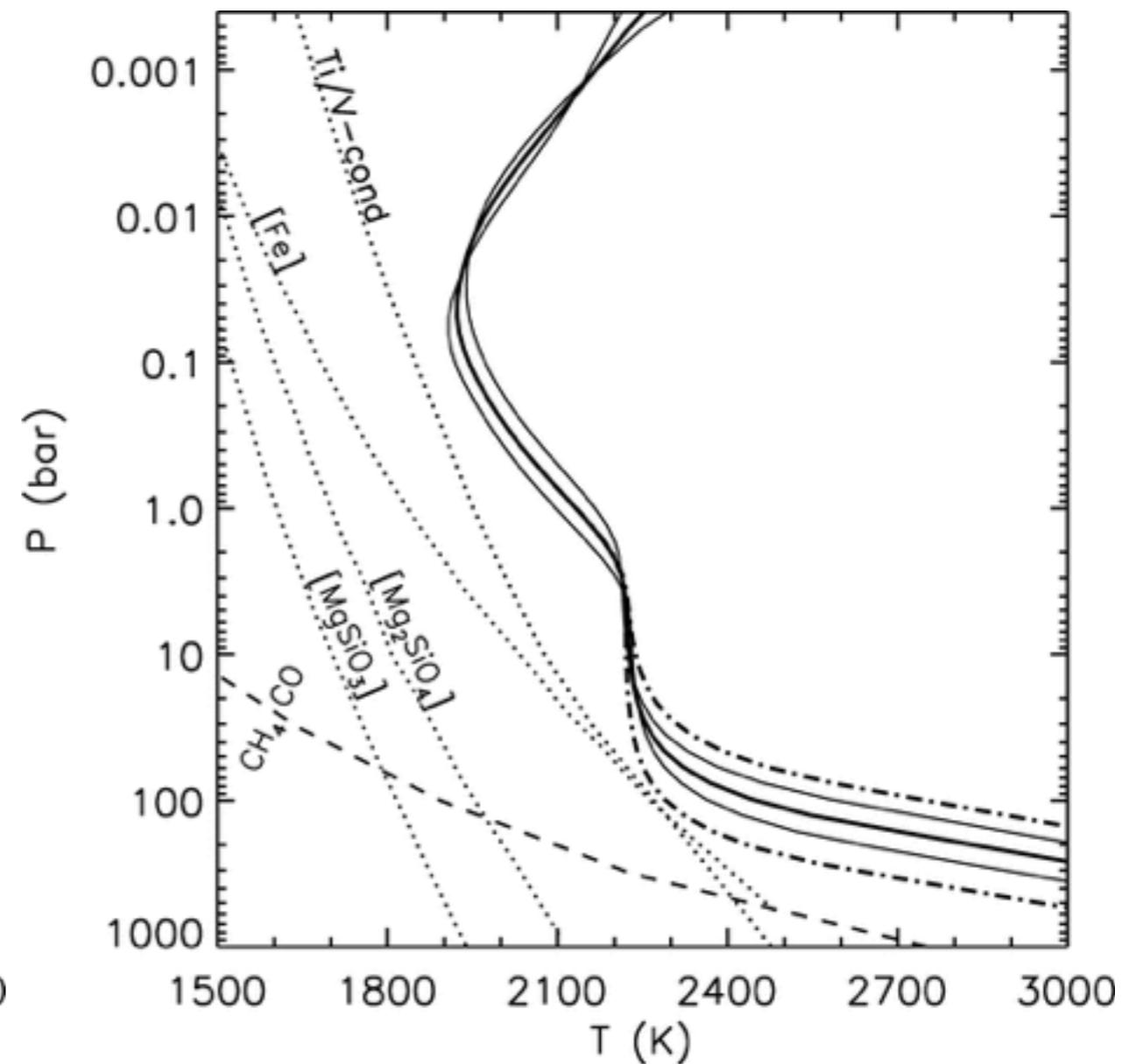


# HD209458b

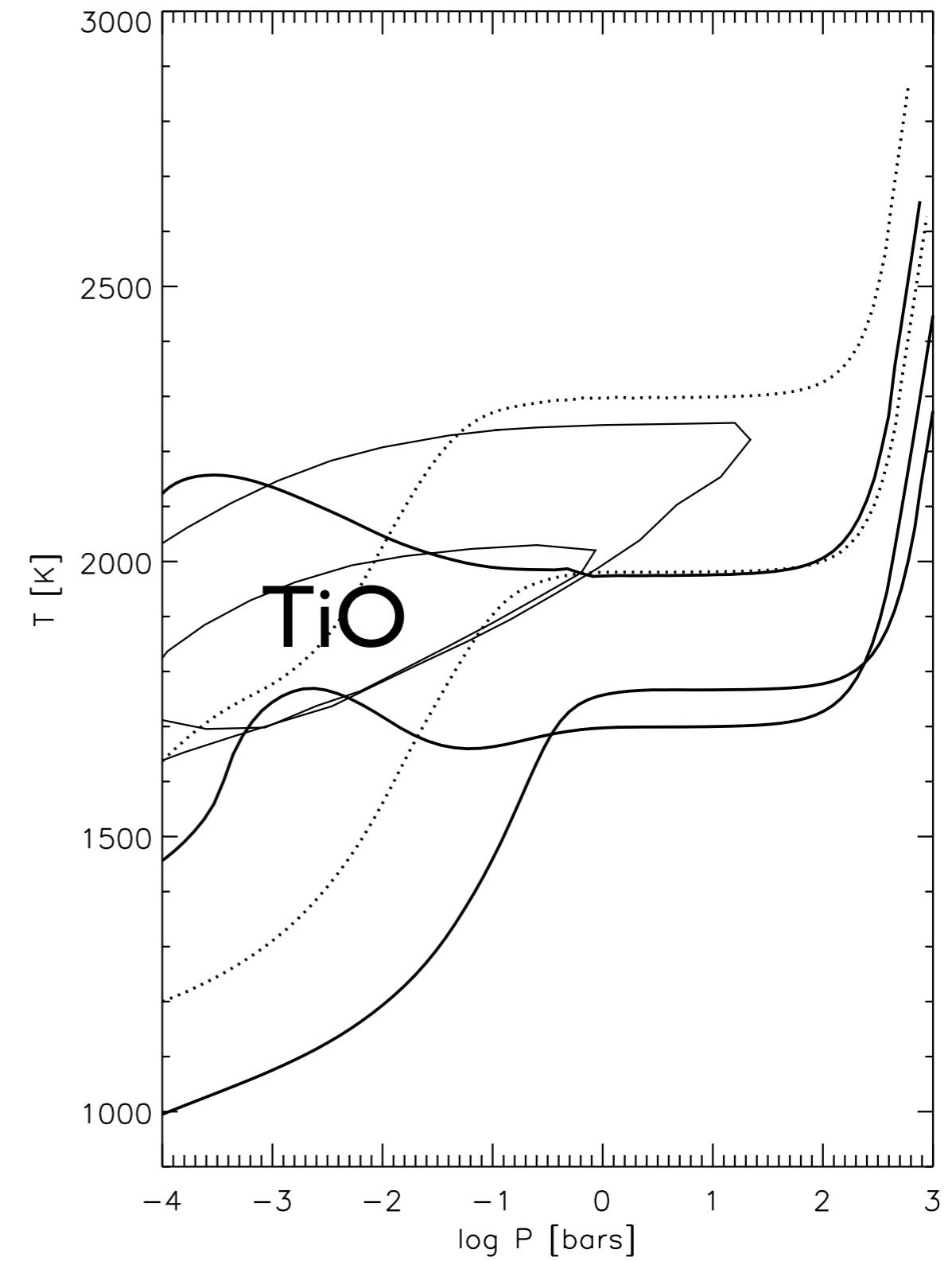
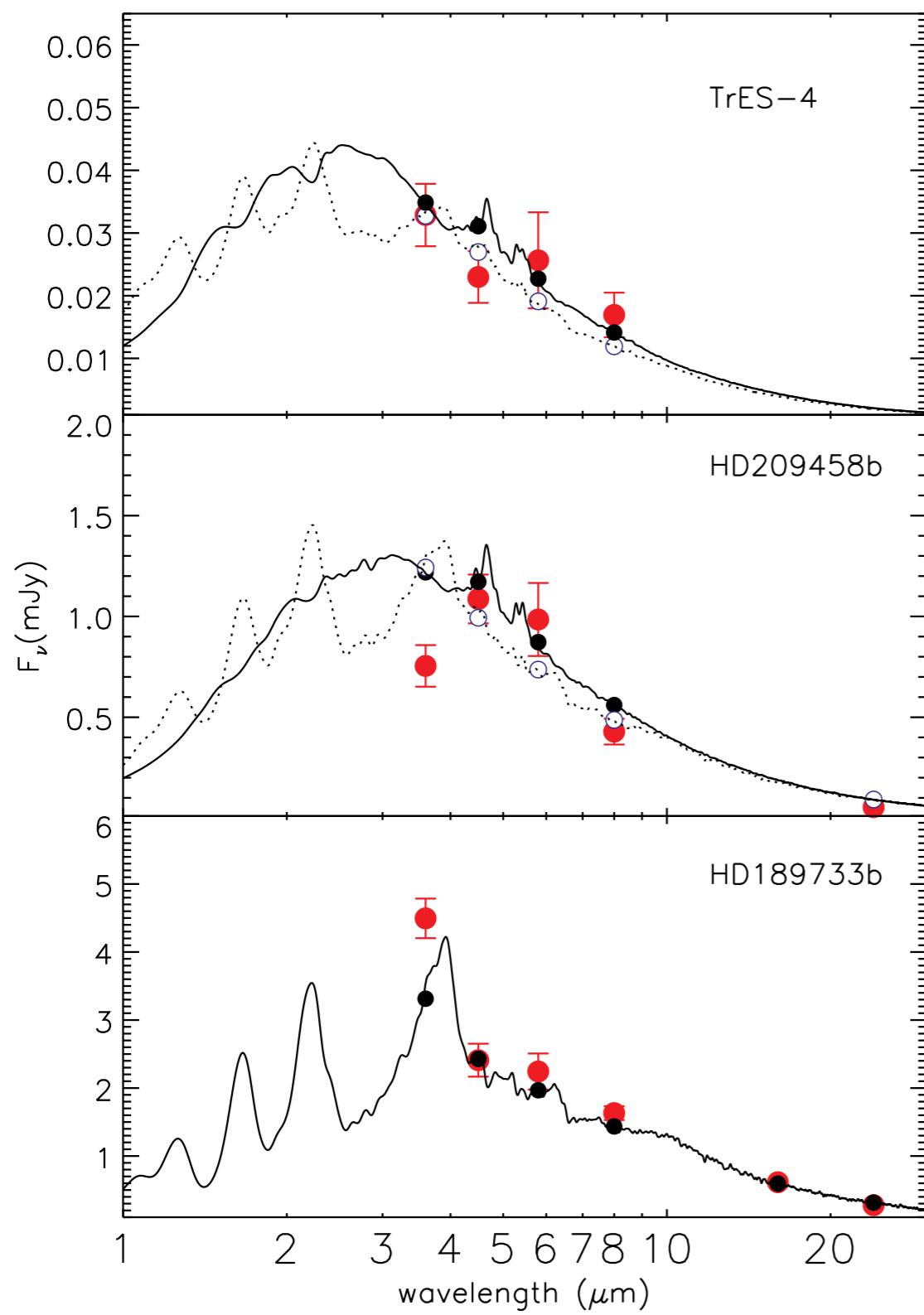




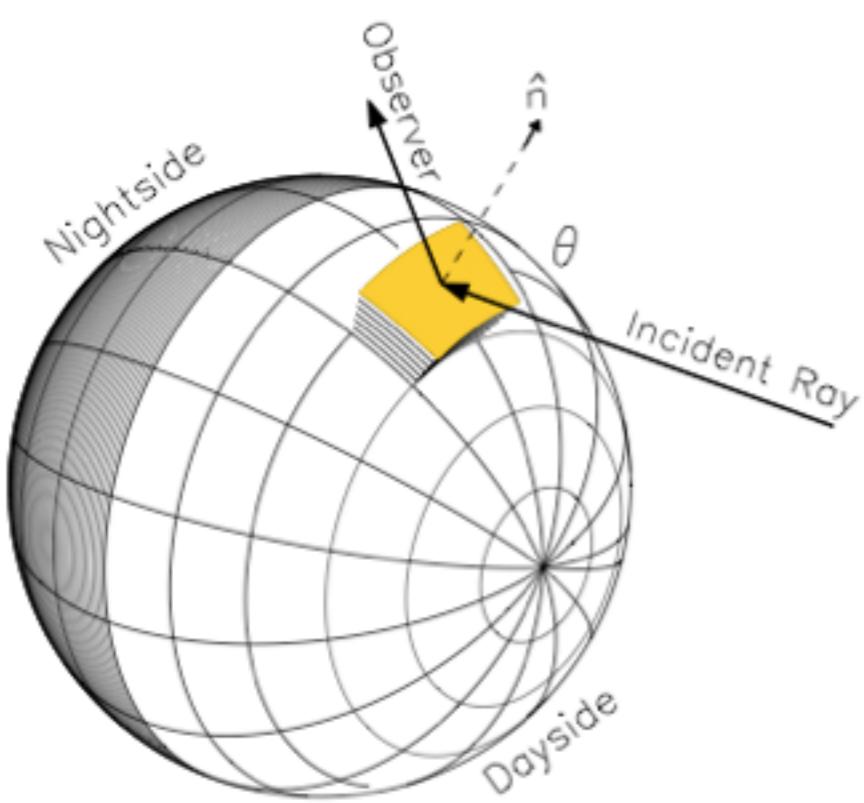
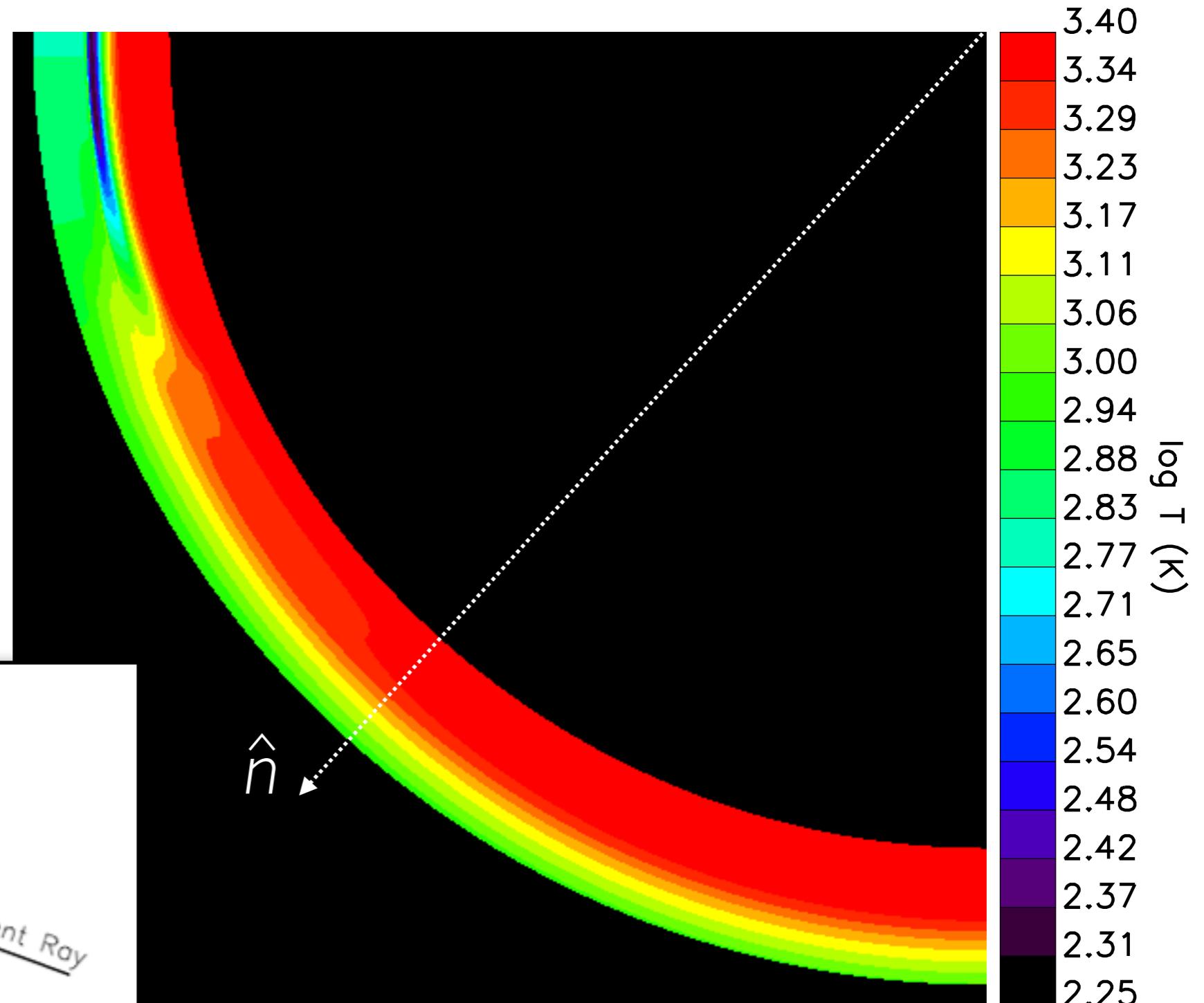
Fortney et al. (2008)

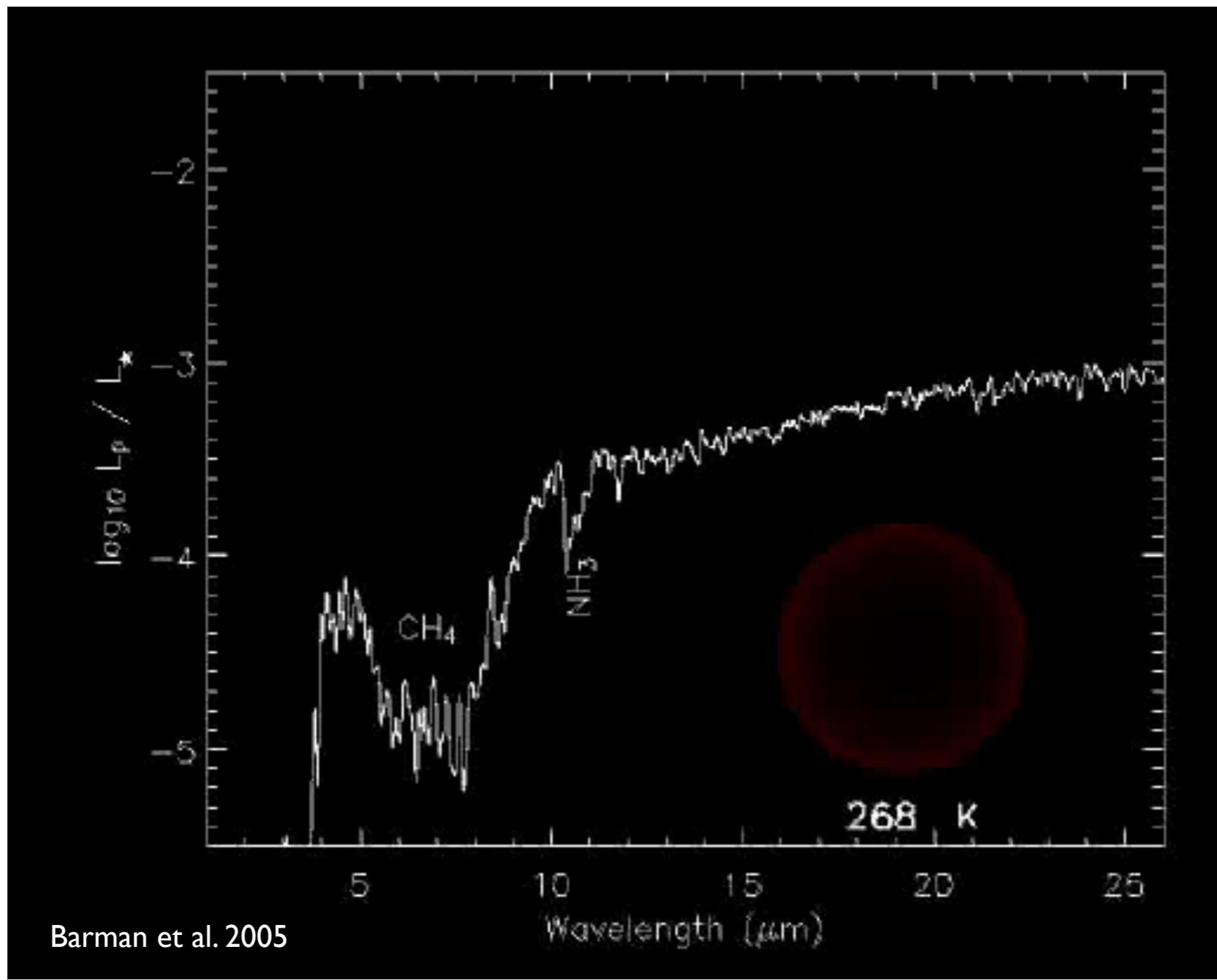


# temperature inversions



# Phase-dependent Properties



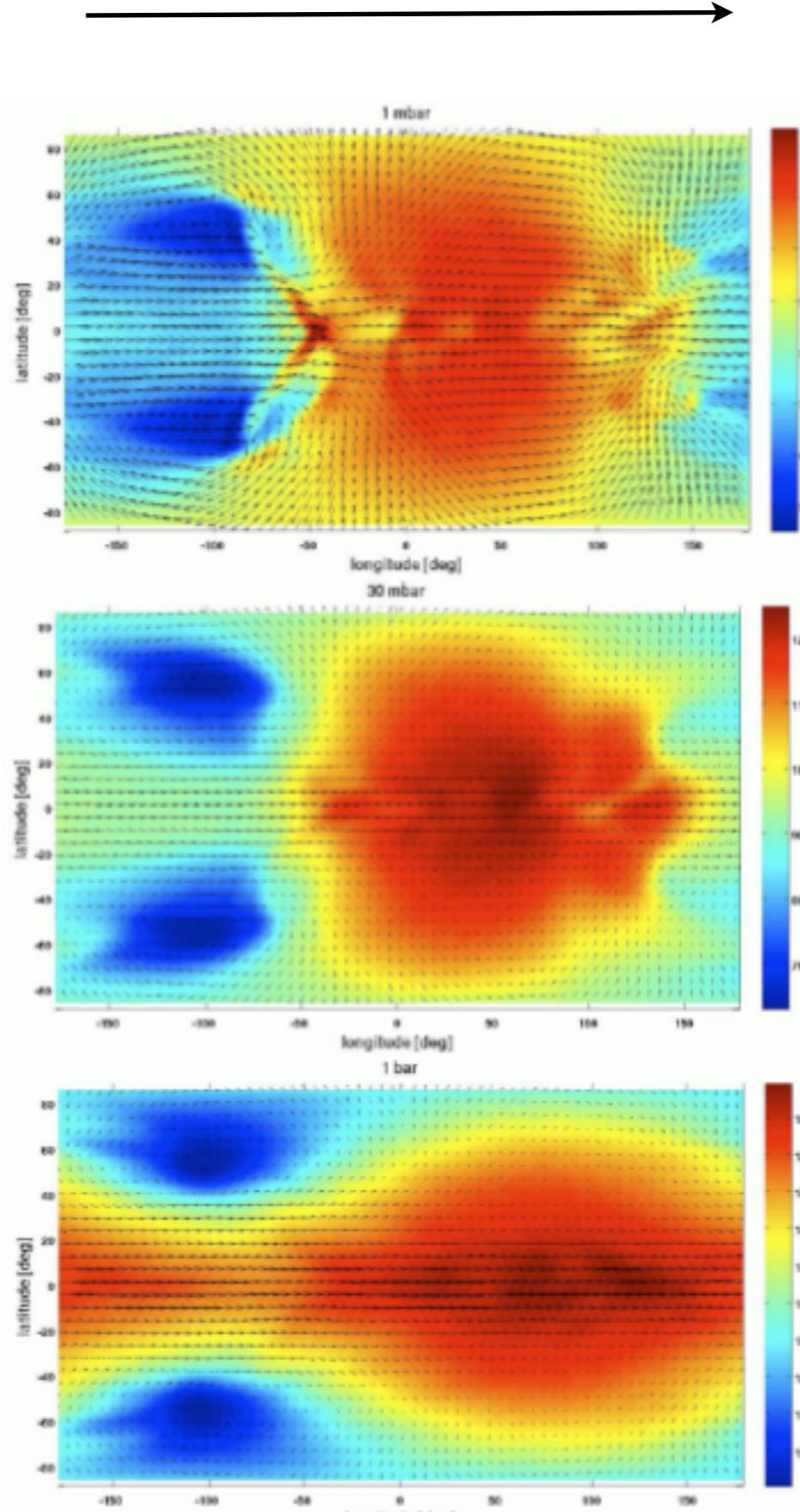


Barman et al. 2005

1200K  
1000K  
750K  
450K

latitude

longitude



1 mbar

30 mbar

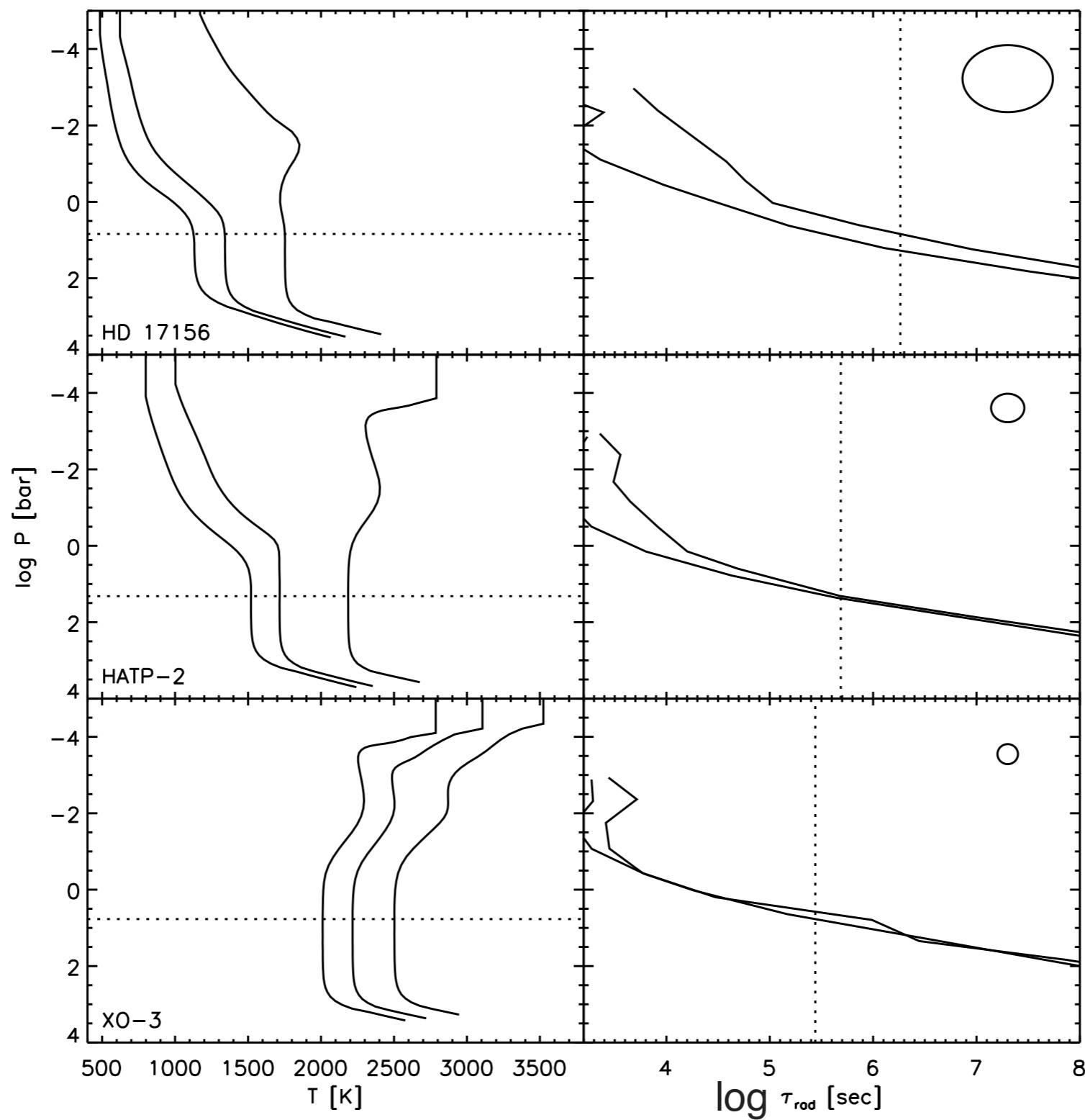
1 bar

# eccentric planets

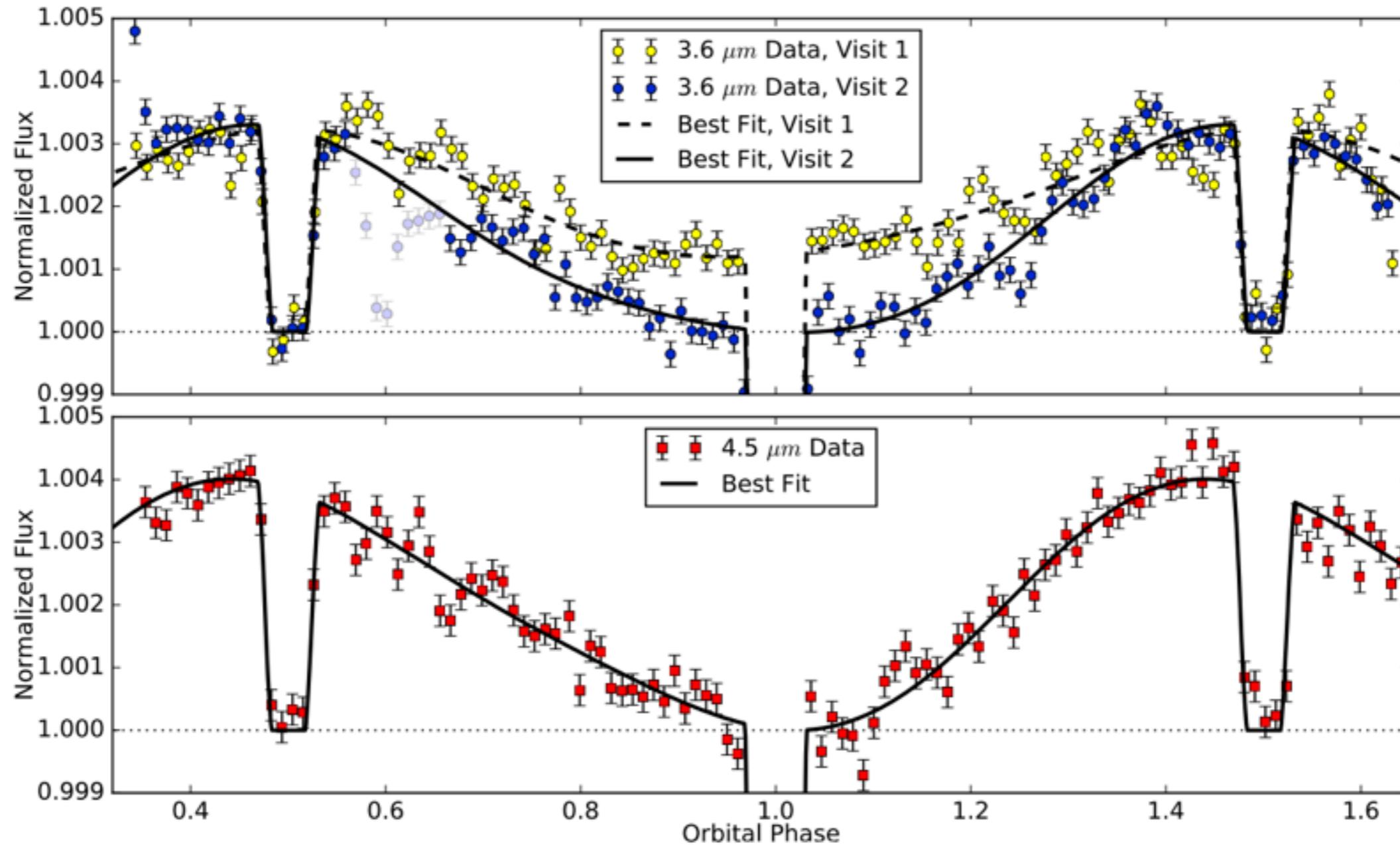
HD 17156b  
 $e = 0.67$

HAT-2  
 $e = 0.52$

XO-3  
 $e = 0.26$



# WASP-43b

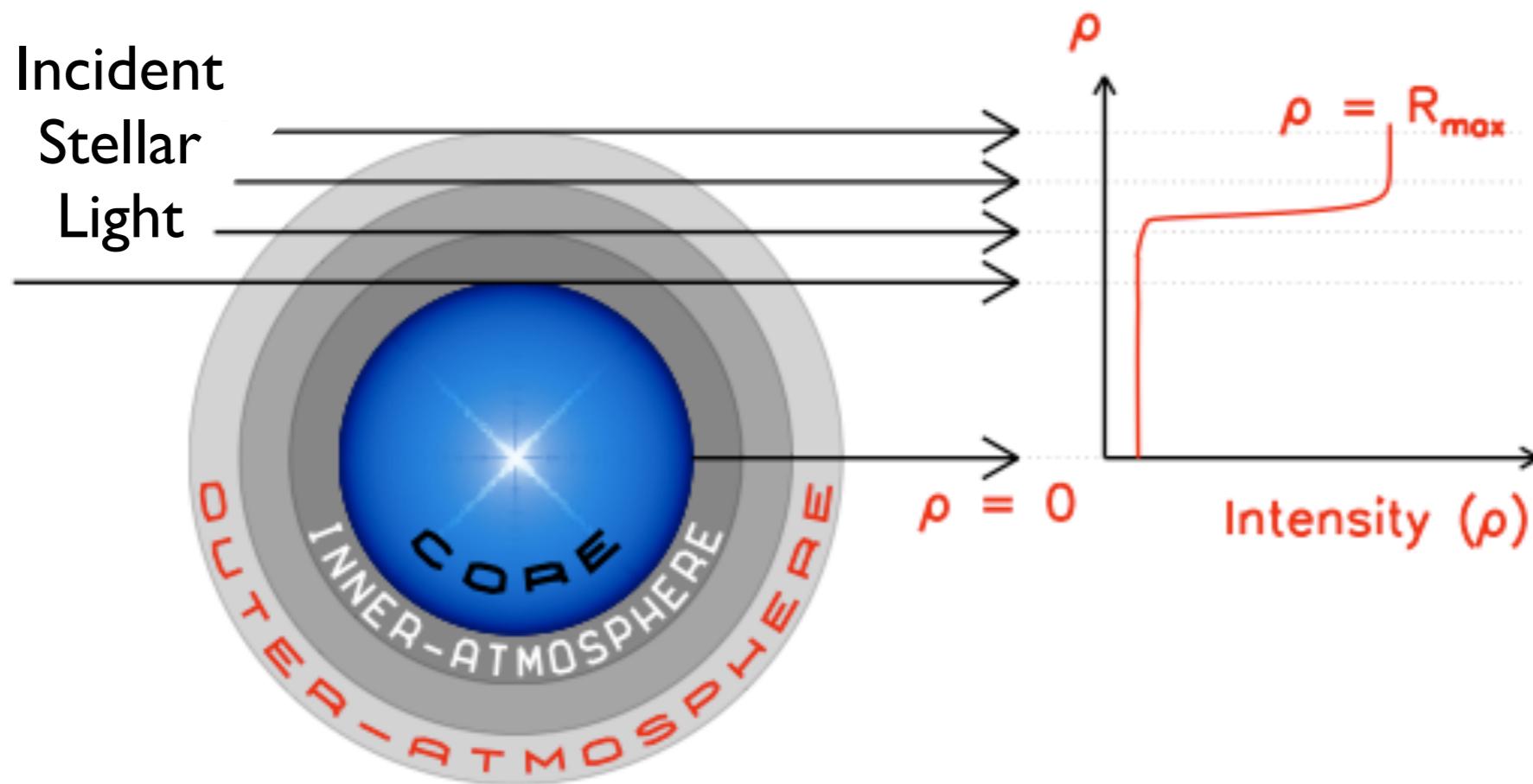


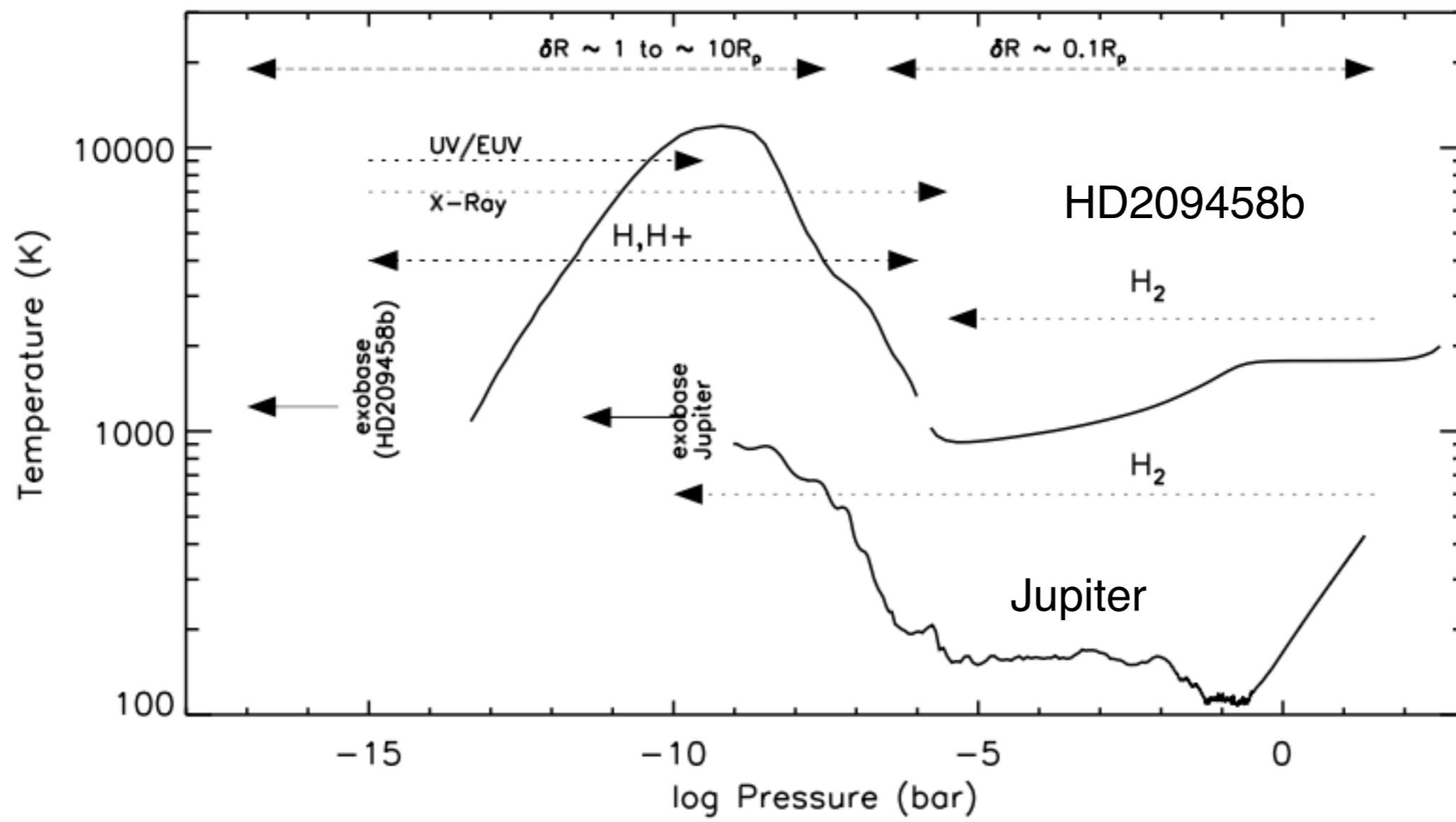
Stevenson et al. (2017)

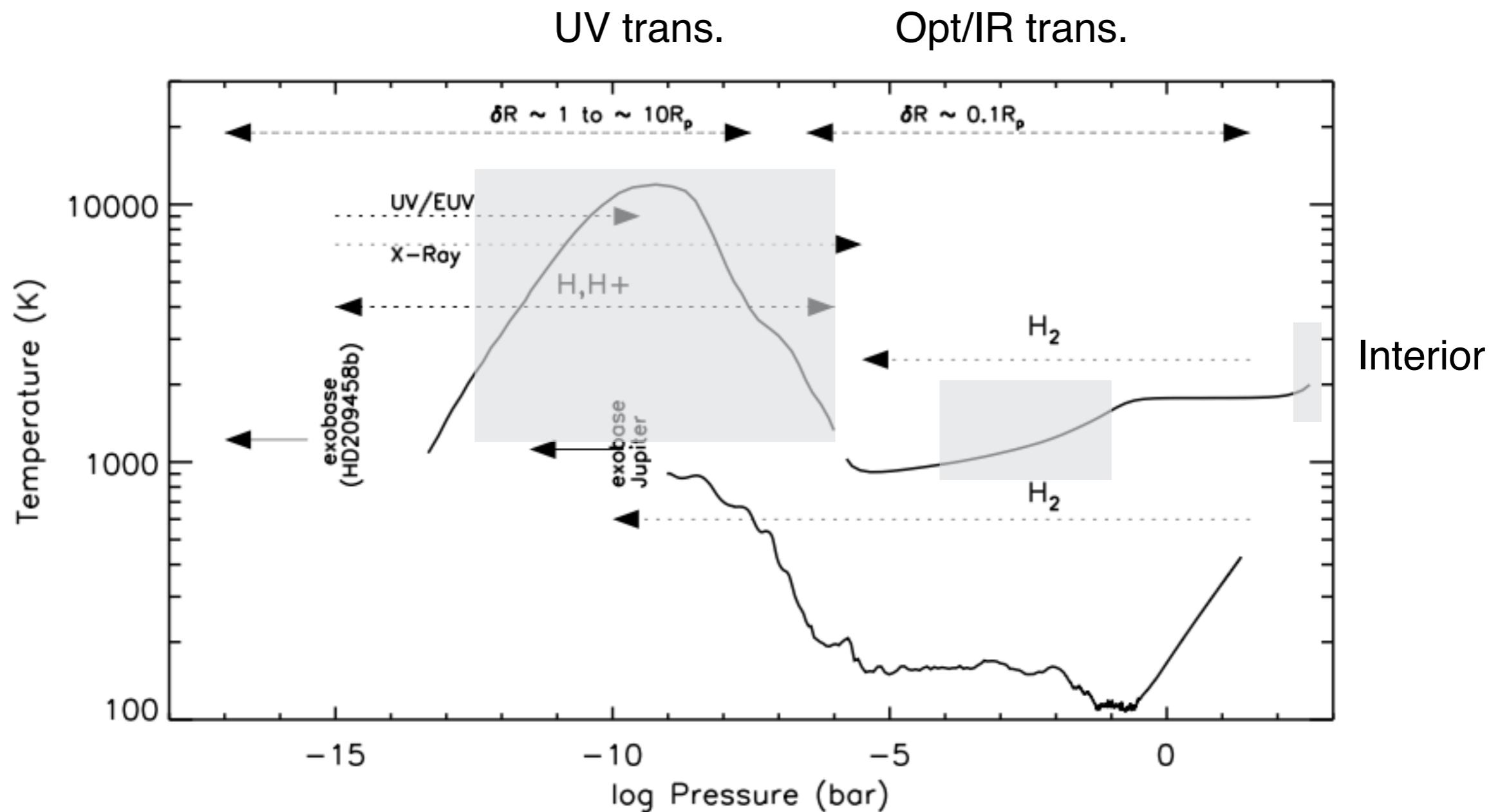
# Exoplanet Atmospheres

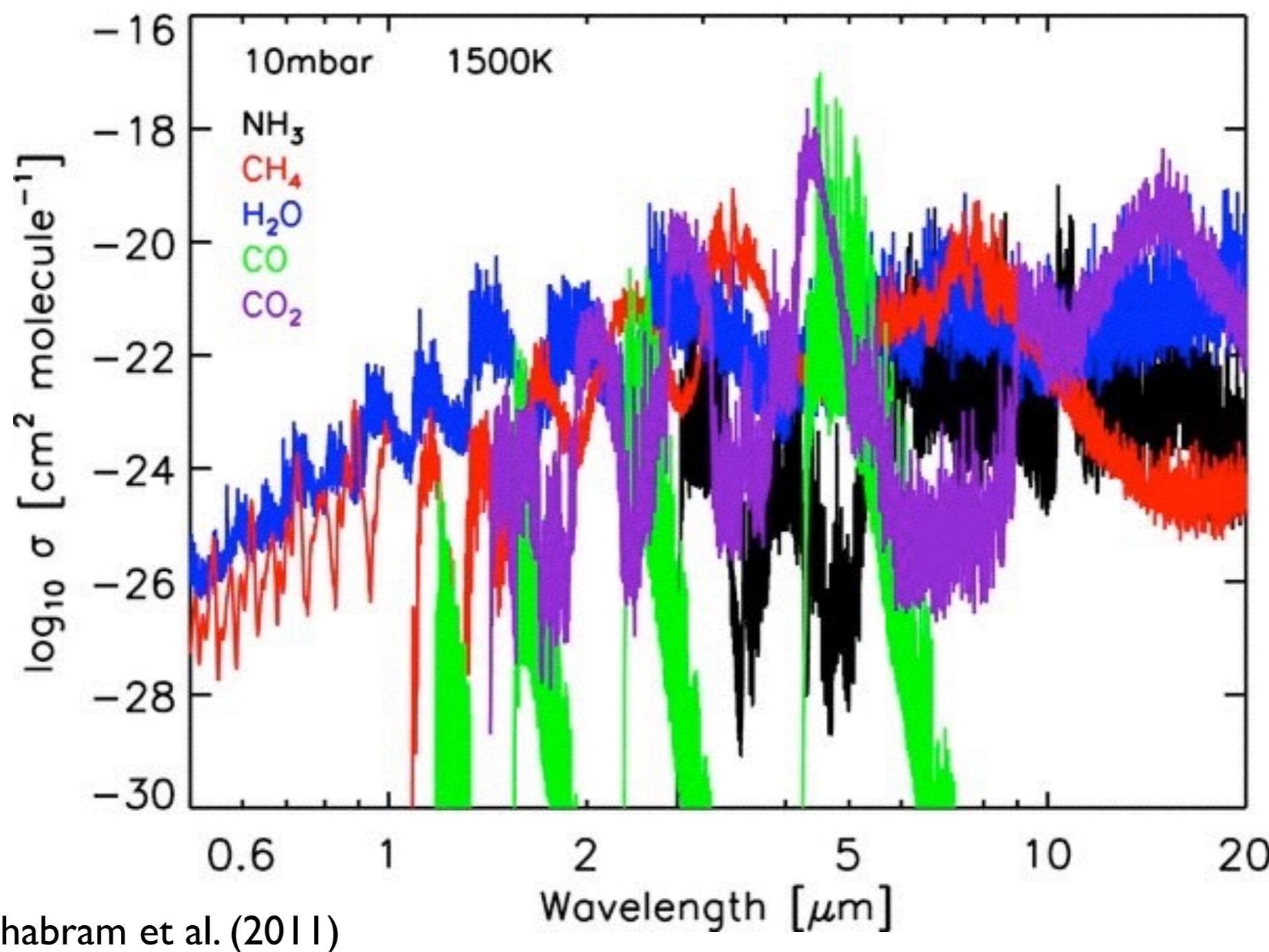
- Secondary Eclipses (e.g., HD 209458b)
- Phase-curves (e.g., HD 189733b)
- Transit spectroscopy (e.g., HD 189733b)
- Spatially Resolved (“directly” imaged)  
(e.g., 2m1207b, HR 8799 bcde)

# Transmission Spectrum (primary eclipse)

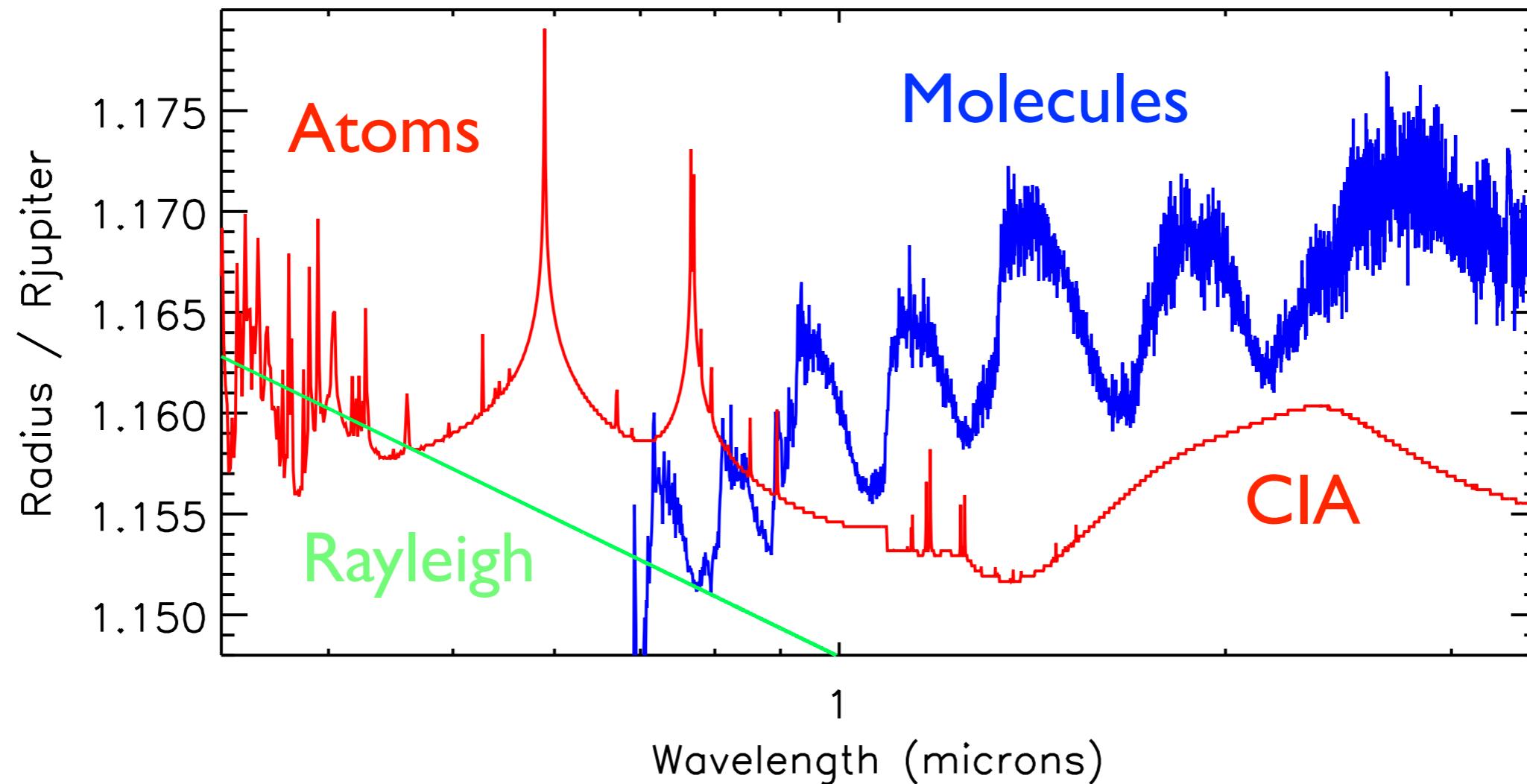


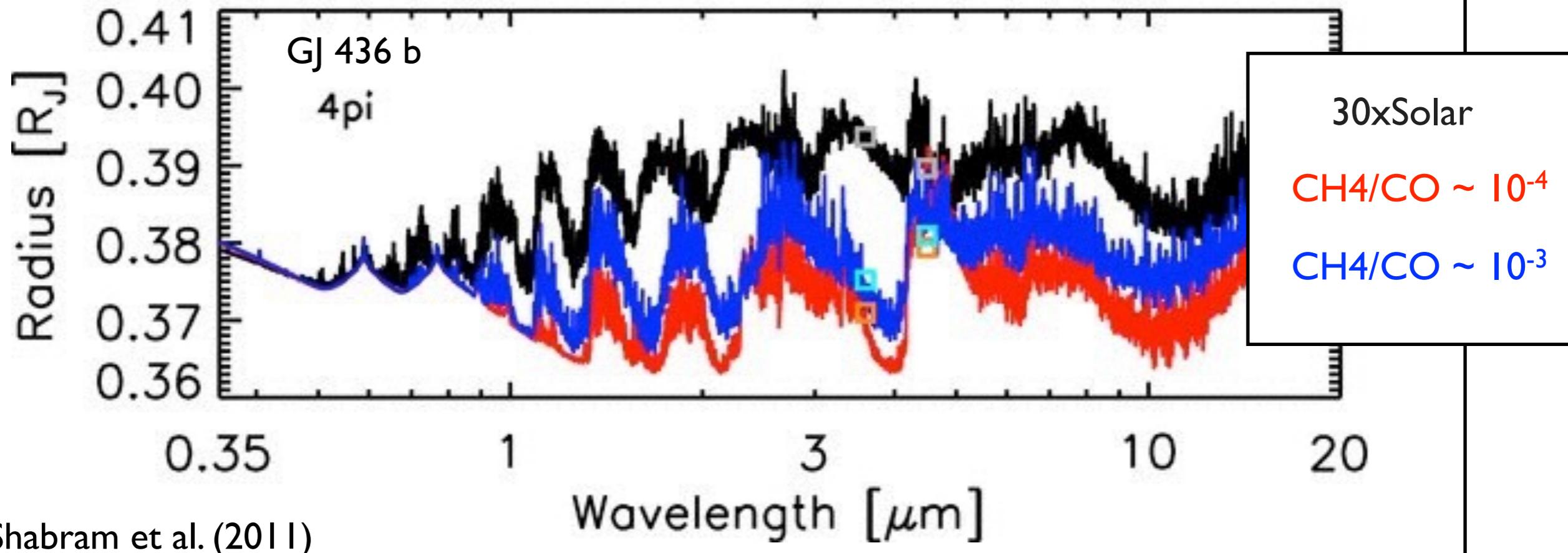


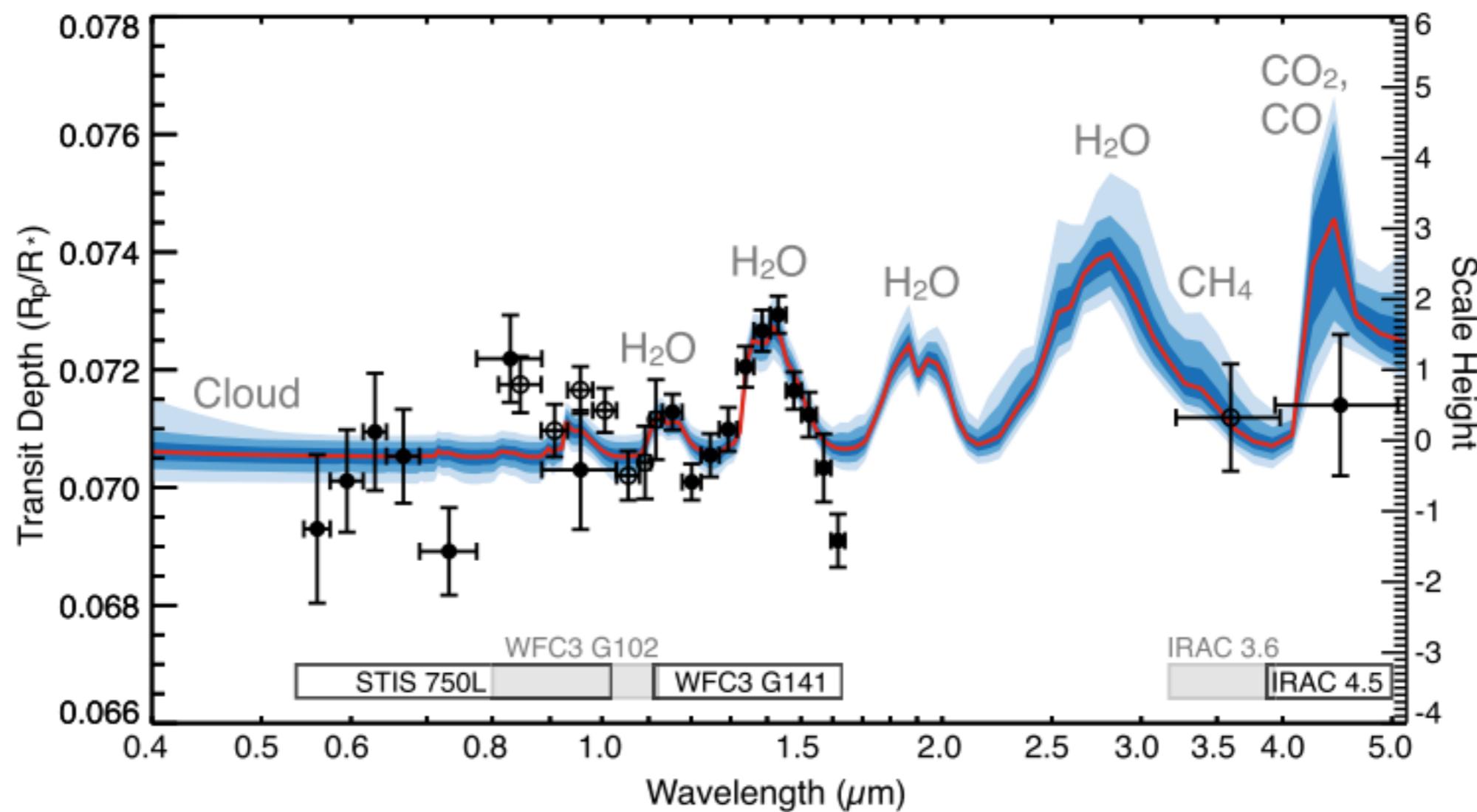




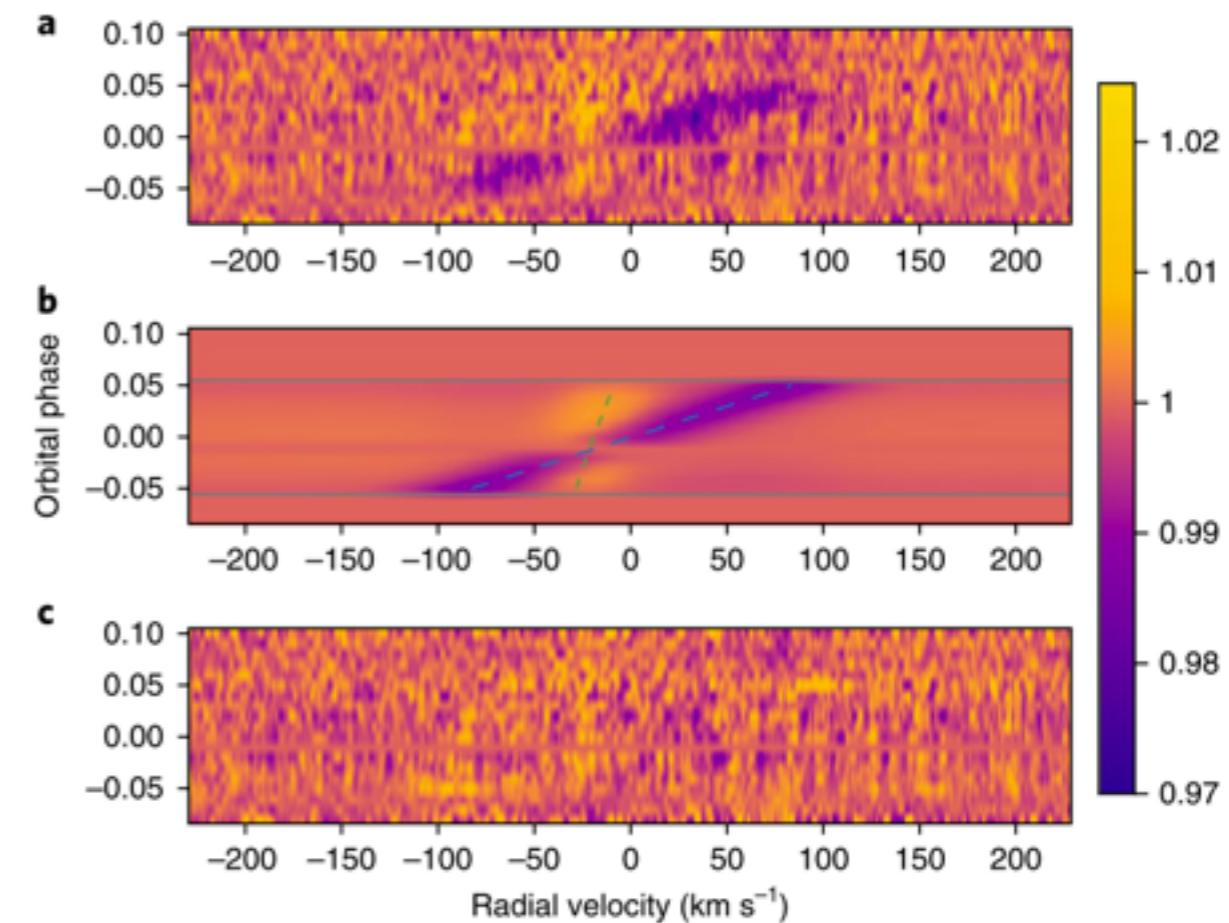
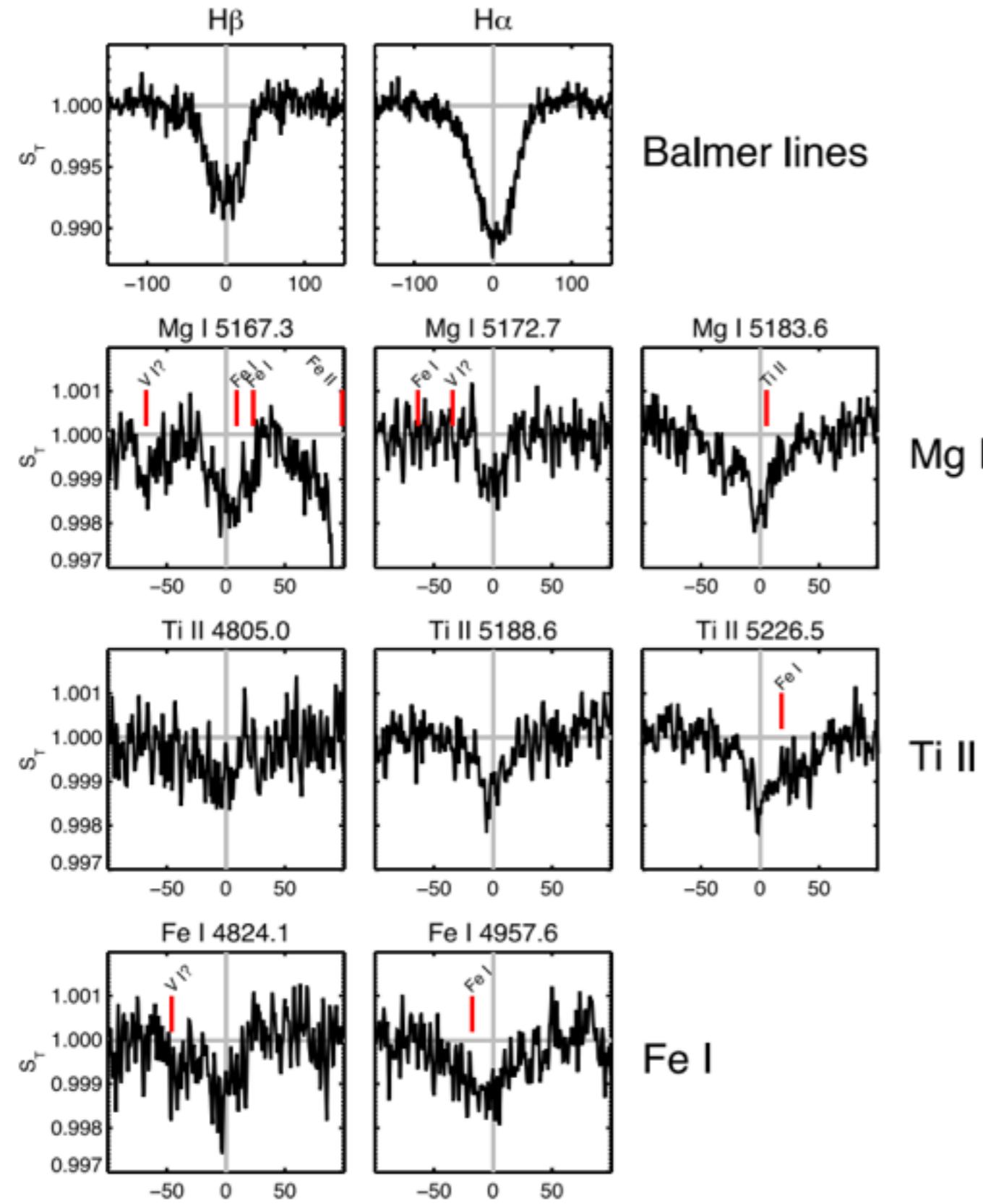
Shabram et al. (2011)







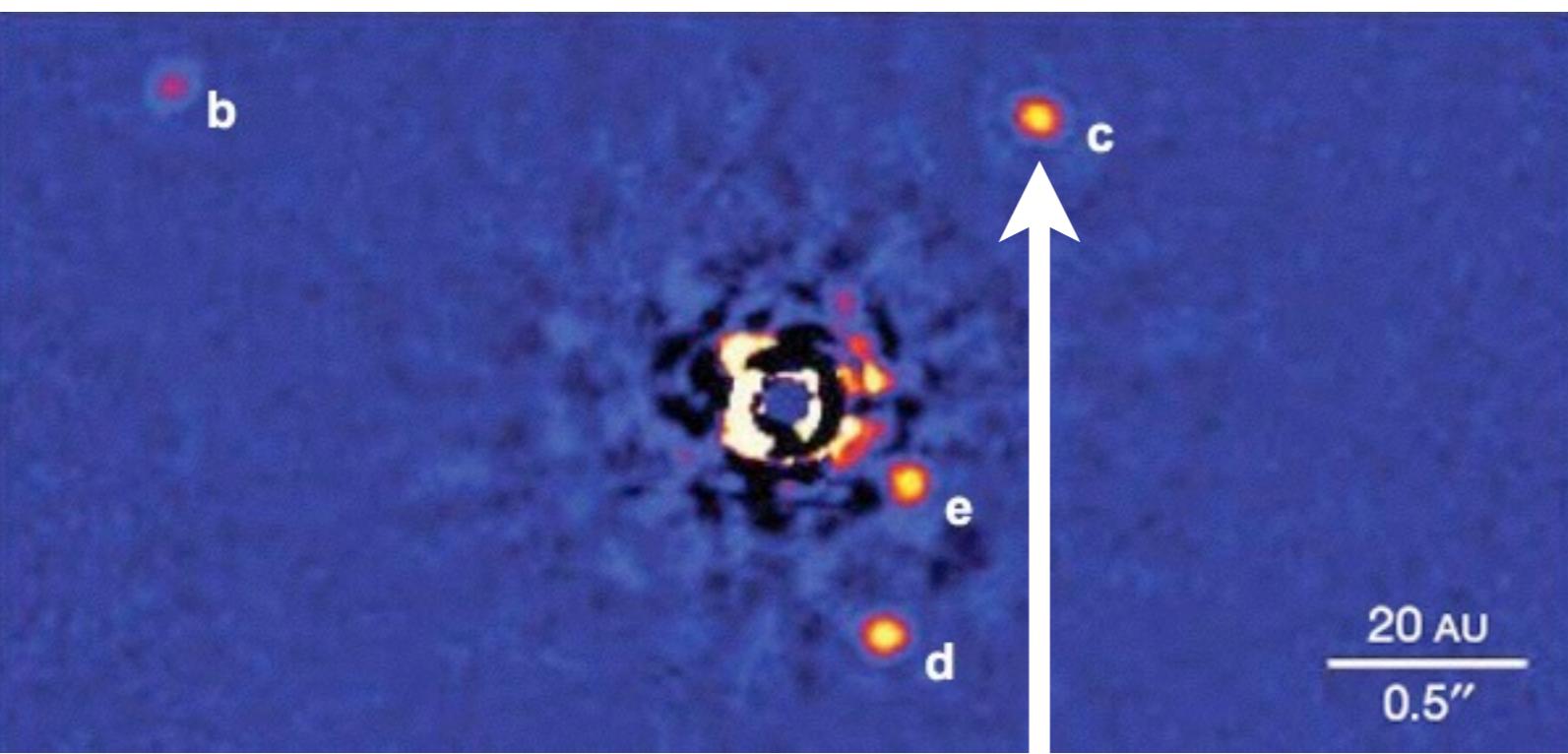
# Kelt9-b, high-resolution transition spectroscopy



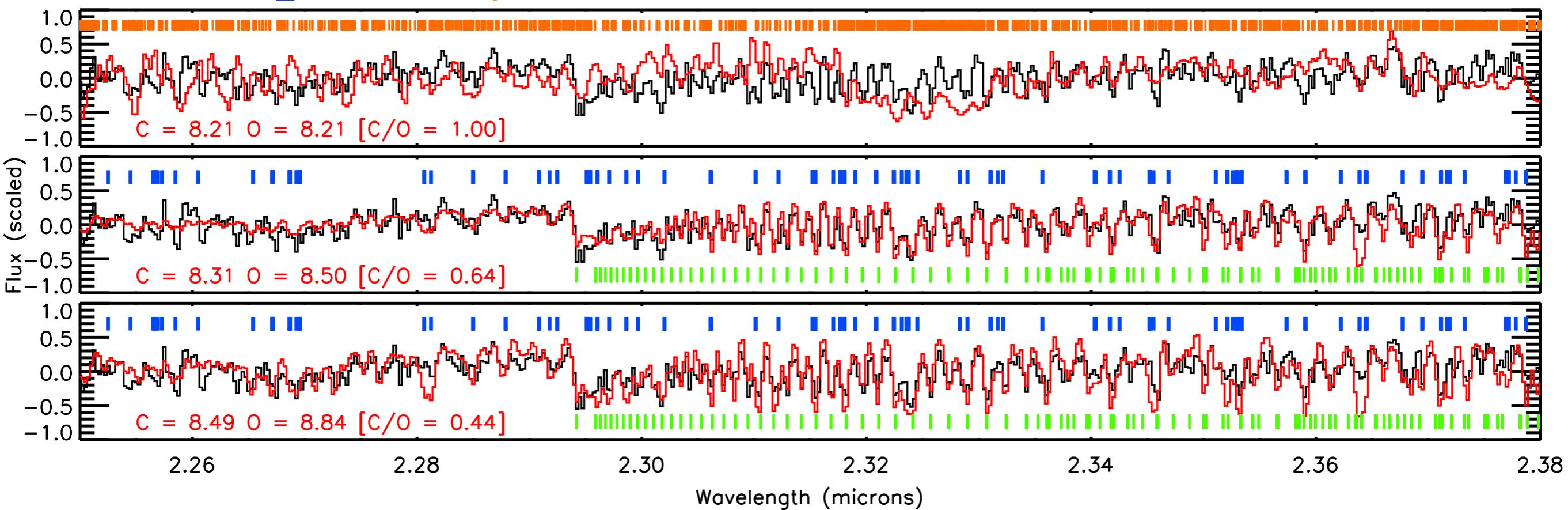
Cauley et al. (2018); Yan et al. 2018

# Exoplanet Atmospheres

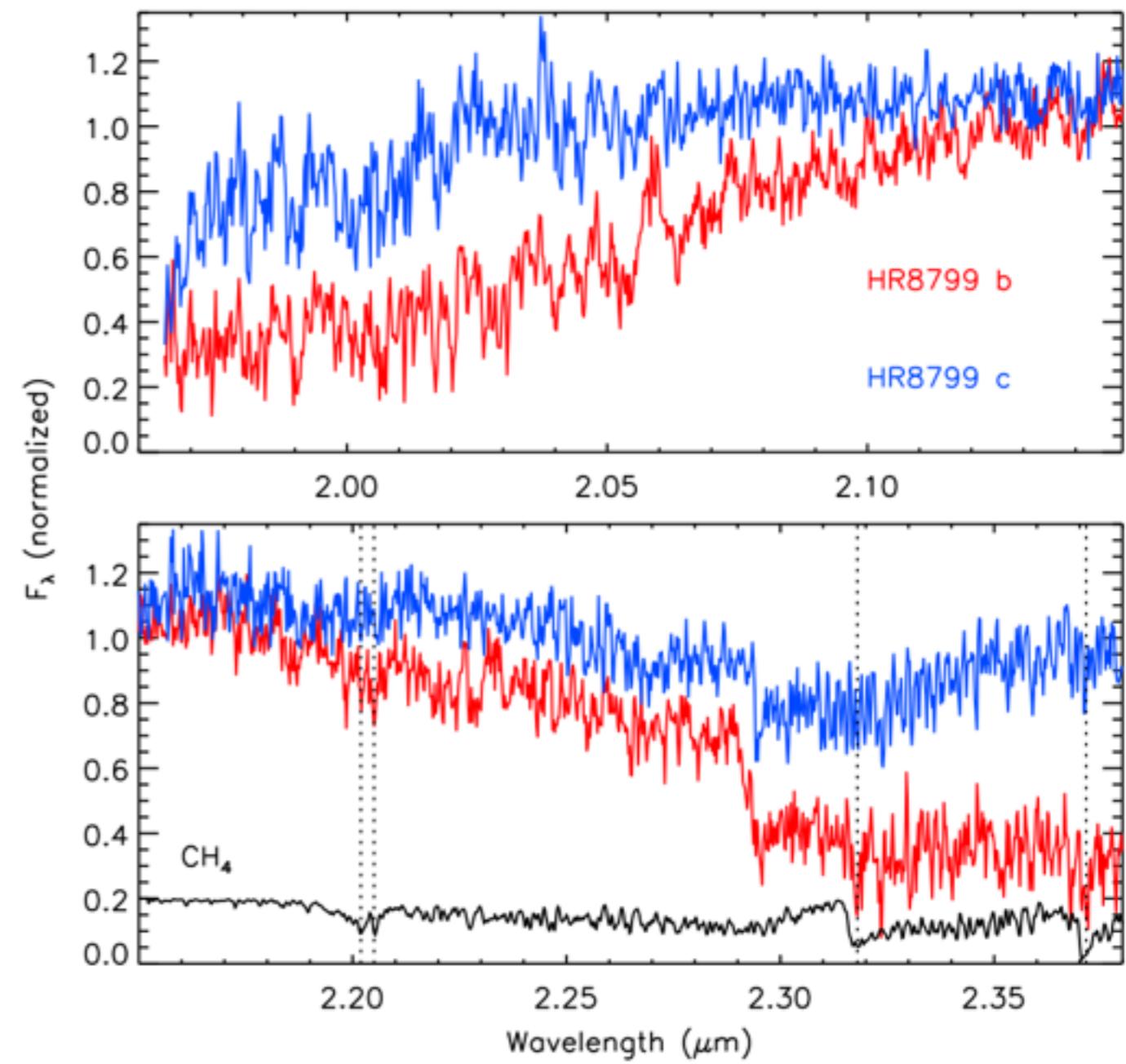
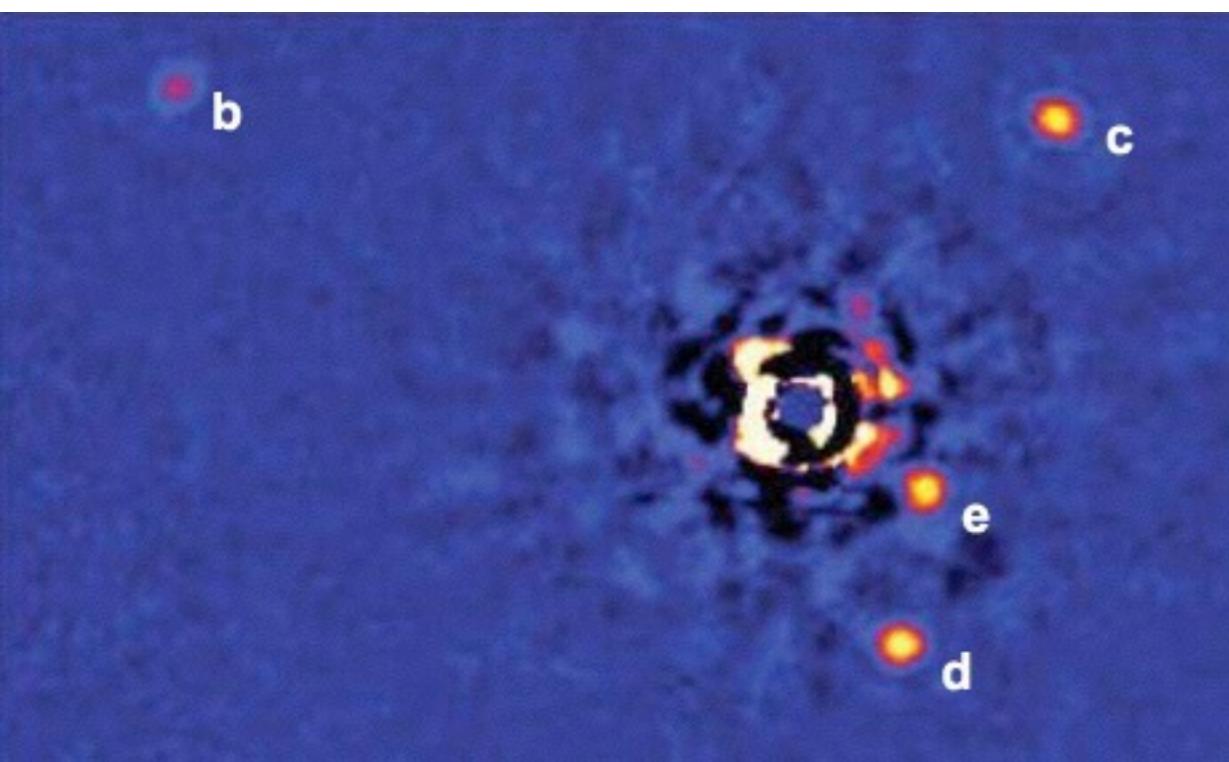
- Secondary Eclipses (e.g., HD 209458b)
- Phase-curves (e.g., HD 189733b)
- Transit spectroscopy (e.g., HD 189733b)
- Spatially Resolved (“directly” imaged)  
(e.g., 2m1207b, HR 8799 b, c, & d)

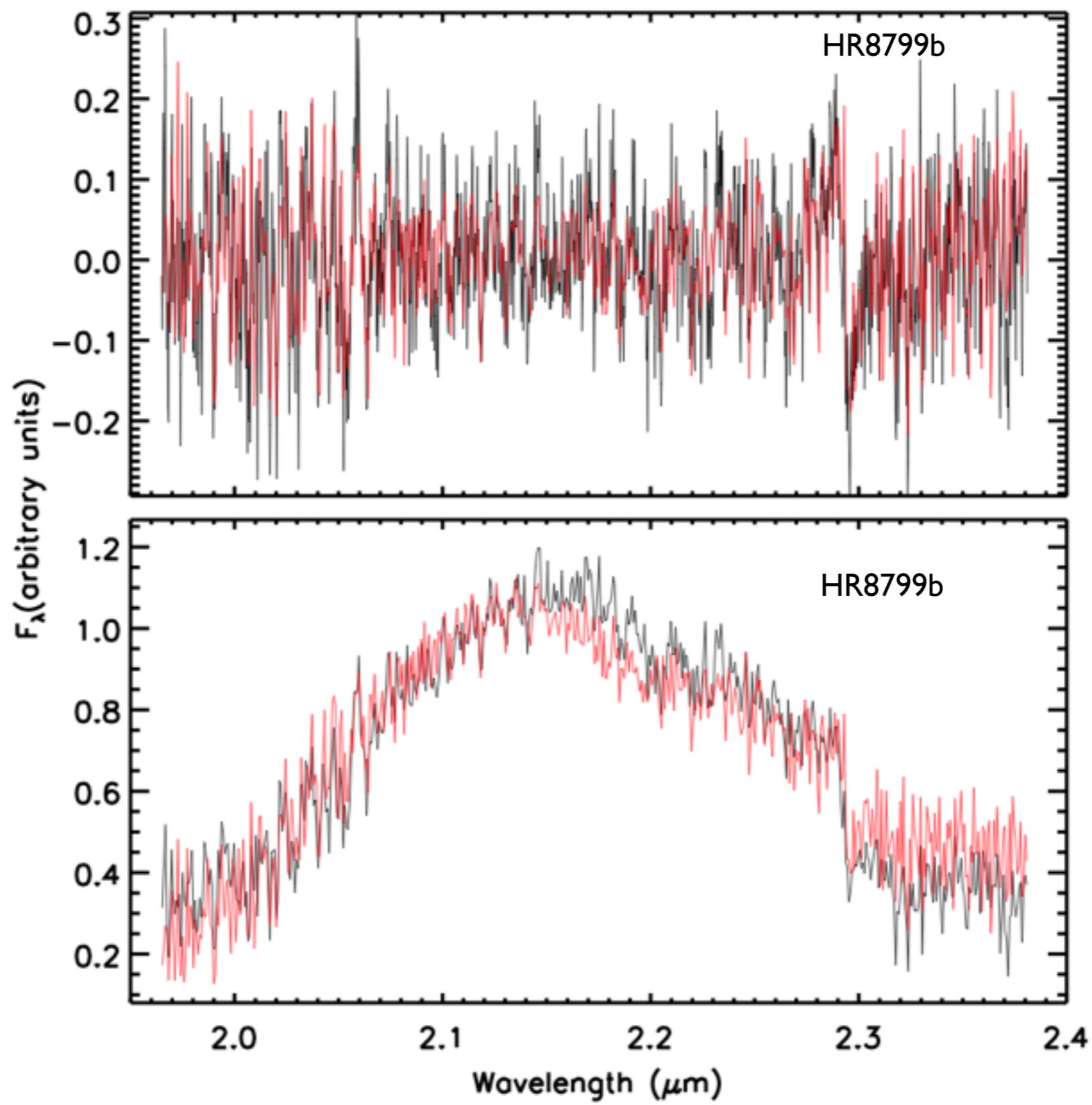


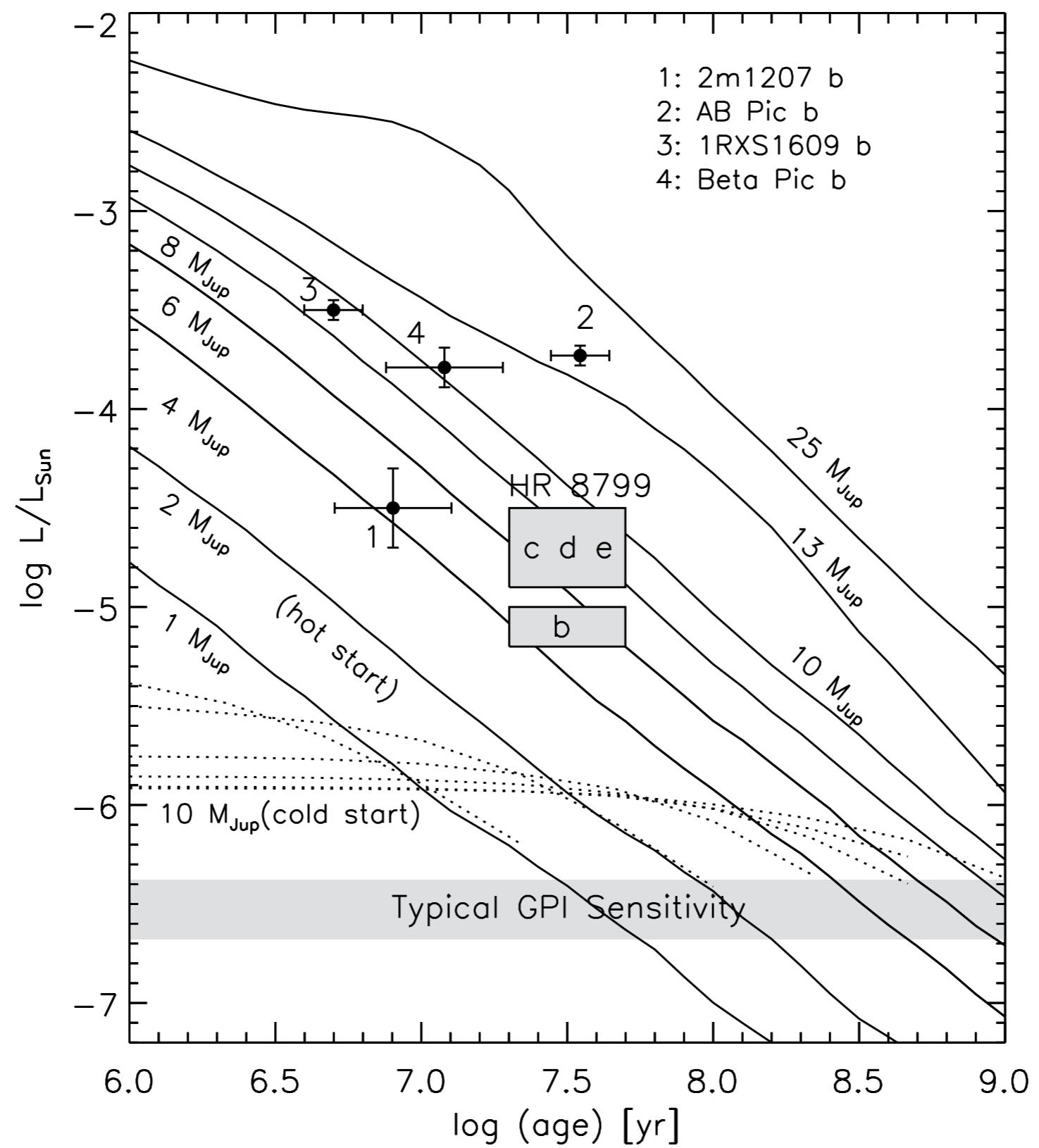
CO H<sub>2</sub>O CH<sub>4</sub>



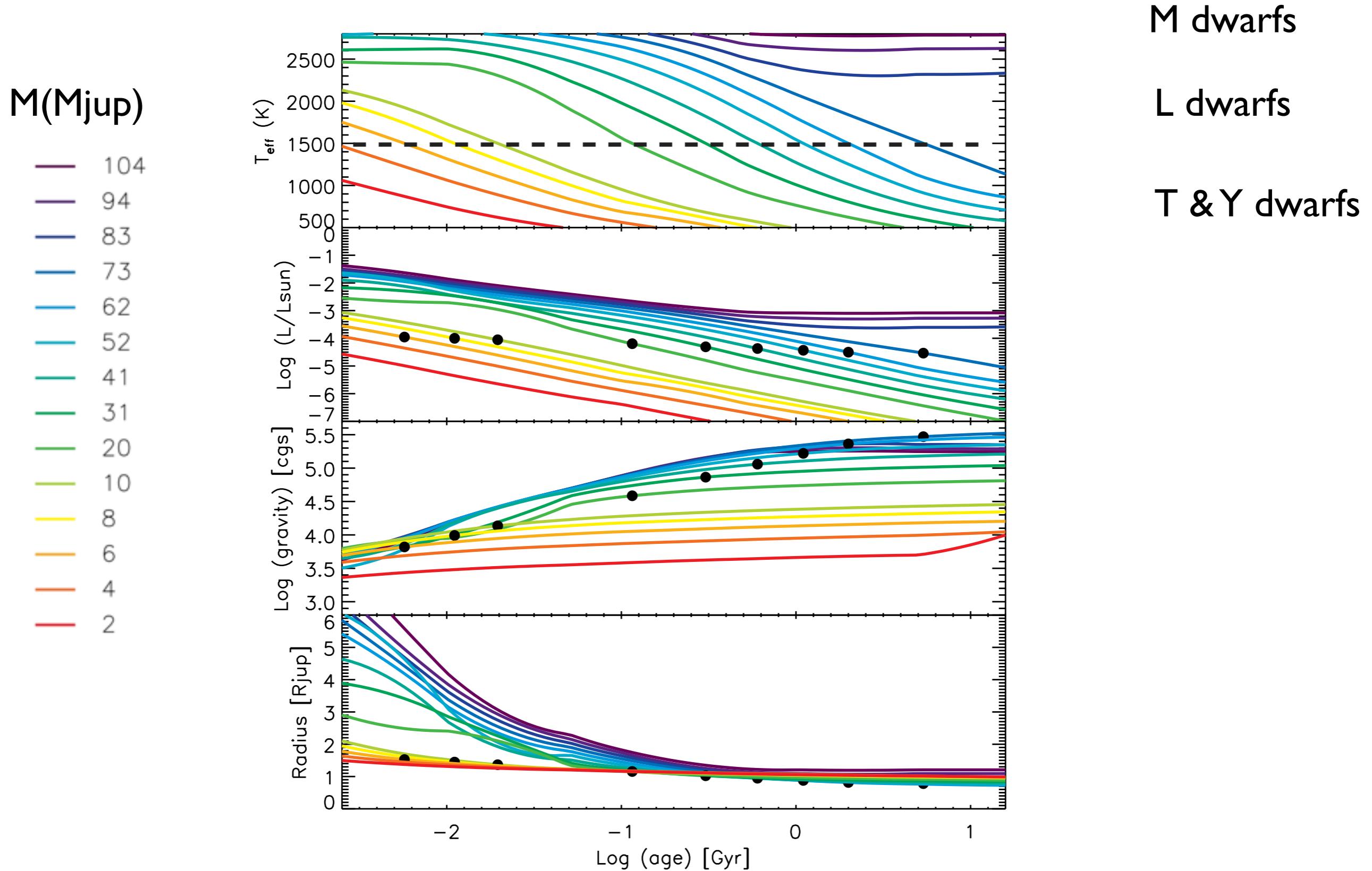
Konopacky, Barman, Macintosh & Marois (2013)



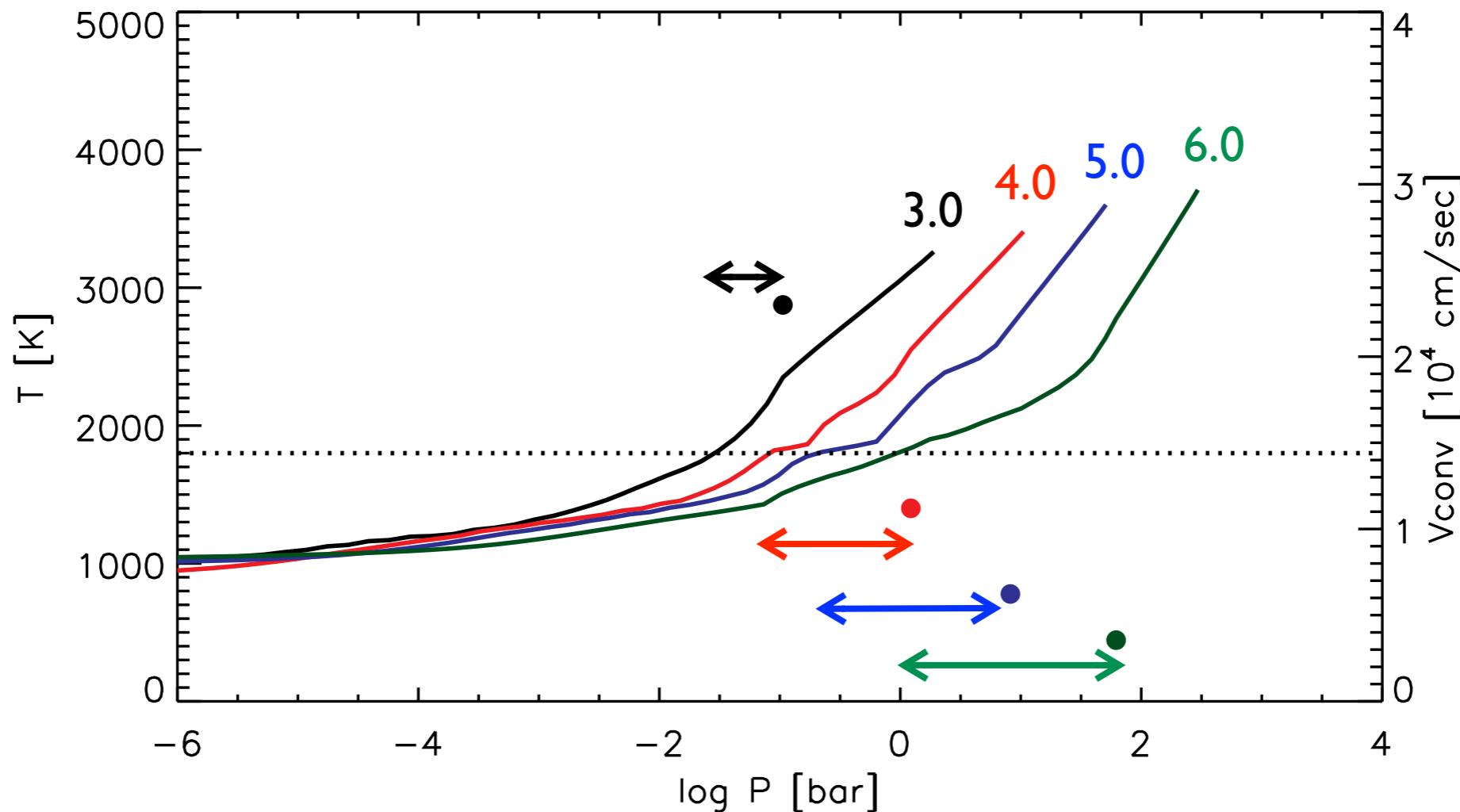




# The importance of surface gravity:

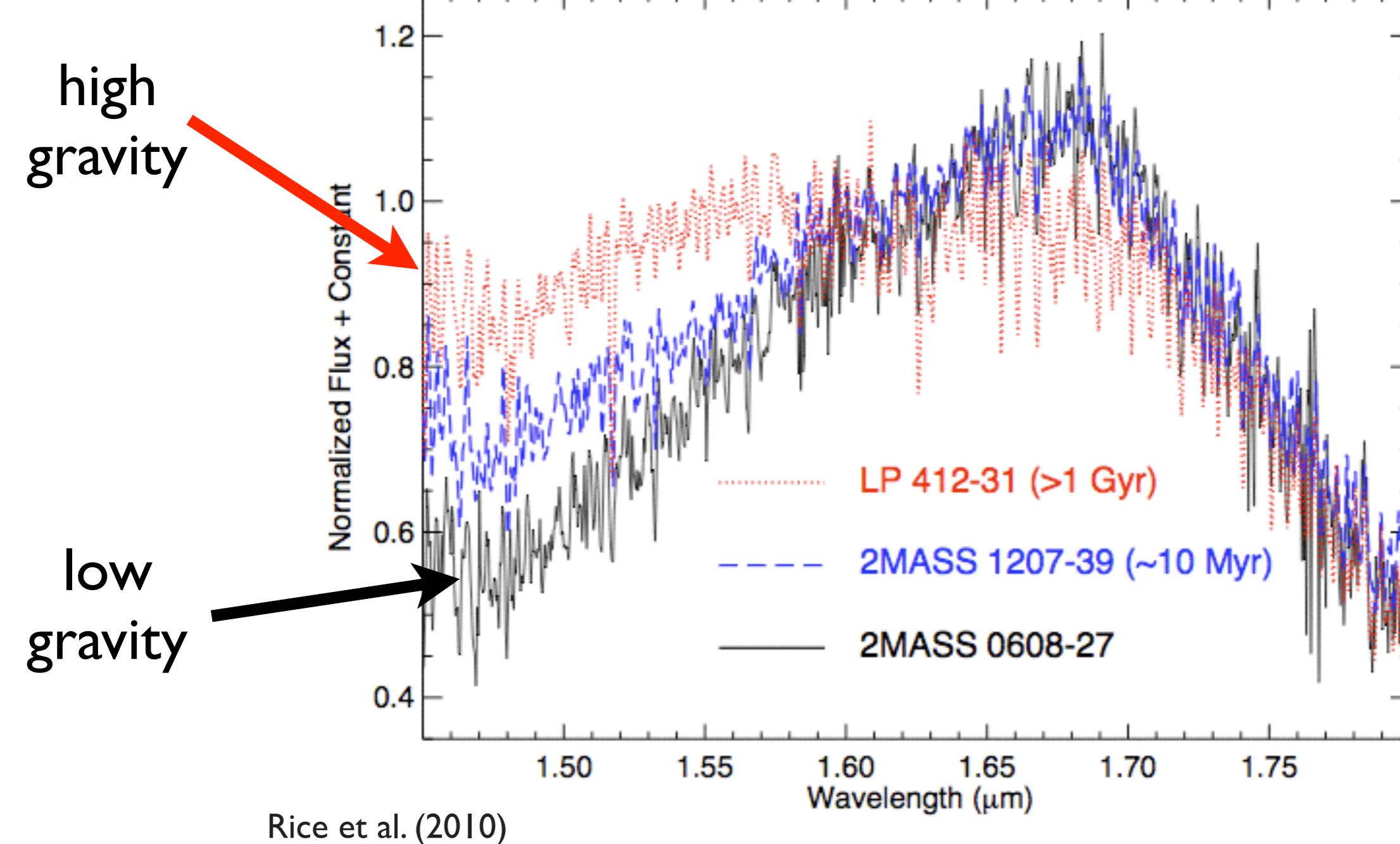


# Convection and Gravity



Relative positions of photosphere and top of convection zone (cz). Vertical position indicates convective velocities at top of cz.

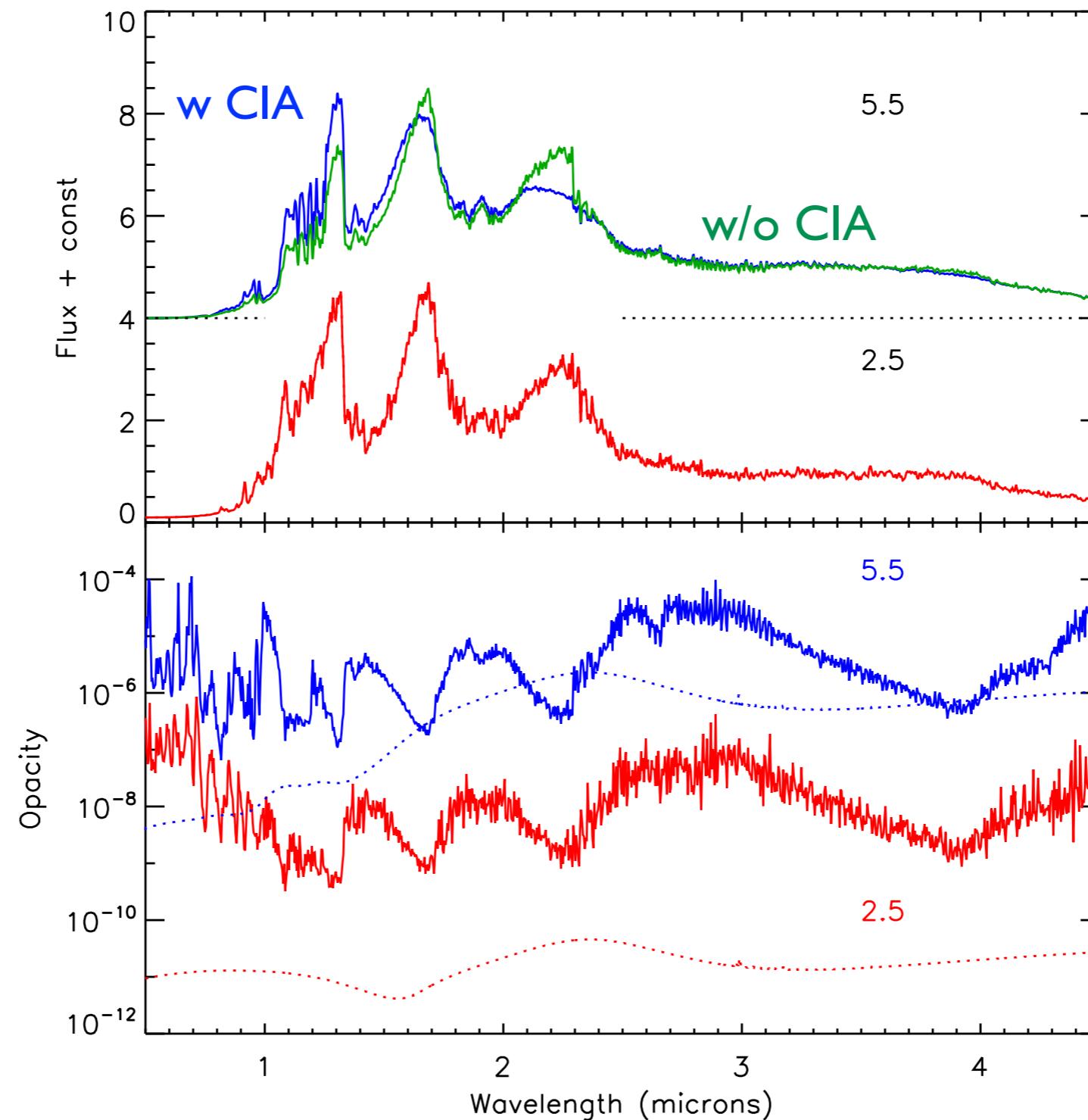
# H-band (triangular shape)



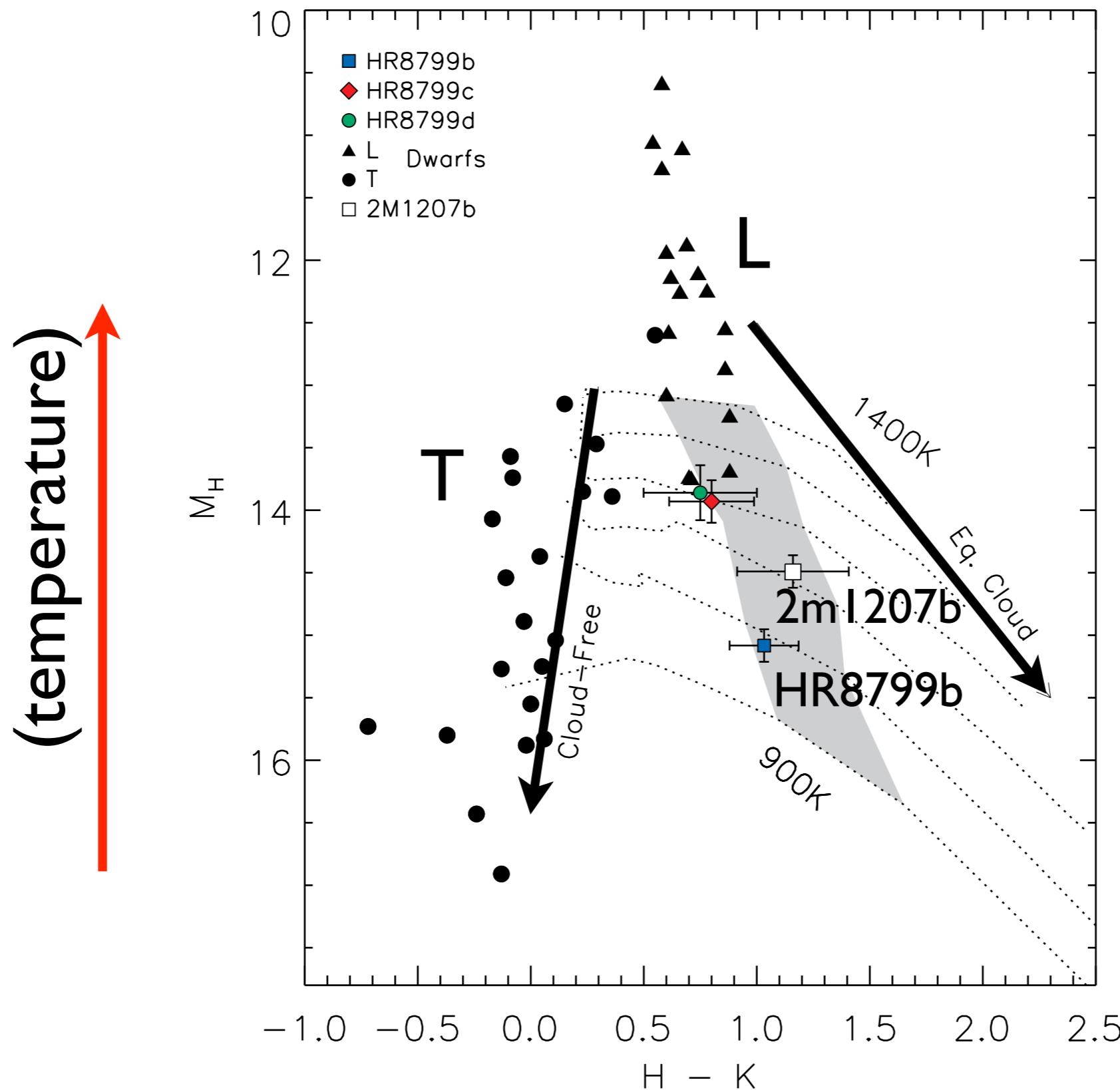
See also Allers et al. (2007) and refs for more examples.

# H-band (triangular shape)

CIA:  
lower gravity  
changes H and  
K bands, also  
makes spectrum  
redder



(see Borysow et al. 1997, Kirkpatrick et al. 2006)

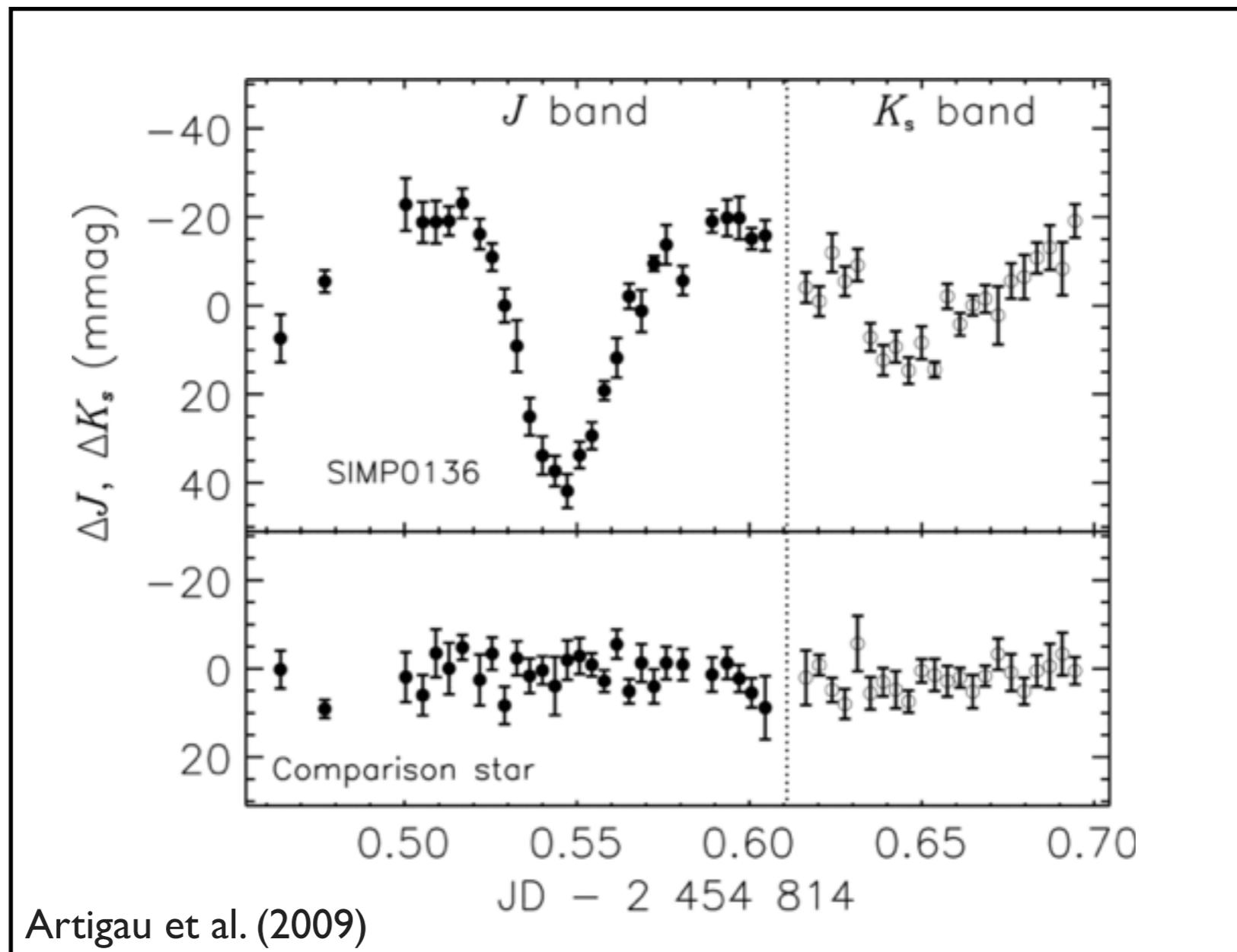


(clouds)

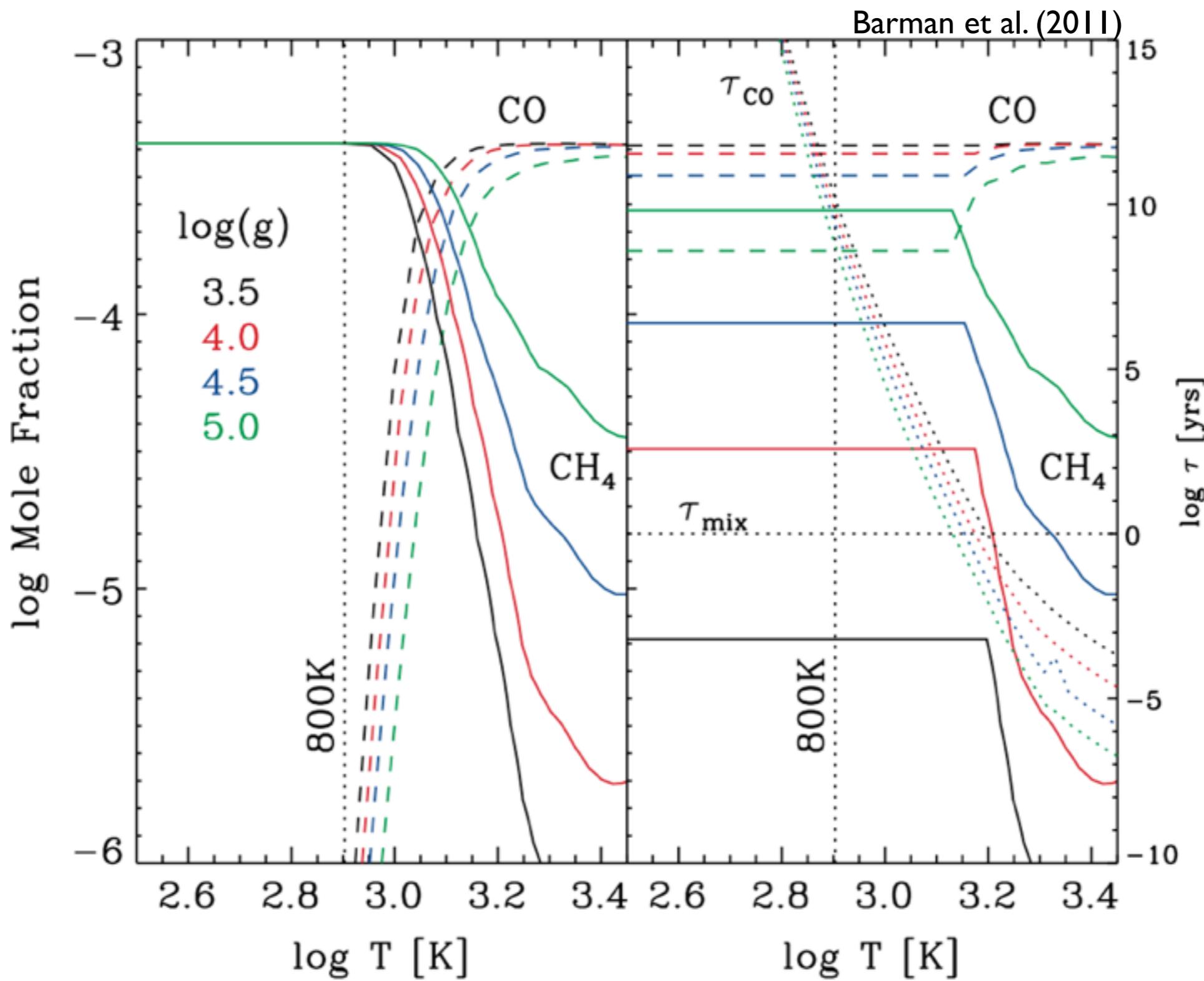
ext. of L  
sequence?

Barman et al. (2011)

# “Weather” in a T-type brown dwarf:



# disequilibrium chemistry (by mixing)



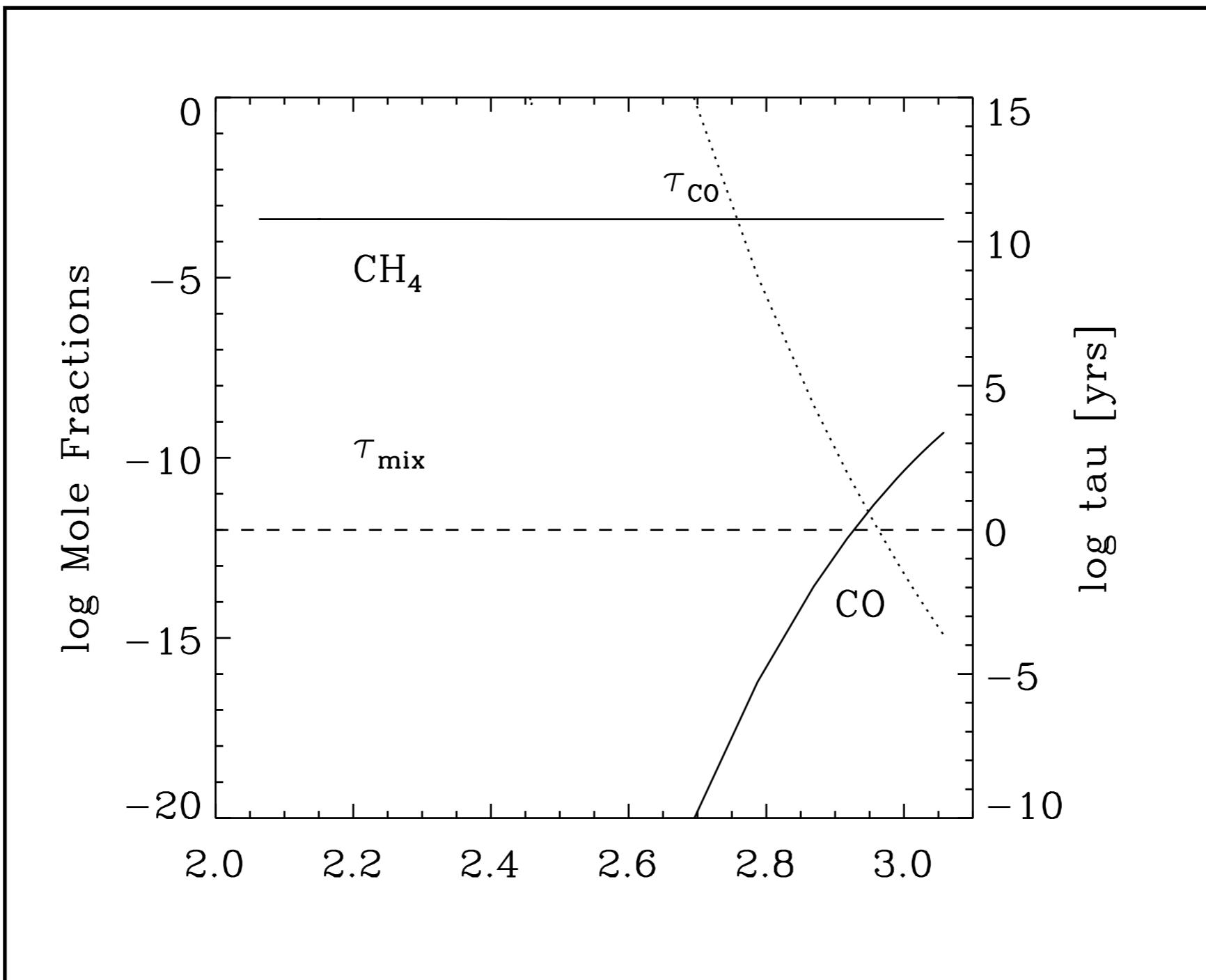
Zahnle & Marley (2014)

Hubeny & Burrows (2007);  
Moses et al. (2011)

$$t_{dyn} = \frac{L^2}{K_{edd}}.$$

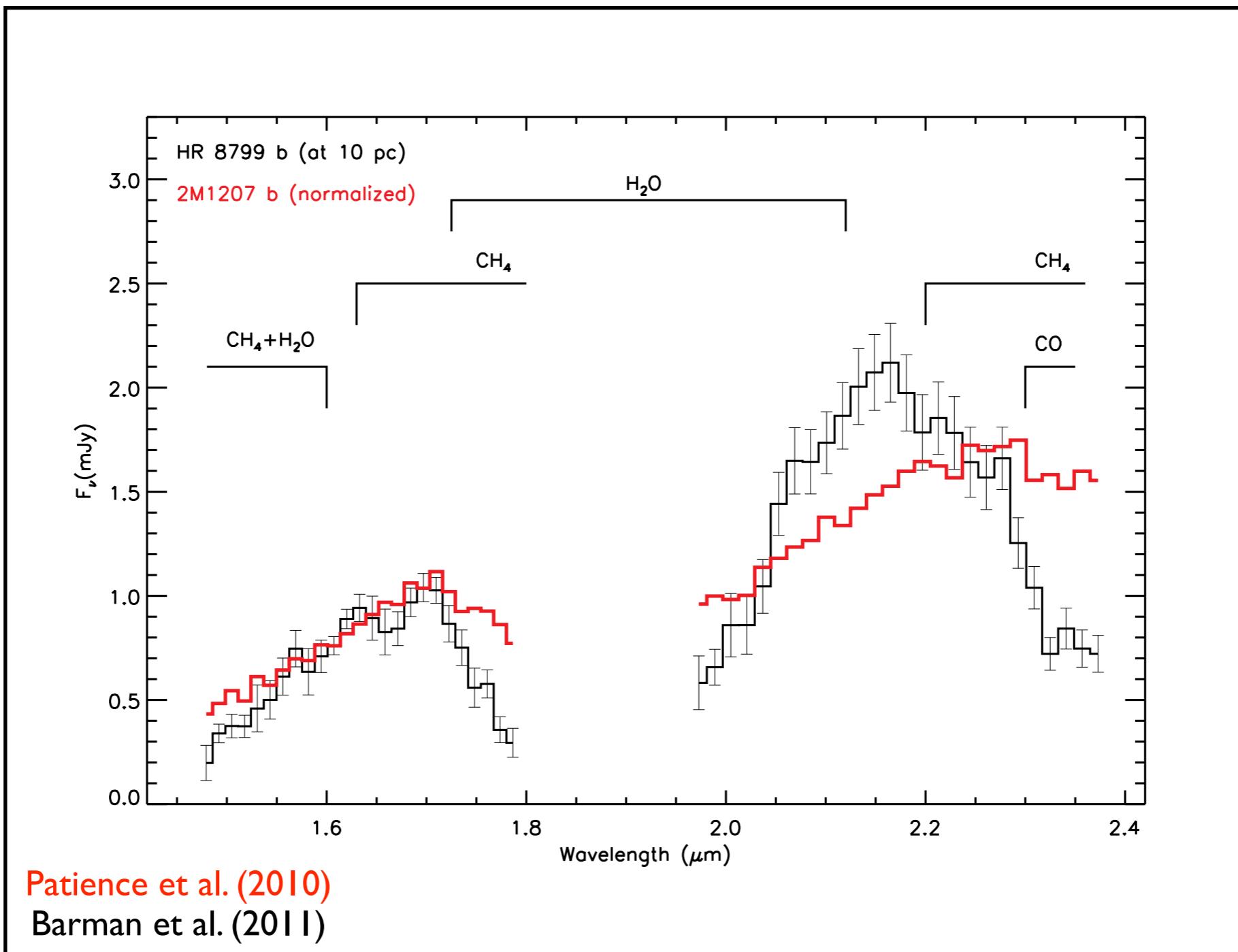
$$t_{chem}(CO) = \frac{1}{2.3 \times 10^{-10} K_a \exp(-36200/T) [H_2]^2} s,$$

# Jupiter ...

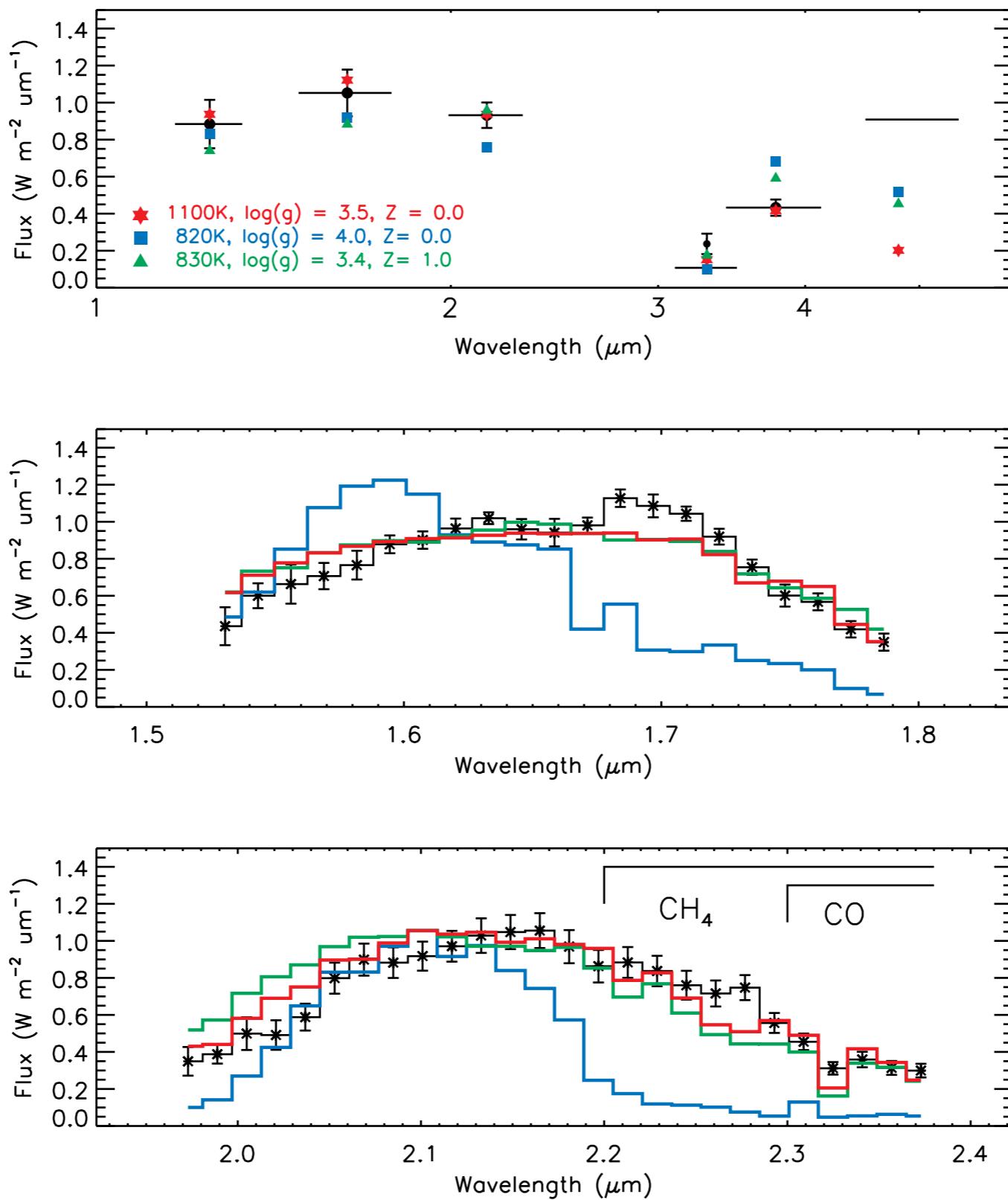


see Visscher et al. (2010)

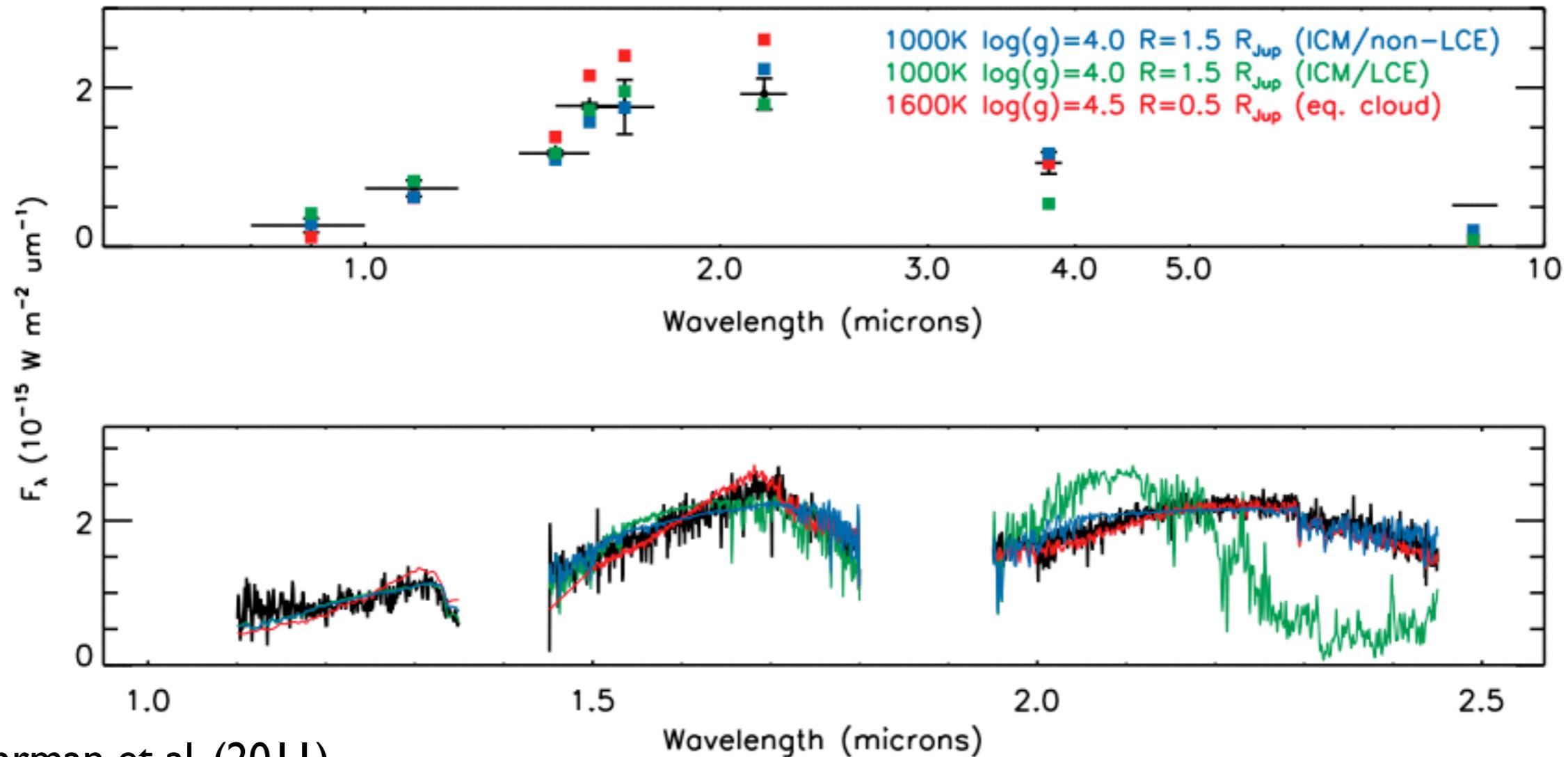
# Direct Spectroscopy of planets: 2M1207b, HR 8799 b



# HR8799 b



# 2M1207b, 1000K and Methane-poor (non-eq CO/CH<sub>4</sub> & clouds)



Barman et al. (2011)

# 2M1207 b

